Ab initio insights on the effect of embedding lanthanide atoms on nitrogenated holey doped graphene (g-C$_2$N)

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Supplementary Material

**Supplementary Figure 1**: Calculated lanthanide-nitrogen distance

**Supplementary Figure 2**: Calculated clustering energy