

Figure S1. ${}^1,{}^3\Delta$ adiabatic potential energy curves.

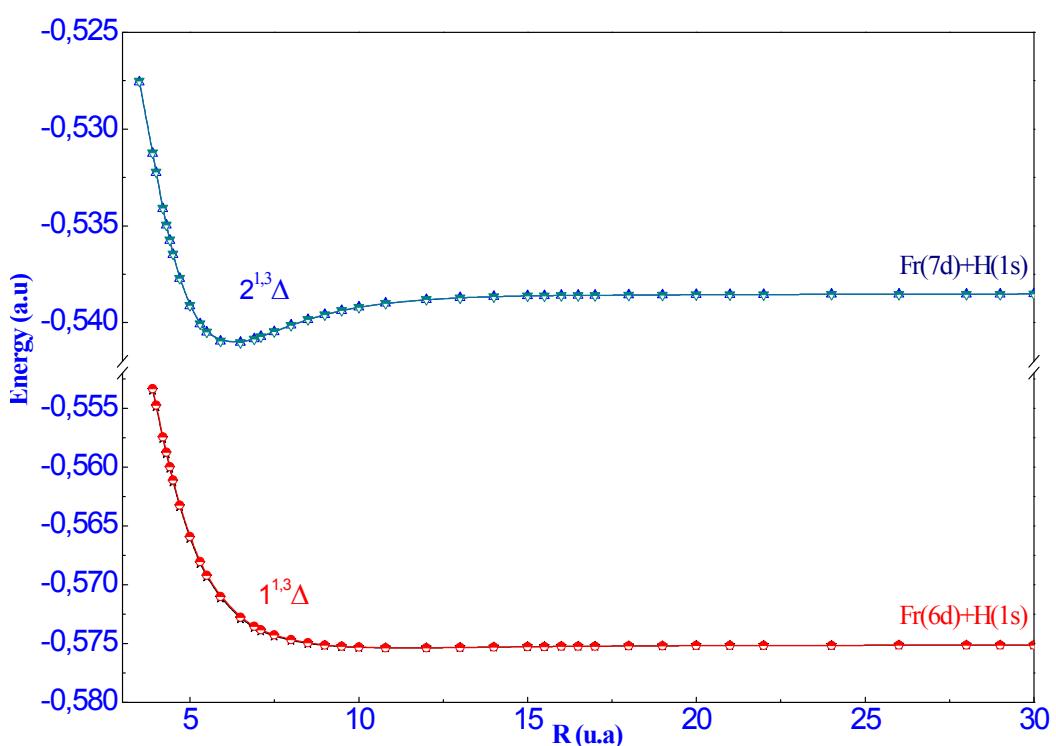


Figure S2. Diabatic ${}^1,{}^3\Delta$ potential energy curves dissociating below the ionic limit Fr^+H^- .

