

Supporting Information

Molecular Dynamics Study of Natural Rubber-Fullerene Composites: Connecting Microscopic Properties to Macroscopic Behavior

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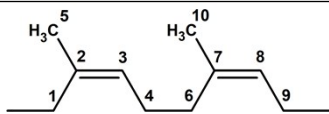
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1. Structure and interaction parameter

The united atom force field of *cis*-1,4-polyisoprene was taken from the existing literatures¹⁻⁴. The details of structure, bonded- and non-bonded-interactions are provided in Table S1.

Table S1: United atom force field of *cis*-PI



cis-1,4-polyisoprene

<u>Atom type</u>						
1	CH2					
2	CH0					
3	CH1					
4	CH2					
5	CH3					
<u>Bonded interaction</u>						
<u>Rigid bond</u>	k_b (kJmol ⁻¹ nm ⁻⁴)	b_0 (nm)				
1-2	5.43×10^6	0.151				
2-3	1.08×10^7	0.134				
2-5	5.43×10^6	0.151				
3-4	5.43×10^6	0.151				
4-6	5.43×10^6	0.153				
<u>Angle bending</u>	k_θ (kJmol ⁻¹ rad ⁻²)	θ_0 (deg)				
1-2-3	374.0	125.9				
2-3-4	374.0	125.9				
3-4-6	481.16	111.65				
5-2-3	374.0	125.9				
4-6-7	481.16	111.65				
<u>Torsions</u>	k_n (n=1,...,6) (kJmol ⁻¹)					
4-6-7-8	3.598	-0.167	4.853	0.669	1.590	-0.502
2-3-4-6	3.598	-0.167	4.853	0.669	1.590	-0.502
3-4-6-7	-4.142	-2.594	-16.903	-0.293	-1.046	-0.795
<u>Improper dihedral</u>	k_ϕ (kJmol ⁻¹ rad ⁻²)	ϕ_0 (deg)				
1-2-3-4	160	0				
5-2-3-4	160	180				
<u>Non-bonded interaction: Lennard-Jones potential</u>						
	C6	C12				
CH0	CH0	0.00252	3.79310×10^{-6}			
CH0	CH1	0.00252	3.79310×10^{-6}			
CH0	CH2	0.00505	1.50419×10^{-5}			
CH0	CH3	0.00750	2.23034×10^{-5}			
CH1	CH1	0.00252	3.79310×10^{-6}			
CH1	CH2	0.00505	1.50419×10^{-5}			
CH1	CH3	0.00750	2.23034×10^{-5}			
CH2	CH2	0.00650	2.70034×10^{-5}			
CH2	CH3	0.01012	4.20052×10^{-5}			
CH3	CH3	0.01573	6.53158×10^{-5}			

2. System setup and stability

Table S2: Number of molecules and the simulation time

[C60]	Number of C60 molecule	Number of <i>cis</i> -PI chain	Simulation time (μ s)
0	0	200	7.0
0.5	3	200	5.0
1	5	200	5.0
2	11	200	5.0
4	21	200	5.0
6	32	200	5.0
8	43	200	5.0
16	85	200	5.0
32	171	200	8.3
64	341	200	6.6

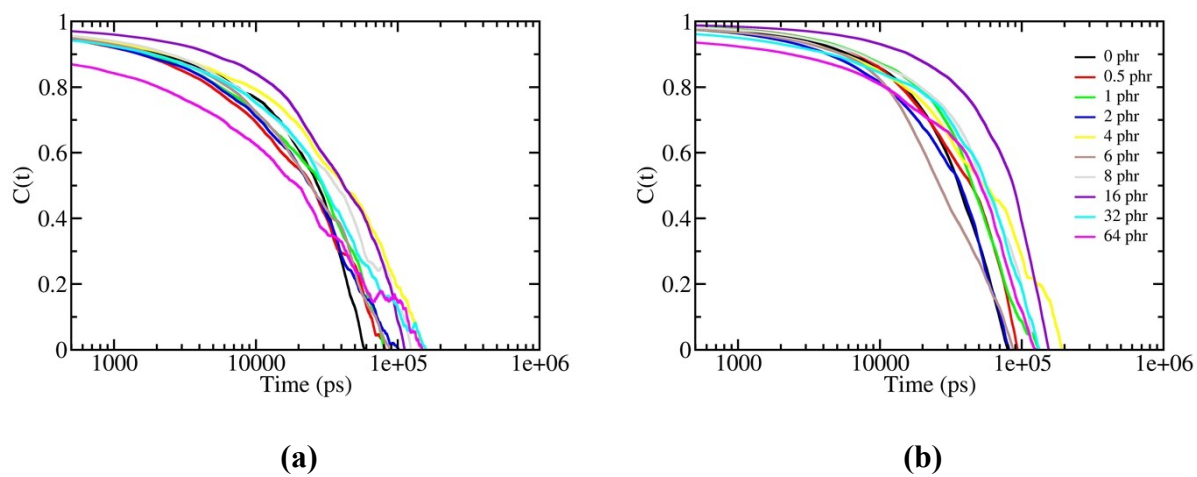


Figure S1: Autocorrelations of rubber chains (a) R_0 and (b) R_g are determined by

$C(t) = \langle R(\xi)R(\xi + t) \rangle_{\xi}$, where ξ is the time origin and $\langle \rangle$ is the average over ξ ^{5, 6}.

