

Supplementary Materials for:

Tuning the Electronic and Quantum Transport Properties of Nitrogenated Holey Graphene Nanoribbons

Table S1: Relative Energies of armchair and zigzag ($n_{a/z}$) C₂N-hNRs in different Magnetic states.

$n_{a/z}$ C ₂ N-hNRs	NM(meV)	AFM(meV)	FM(meV)
3A	22.6	19.2	0
7A	14.1	0.02	0
11A	18.6	10.02	0
4Z	0	0.01	
10Z	0	0.13	
12Z	0	0.09	

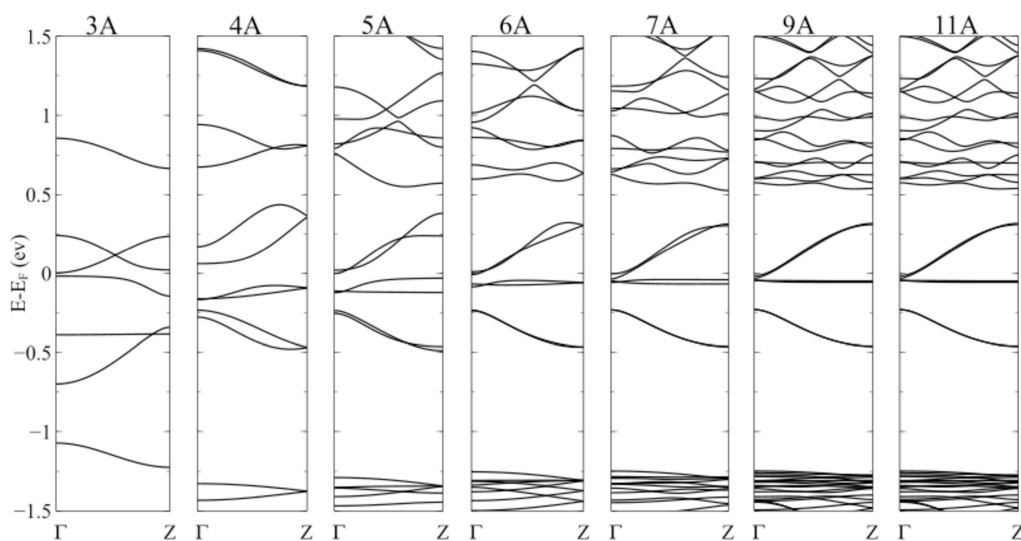


Figure S1: Evolution of band structures for 3A, 4A, 5A, 6A, 7A, 9A and 11A C₂N-hNRs, respectively.

