

Supporting Information

Difference of the Micro-Dynamics Mechanism between Aromatic Nylon and Aliphatic Nylon during Water Absorption: Spectroscopic Evidence

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Theory of the scaling-MW2D spectroscopy based on auto-correlation

$Q(\nu, T)$ is an $M \times N$ spectral intensity matrix. The ν and T are spectral variable (e.g., wavenumber) and perturbation variable (e.g., temperature), respectively.

$$Q(\nu, T) = \begin{pmatrix} y(\nu, T_1) \\ \vdots \\ y(\nu, T_j) \\ \vdots \\ y(\nu, T_M) \end{pmatrix} \quad (1)$$

The reference spectrum and dynamic spectrum in the j th submatrix of $Q(\nu, T)$:

$$\bar{y}(\nu) = \frac{1}{2m+1} \sum_{j=j-m}^{j+m} y(\nu, T_j) \quad (2)$$

$$\tilde{y}(\nu, T_j) = y(\nu, T_j) - \bar{y}(\nu) \quad (3)$$

where J corresponds to the index of rows. A mean-centered j th submatrix of $Q(\nu, T)$ is obtained.

$$q_j(\nu, T) = \begin{pmatrix} \tilde{y}(\nu, T_{j-m}) \\ \vdots \\ \tilde{y}(\nu, T_j) \\ \vdots \\ \tilde{y}(\nu, T_{j+m}) \end{pmatrix} \quad (4)$$

The $q_j(\nu, T)$ has $2m+1$ rows which is called the window size. The index range of the perturbation variable T of $q_j(\nu, T)$ is from $j-m$ to $j+m$.

The generalized synchronous 2D correlation spectra is calculated from $q_j(\nu, T)$:

$$\Phi_j(\nu_1, \nu_2) = \frac{1}{2m} \sum_{j=j-m}^{j+m} \tilde{y}(\nu_1, T_j) \cdot \tilde{y}(\nu_2, T_j) \quad (5)$$

For each window, the standard deviations of spectral intensities at ν_1 and ν_2 are defined as follows.

$$\sigma(\nu_1) = \sqrt{\Phi_j(\nu_1, \nu_1)} \quad (6)$$

$$\sigma(\nu_2) = \sqrt{\Phi_j(\nu_2, \nu_2)} \quad (7)$$

The correlation coefficient $\rho(v_1, v_2)$ is defined:

$$\rho(v_1, v_2) = \Phi_j(v_1, v_2) / [\sigma(v_1) \cdot \sigma(v_2)] \quad (8)$$

The scaled forms of the synchronous correlation spectrum in each window are defined:

$$\Phi_j(v_1, v_2)^{(Scaled)} = \Phi_j(v_1, v_2) \cdot [\sigma(v_1) \cdot \sigma(v_2)]^{-\alpha} \cdot |\rho(v_1, v_2)|^\beta \quad (9)$$

The constant α is the scaling factor, and β is a correlation enhance factor. The value of α is limited to 0–1.0.

For scaling-MW2D based on auto-correlation, each row of the correlation matrix of scaling-MW2D is directly extracted from a diagonal line of $\Phi_j^{(Scaled)}$ matrix, namely $v_1=v_2$. Thus, the auto-correlation scaling-MW2D can be described below.

$$\Phi_j(v_1, v_1)^{(Scaled)} = \Phi_j(v_1, v_1) \cdot [\sigma(v_1) \cdot \sigma(v_1)]^{-\alpha} \cdot |\rho(v_1, v_1)|^\beta \quad (10)$$

$$\rho(v_1, v_1) = \Phi_j(v_1, v_1) / [\sigma(v_1) \cdot \sigma(v_1)] = 1 \quad (11)$$

$$\Phi_j(v_1, v_1)^{(Scaled)} = [\Phi_j(v_1, v_1)]^{1-\alpha} \quad (12)$$

The auto-correlation scaling-MW2D correlation spectrum is gained *via* sliding window position from $j=l+m$ to $M-m$ and repeating calculations of equation (2)-(12) at each window.