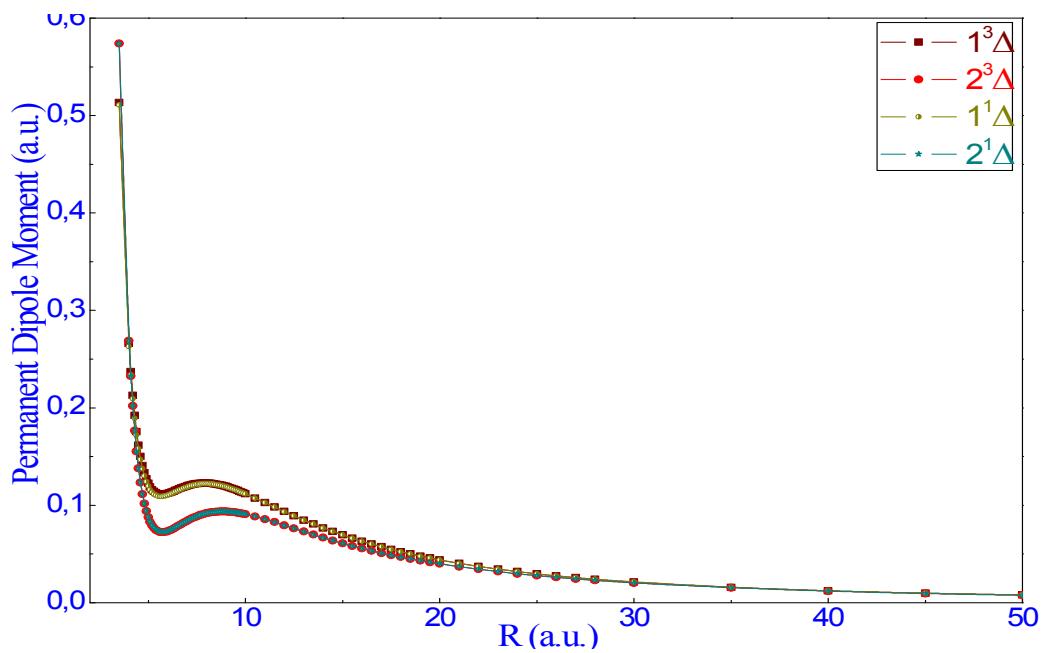


Figure S3. Adiabatic permanent dipole moment for the states of ${}^1,{}^3\Delta$ for the FrH.

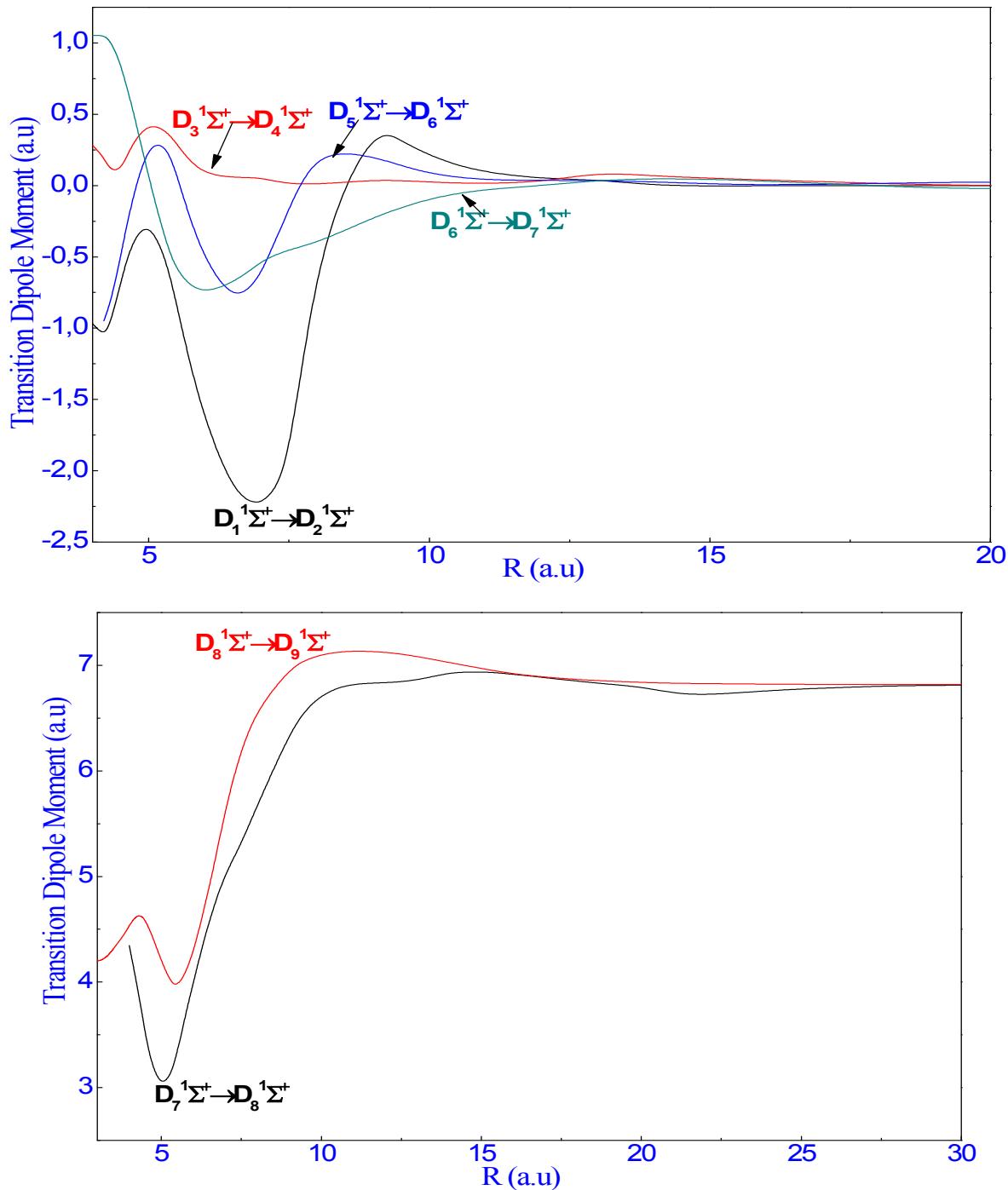


Figure.S4. Transition dipole moment between selected ${}^1\Sigma^+$ diabatic states.