Table S3: Autocorrelation relaxation time of R_0 and R_g

[C60]	Autocorrelation relaxation time (ns)	
	R_0	R_g
0	58	79
0.5	81	93
1	80	132
2	101	81
4	144	191
6	87	87
8	123	121
16	111	154
32	157	133
64	149	125

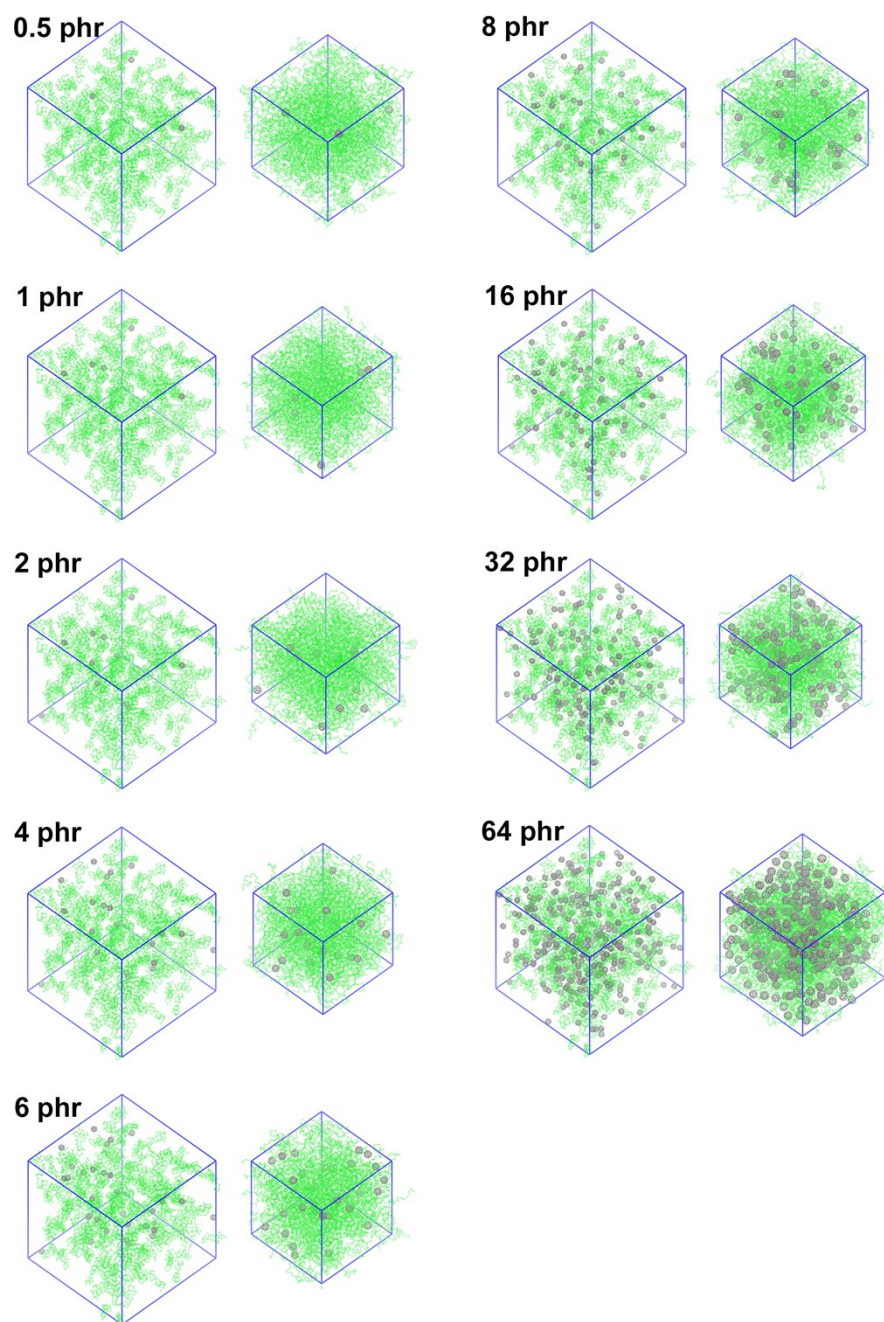


Figure S2: The initial structure of each simulation system; the C_{60} molecules and *cis*-PI chains are initially random added in the simulation box (left) comparing to their final structure (right).

3. Force field testing

Table S4: Comparison of the structural and bulk properties of *cis*-PI in melts at 300 K to the previous studies.