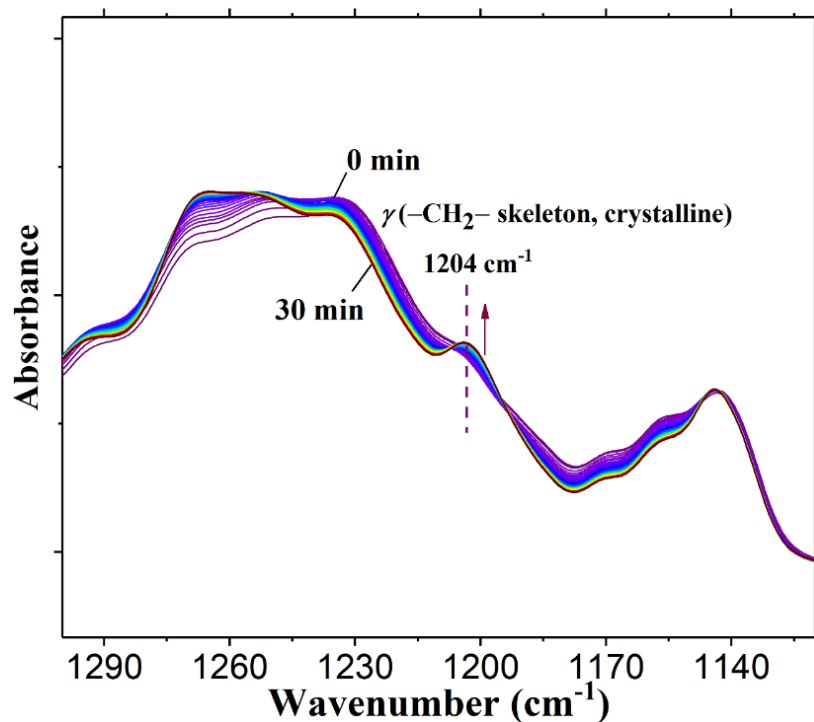


Figure S1. Time-dependent ATR FTIR spectra of the MXD6 film in the region of 1300–1120 cm^{-1} collected during ordinary water (H_2O) absorption.

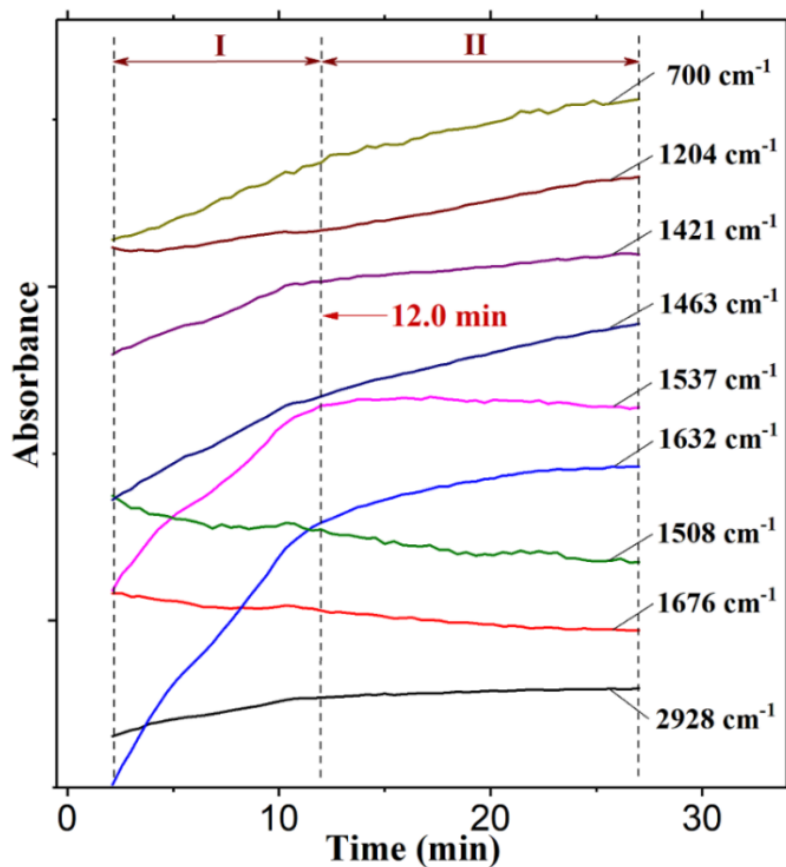


Figure S2. Spectral intensity changes extracted from the time-dependent ATR FTIR spectra of MXD6 during D_2O absorption from 2.0 min to 27.0 min.