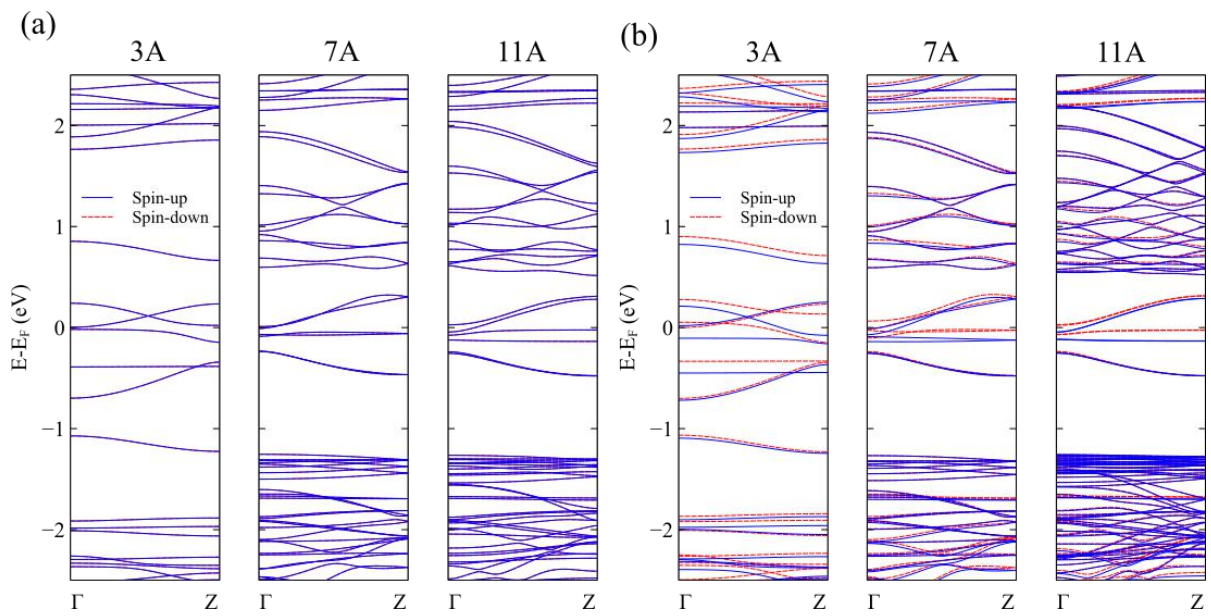


Figure S2: (a) and (b) Evolution of band structures for 3A, 7A, and 11A C₂N-*h*NRs for antiferromagnetic (AFM) and ferromagnetic (FM) states, respectively.

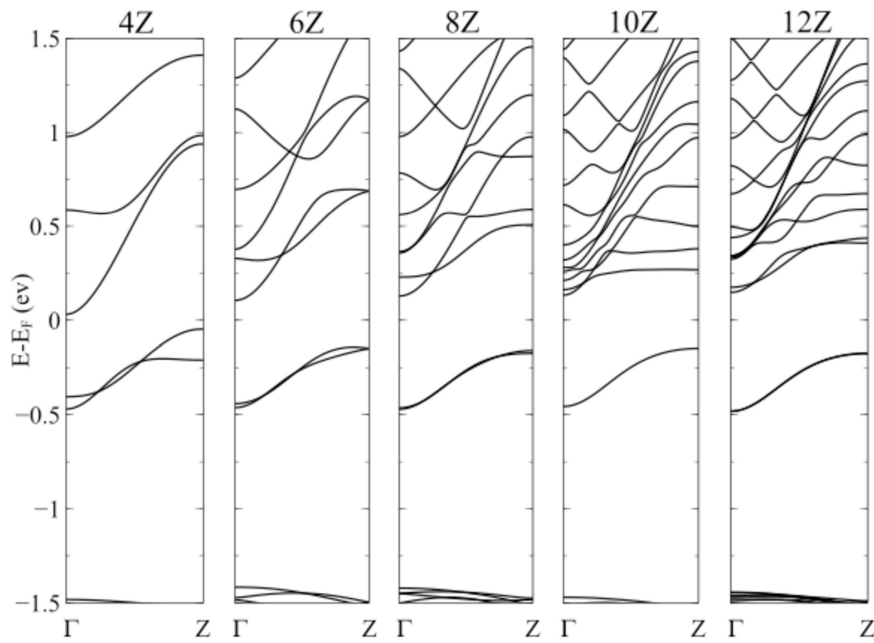


Figure S3: Evolution of band structures for 4Z, 6Z, 8Z, 10Z and 12Z C₂N-*h*NRs, respectively.