Table S1. Basis set for francium.

| | Exponents |
|----------|-----------|
| s | 1.3 |
| | 0.650 |
| | 0.28 |
| | 0.109 |
| | 0.0400 |
| | 0.01980 |
| | 0.00620 |
| p | 0.00208 |
| | 0.330 |
| | 0.1090 |
| | 0.0310 |
| | 0.0150 |
| | 0.0047 |
| d | 0.0020 |
| | 0.90 |
| | 0.208 |
| | 0.0634 |
| | 0.0196 |
| | 0.0057 |

Table S2. Theoretical ionization energies (in cm⁻¹) of hydrogen atom compared with the experimental ones⁸³.

| Atomic levels | Expt. ⁸³ | This work | ΔE(cm ⁻¹) |
|---------------|---------------------|-----------|-----------------------|
| 1s | -109678 | -109725 | 47 |
| 2s | -27419 | -27371 | 48 |
| 2p | -27419 | -27369 | 50 |
| 3s | -12186 | -12189 | 3 |

ΔE : Energy difference between the experimental values and theoretical work in cm⁻¹.

Table S3. Theoretical ionization energies (in cm⁻¹) of francium atom compared with the experimental energies⁸³.

| Atomic levels | Expt. ⁸³ | This work | ΔE | M. Aymar et al. ⁴⁹ | ΔE |
|---------------|---------------------|-----------|----|-------------------------------|-----|
| 7s | -32848 | -32848 | 0 | -32 848 | 0 |
| 7p | -19487 | -19487 | 0 | -19 486 | 1 |
| 6d | -16499 | -16499 | 0 | -16 470 | 29 |
| 8s | -13108 | -13176 | 68 | -13 161 | 53 |
| 8p | -9372 | -9425 | 53 | -9448 | 76 |
| 7d | -8551 | -8463 | 88 | -8394 | 157 |
| 9s | -7177 | -7192 | 15 | -7161 | 16 |
| 9p | -5565 | -5580 | 15 | -5619 | 54 |

ΔE : Energy difference between the experimental values and theoretical work in cm⁻¹.

Table S4. Various molecular states of FrH below the ionic limit (Fr⁺+ H⁻).

| Asymptotic limits | Molecular states | Exp ⁸³ (cm ⁻¹) | This work (cm ⁻¹) | Δ |
|---------------------------------|--|---------------------------------------|-------------------------------|-------|
| Fr (7s) +H (1s) | ^{1,3} Σ ⁺ | -142527 | -142574 | 0.033 |
| Fr (7p) +H (1s) | ^{1,3} Σ ⁺ , ^{1,3} Π | -129165 | -129212 | 0.036 |
| Fr (6d) +H (1s) | ^{1,3} Σ ⁺ , ^{1,3} Π, ^{1,3} Δ | -126177 | -126225 | 0.038 |
| Fr (8s) +H (1s) | ^{1,3} Σ ⁺ | -122787 | -122902 | 0.094 |
| Fr (8p) +H (1s) | ^{1,3} Σ ⁺ , ^{1,3} Π | -119051 | -119151 | 0.084 |
| Fr (7d) +H (1s) | ^{1,3} Σ ⁺ , ^{1,3} Π, ^{1,3} Δ | -118230 | -118189 | 0.035 |
| Fr (9s) +H (1s) | ^{1,3} Σ ⁺ | -116856 | -116918 | 0.053 |
| Fr (9p) +H (1s) | ^{1,3} Σ ⁺ , ^{1,3} Π | -115244 | -115306 | 0.054 |
| Fr ⁺ +H ⁻ | | -115761 | | |

Δ : Relative errors between the experimental and theoretical energy values ($\Delta = ((\text{Exp}-\text{this work})/\text{E}) * 100$) (in %).