Properties	Simulation*	Refs.	Simulation details
<i>cis</i> -PI in melts (200 chains PI, <i>DP</i> of PI=32)			
density (kg/m ³)	853.9±1.6	910 ^{a7}	
		825 ^{b2, 3}	<i>DP</i> of PI=20, united-atoms at 413 K
		840 ^{b8}	<i>DP</i> of PI=24, all-atoms at 413 K
		885.1±0.2 ^{b6}	<i>DP</i> of PI=32, united-atom at 298 K and 1 bar
$\langle R_0^2 \rangle$ (nm ²)	12.85±0.41	14.10 ± 0.20 ^{b6}	<i>DP</i> of PI=32, united-atom at 298 K and 1 bar
$\langle R_g^2 \rangle$ (nm ²)	2.07±0.04	2.28 ± 0.5 ^{b6}	<i>DP</i> of PI=32, united-atom at 298 K and 1 bar
$\langle R_0^2 \rangle / \langle R_g^2 \rangle$	6.20	6.18 ^{b6}	<i>DP</i> of PI=32, united-atom at 298 K and 1 bar
Bulk modulus (GPa)	1.37±0.02	2.020 ^{a6, 9} ,	
		1.95 ^{b6} ,	<i>DP</i> of PI=32, united-atom at 298 K and 1 bar
Thermal expansion (10 ⁻⁴ ·K ⁻¹)	7.80±0.15	6.1 ^{a 6, 10, 11} ,	
		6.6 ^{b 6}	<i>DP</i> of PI=32, united-atom at 298 K and 1 bar

* average from the last 1000 ns of current simulations

^aexperiment, ^b simulations

4. Mean Square Displacement (MSD)

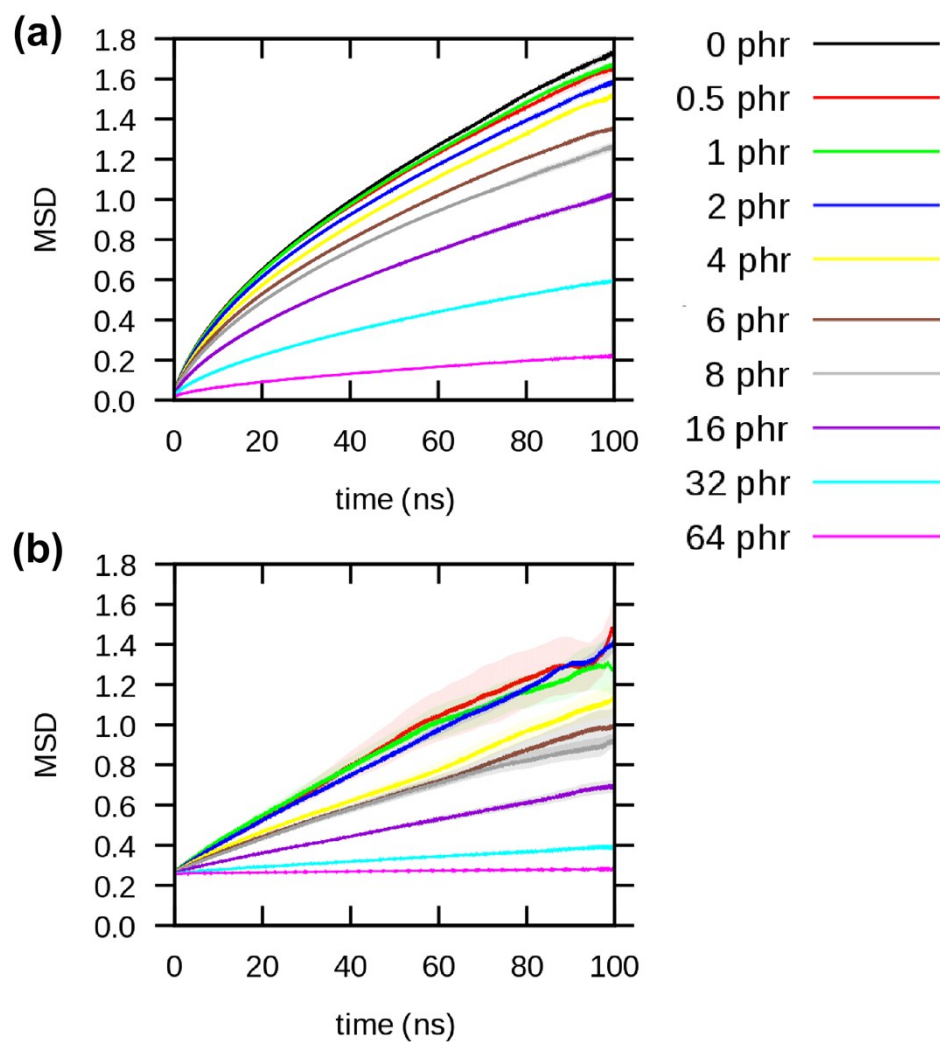


Figure S3: The mean squared displacement (MSD), Eq 6. in the main text, (a) *cis*-PI and (b) C60 is determined by the deviation of the position of a molecule with respect to a reference position over time, $\langle r^2 \rangle$. The standard deviation is used for error estimate.

References

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