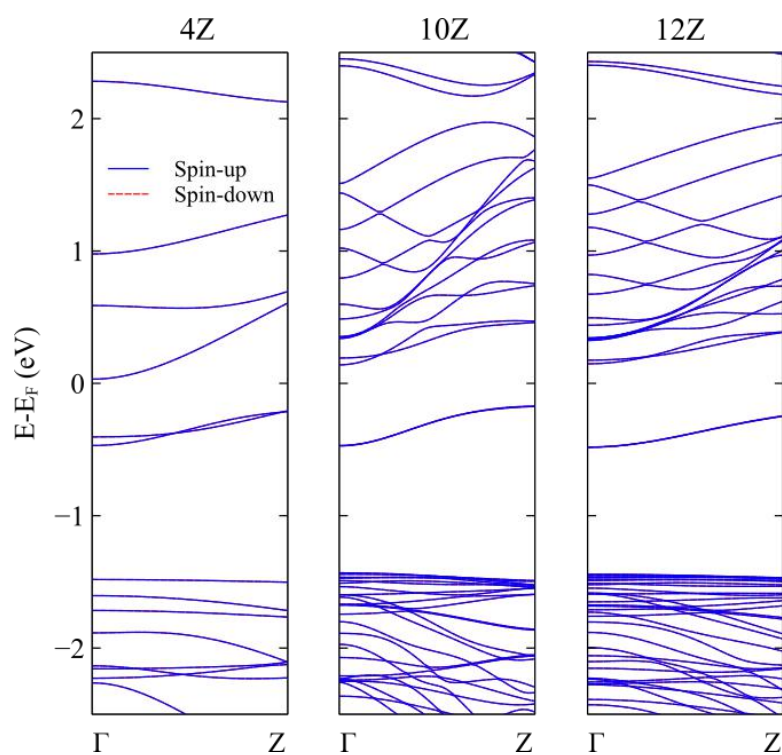


Figure S4: Evolution of band structures of for antiferromagnetic (AFM) for 4Z, 10Z and 12Z C_2N - h NRs, respectively.