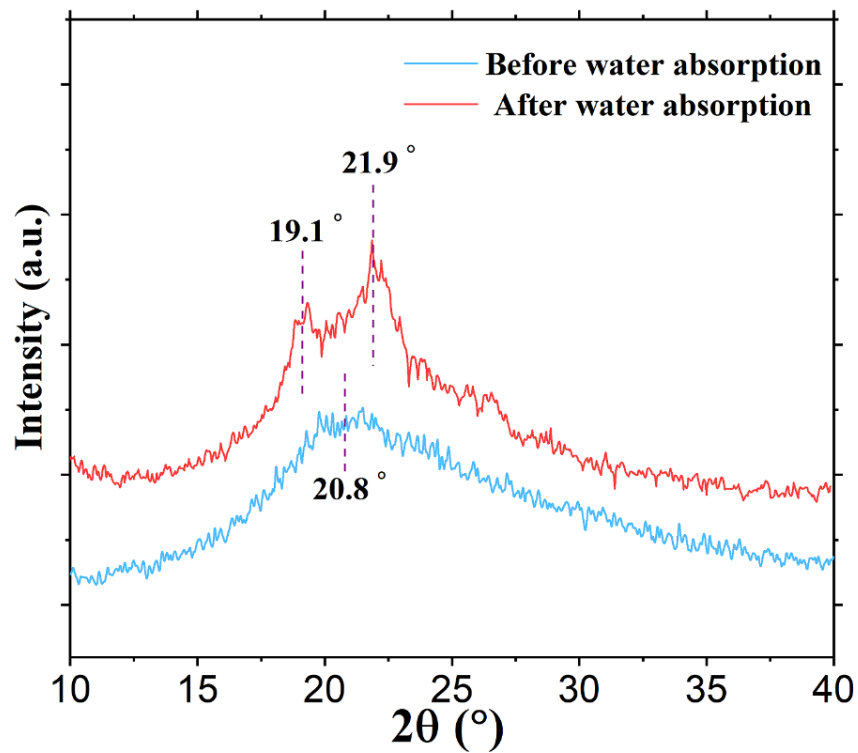


Figure S3. WAXD spectra of MXD6 films before and after water absorption.

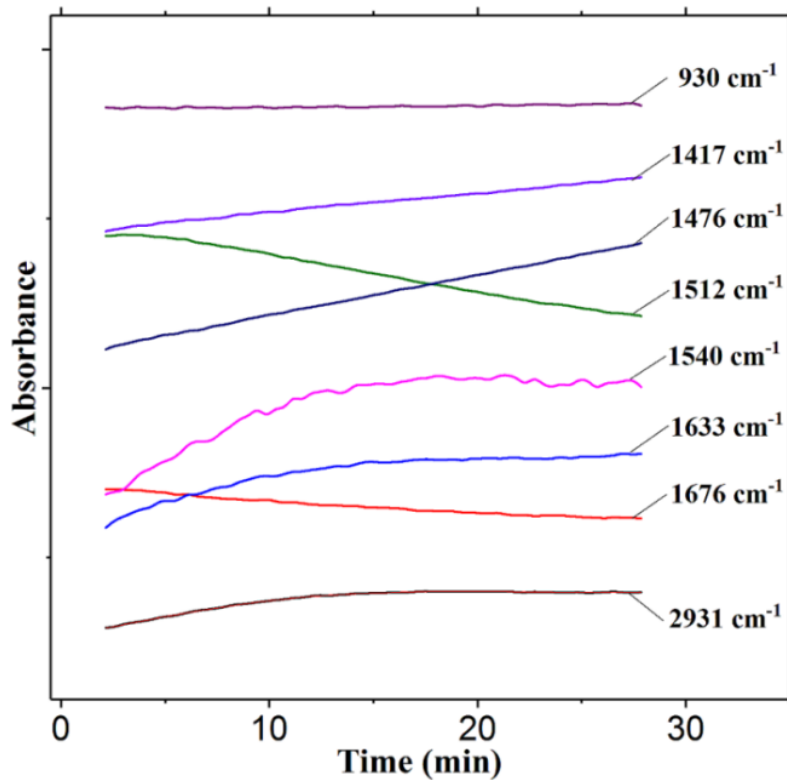


Figure S4. Spectral intensity changes extracted from the time-dependent ATR FTIR spectra of the PA6 film during D₂O absorption from 2.0 min to 27.0 min.