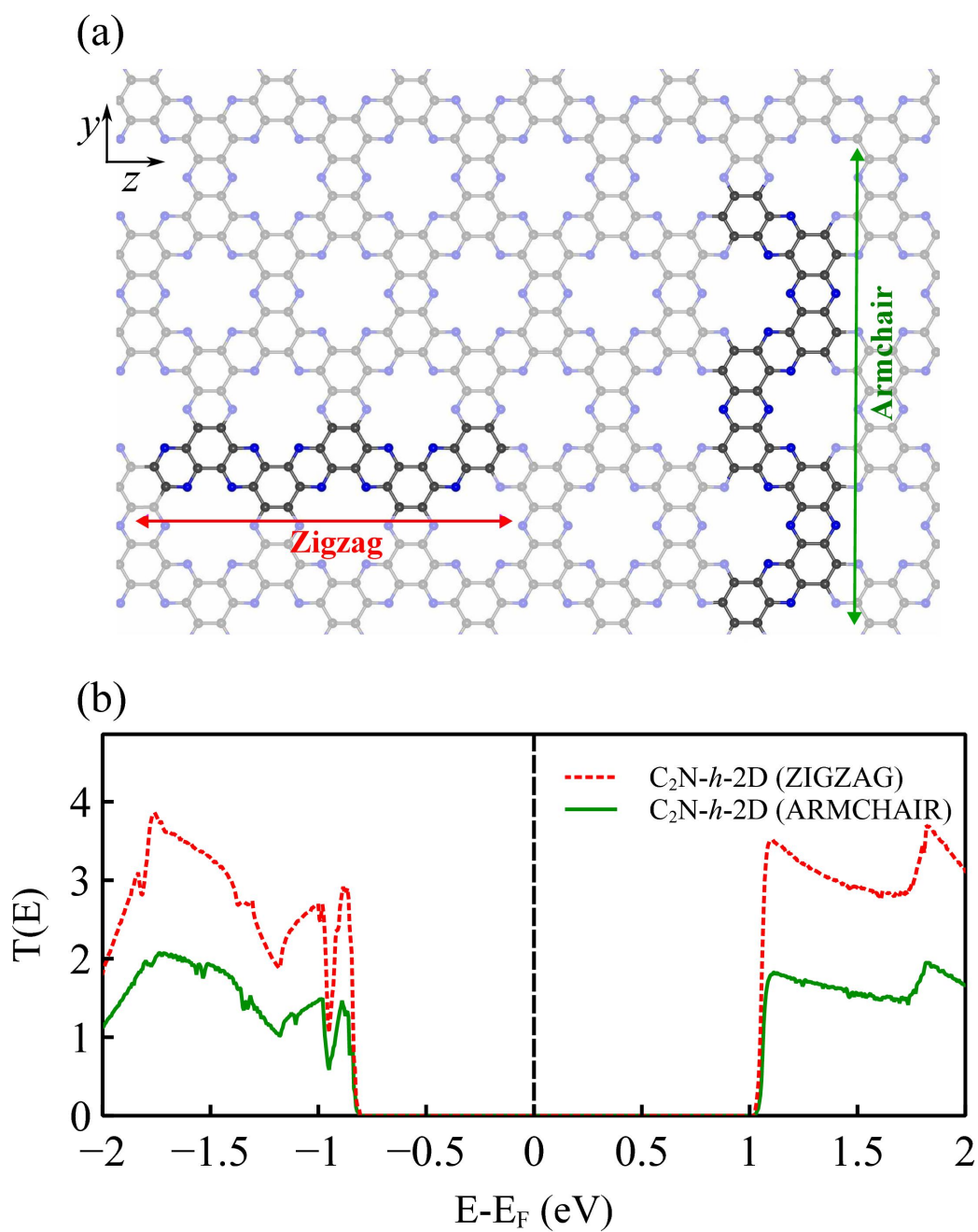


Figure S5: (a) Schematic view of the $\text{C}_2\text{N-}h\text{-2D}$ with labelled armchair and zigzag directions. (b) Transmission spectra of the $\text{C}_2\text{N-}h\text{-2D}$ for each direction.

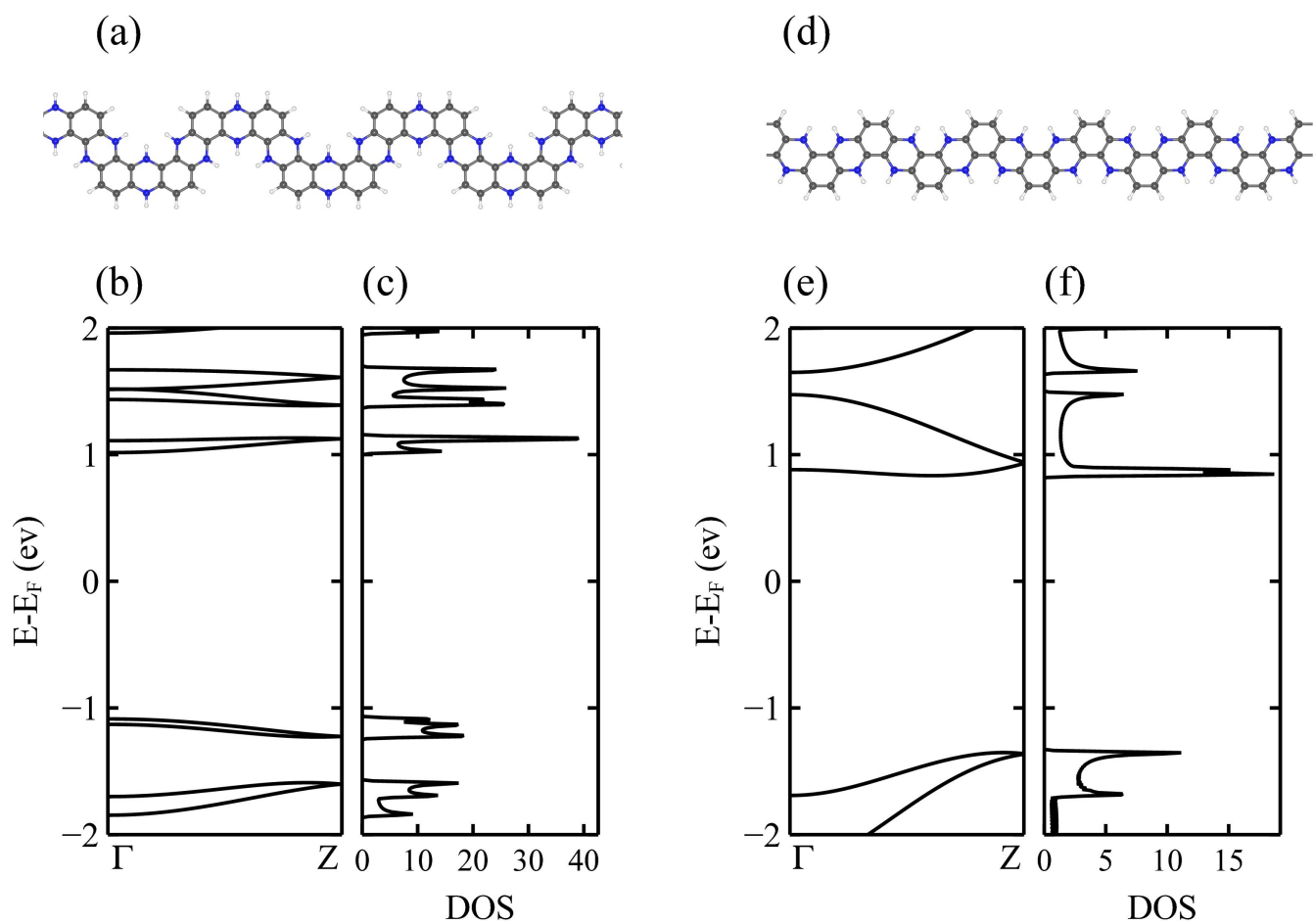


Figure S6: (a) and (d) Schematic view; (b) and (e) calculated band structures and (c) and (f) density of states (DOS) of the narrowest armchair and zigzag C_2N NRs, respectively.

Supplementary Note 1 | Sample Input Files for Calculations.

1) Siesta

Version: 3.2-pl-5

4ZC₂N-*h*-NR SCF input file:

```
SystemName      4-z

SystemLabel      4-z.file


LatticeConstant      1.00 Ang


%block LatticeVectors

    15.936505    0.000000    0.000000

    0.000000    30.246551    0.000000

    0.000000    0.000000    8.438071

%endblock LatticeVectors


NumberOfSpecies    3

NumberOfAtoms      42


%block ChemicalSpeciesLabel

    1    1    pseudos/H-gga
```

2 6 pseudos/C-gga

3 7 pseudos/N-gga

%endblock ChemicalSpeciesLabel

AtomicCoordinatesFormat Ang

%block AtomicCoordinatesAndAtomicSpecies

7.96839552	12.75967562	2.81335136	3
7.96859021	19.96203911	7.01018536	3
7.96836749	15.14275158	7.01644177	3
7.96834734	10.31878083	7.01096619	3
7.96864459	17.52559324	2.81209156	3
7.96844720	10.31874820	1.42924311	3
7.96854933	17.52579770	5.62782336	3
7.96846649	15.14239122	1.42361585	3
7.96836170	12.75989564	5.62665312	3
7.96873344	19.96176024	1.42959976	3
7.96835353	11.50678911	0.70108191	2
7.96852979	18.72031714	4.94148415	2
7.96839667	13.99429580	0.72034051	2

7.96845815	21.20501773	4.92386683	2
7.96833166	12.72367933	6.95999126	2
7.96856317	19.98862209	2.81962186	2
7.96834775	11.56293324	3.49829328	2
7.96846441	18.77608769	7.73914167	2
7.96829165	9.07597555	3.51586407	2
7.96844438	16.29088285	7.71990020	2
7.96830499	10.29276235	5.62014989	2
7.96854941	17.56062095	1.47937889	2
7.96834686	10.29262409	2.82007945	2
7.96847883	17.56086567	6.96056762	2
7.96833085	11.56298065	4.94191419	2
7.96850804	18.77572951	0.70070404	2
7.96826684	9.07600532	4.92432853	2
7.96849397	16.29052370	0.72014653	2
7.96836877	12.72325804	1.48009917	2
7.96850643	19.98881556	5.62014046	2
7.96832115	11.50708194	7.73894329	2
7.96856958	18.72020815	3.49830303	2
7.96835644	13.99469588	7.71963746	2

7.96848031	21.20491566	3.51570557	2
7.96844140	20.86483613	7.48192541	1
7.96826449	9.41522810	7.48251080	1
7.96832085	9.41522218	0.95745964	1
7.96848847	20.86451693	0.95788196	1
7.96845328	22.16241230	5.47571767	1
7.96827252	8.12027286	2.96081626	1
7.96824558	8.12013047	5.47921334	1
7.96847515	22.16210951	2.96350090	1

%endblock AtomicCoordinatesAndAtomicSpecies

2) Nanodcal

Electrode SCF input file:

system.name = ' 4zig_elec '

system.spinType = ' NoSpin '

system.orbitalType = ' DZP '

system.atomCoordinateFormat = ' cartesian '

system.atomFile = ' ./4zigelec.xyz '

```
system.centralCellVectors = ' [15.996000, 17.642600, 8.536120] '
```

```
calculation.name = ' scf '
```

Central region SCF input file:

```
system.name = ' 4zig_scat '
```

```
system.spinType = ' NoSpin '
```

```
system.orbitalType = ' DZP '
```

```
system.centralCellVectors = [15.996000 , 17.642600, 51.216720]
```

```
system.atomFile = ' scat.xyz '
```

```
calculation.name = ' scf '
```