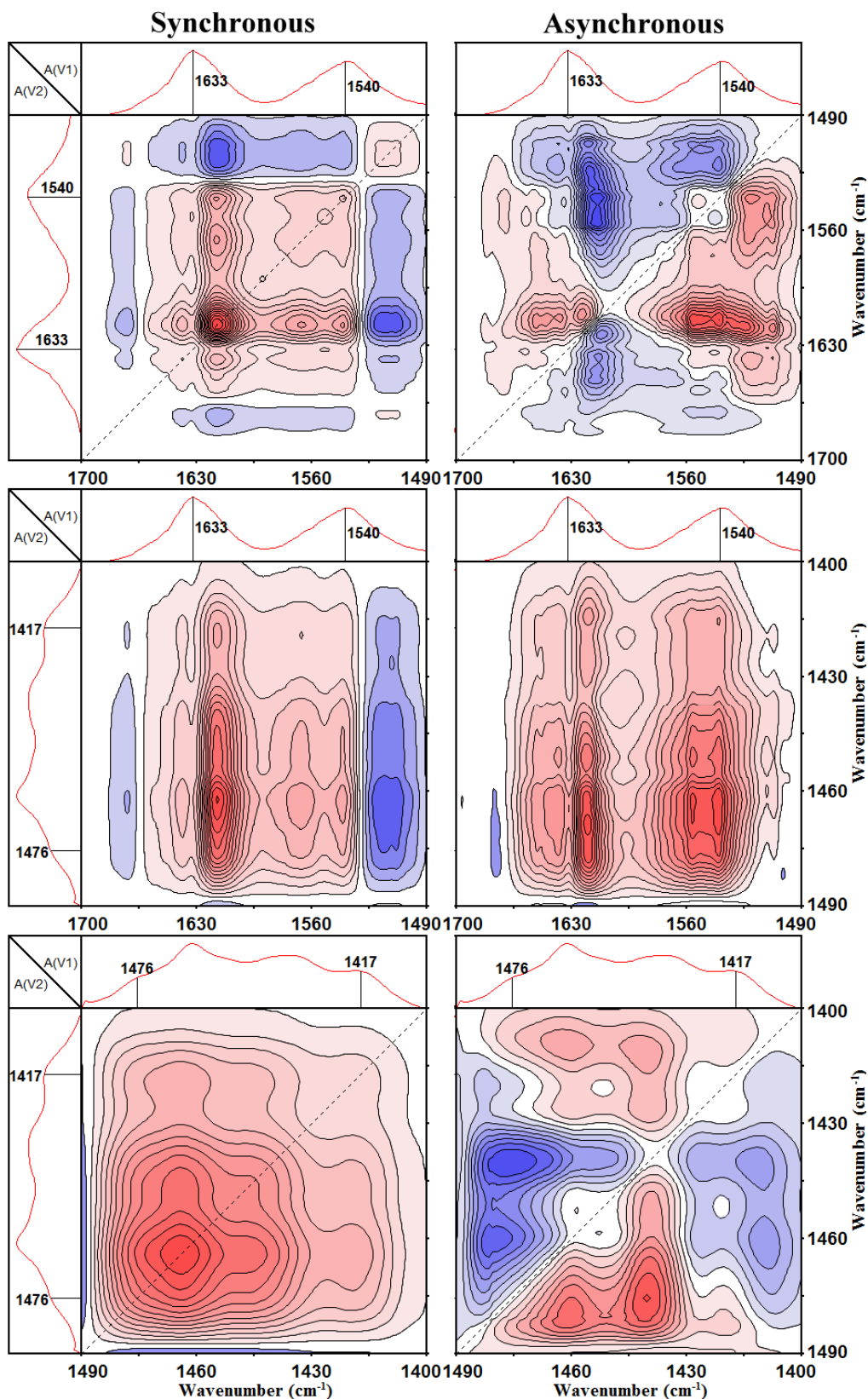


Figure S5. Synchronous (left) and asynchronous (right) generalized 2D correlation ATR FTIR spectra calculated from time-dependent ATR FTIR spectra of the PA6 film during D₂O absorption within 2.0–27.0 min in the regions of 1700–1490 cm⁻¹, 1700–1490 cm⁻¹ vs 1490–1400 cm⁻¹, and 1490–1400 cm⁻¹.

Table S1. Sequential orders of the process I (2.0–12.0 min) for MXD6 obtained from the synchronous and asynchronous 2D correlation ATR-FTIR spectra in **Figure 6**.

Cross correlation peaks (cm ⁻¹ , cm ⁻¹)	Sign in synchronous spectra	Sign in asynchronous spectra	Sequential order
(1632, 1537)	+	-	1632←1537
(1632, 1463)	+	+	1632→1463
(1632, 1421)	+	+	1632→1421
(1632, 700)	+	+	1632→700
(1537, 1463)	+	+	1537→1463
(1537, 1421)	+	+	1537→1421
(1537, 700)	+	+	1537→700
(1463, 1421)	+	+	1463→1421
(1463, 700)	+	+	1463→700
(1421, 700)	+	+	1421→700
(1632, 1204)	+	+	1632→1204
(1537, 1204)	+	+	1537→1204
(1463, 1204)	+	+	1463→1204
(1421, 1204)	+	+	1421→1204
(1204, 700)	+	-	1204←700
1537 cm ⁻¹ →1632 cm ⁻¹ →1463 cm ⁻¹ →1421 cm ⁻¹ →700 cm ⁻¹ →1204 cm ⁻¹			
$\delta(\text{N-H, bonded}) \rightarrow \nu(\text{C=O, bonded}) \rightarrow \delta(\text{C-H, -CH}_2\text{-NH-}) \rightarrow \delta(\text{C-H, -CH}_2\text{-CO-}) \rightarrow$ $\delta(=\text{C-H, benzene ring}) \rightarrow \gamma(\text{-CH}_2\text{- skeleton, crystalline})$			

Table S2. Sequential orders of the process II (12.0–27.0 min) for MXD6 obtained from the synchronous and asynchronous 2D correlation ATR-FTIR spectra in **Figure 7**.

Cross correlation peaks (cm ⁻¹ , cm ⁻¹)	Sign in synchronous spectra	Sign in asynchronous spectra	Sequential order
(1632, 1463)	+	+	1632→1463
(1632, 1421)	+	+	1632→1421
(1632, 700)	+	+	1632→700
(1463, 1421)	+	0	1463=1421
(1463, 700)	+	-	1463←700
(1421, 700)	+	-	1421←700
(1632, 1204)	+	+	1632→1204
(1463, 1204)	+	0	1463=1204
(1421, 1204)	+	0	1421=1204
(1204, 700)	+	-	1204←700
1632 cm ⁻¹ →700 cm ⁻¹ →1463 cm ⁻¹ =1421 cm ⁻¹ =1204 cm ⁻¹			
$\nu(\text{C=O, bonded}) \rightarrow \delta(=\text{C-H, benzene ring}) \rightarrow \delta(\text{C-H, -CH}_2\text{-NH-}) = \delta(\text{C-H, -CH}_2\text{-CO-}) =$ $\gamma(\text{-CH}_2\text{- skeleton, crystalline})$			

Table S3. Sequential orders of PA6 (2.0–27.0 min) obtained from the synchronous and asynchronous 2D correlation ATR-FTIR spectra in **Figure S5**.

Cross correlation peaks (cm⁻¹, cm⁻¹)	Sign in synchronous spectra	Sign in asynchronous spectra	Sequential order
(1633, 1540)	+	-	1633←1540
(1633, 1476)	+	+	1633→1476
(1633, 1417)	+	+	1633→1417
(1540, 1476)	+	+	1540→1476
(1540, 1417)	+	+	1540→1417
(1476, 1417)	+	-	1476←1417
1540 cm ⁻¹ →1633 cm ⁻¹ →1417cm ⁻¹ →1476 cm ⁻¹			
$\delta(\text{N-H, bonded}) \rightarrow \nu(\text{C=O, bonded}) \rightarrow \delta(\text{C-H, -CH}_2\text{-CO-}) \rightarrow \delta(\text{C-H, -CH}_2\text{-NH-})$			