## Molecular insight into the high selectivity of double-walled carbon nanotubes

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## 1. Force fields

Carbon dioxide	$\sigma_{\rm ff}$ (Å)	$\epsilon_{\mathrm{ff}}/k_{\mathrm{B}}\left(\mathrm{K} ight)$	l <sub>CO</sub> (Å)	$l_{q}\left( e ight)$
	C: 2.824	C: 28.68		$C \cdot 0.664$
	O: 3.026	O: 82.0	1.162	C. 0.004
	C-O: 2.925	C-O: 48.495		0: -0.332

**Table 1.** Lennard-Jones parameters and partial charges for the 3-site carbon dioxide model: C-O denotes LJ parameters obtained from Lorentz-Berthelot mixing rule,  $l_{CO}$  is the C-O bond length.

	$\sigma_{\rm ff}$ (Å)	$\epsilon_{\mathrm{ff}}/k_{\mathrm{B}}\left(\mathrm{K} ight)$	l <sub>CH</sub> (Å)	$l_{q}(e)$
Methane	C: 3.4	C: 55.055		H: 0.165
Wiethane	H: 2.65	H: 7.901	1.09	$\begin{array}{c} \mathbf{n} \\ 0 \\ $
	C-H: 3.025	С-Н: 30.6		C0.00

**Table 2.** Lennard-Jones parameters and partial charges for the 5-site methane model: C-H denotes LJ parameters fitted to experimental data, l<sub>CH</sub> is the C-H bond length.

	σ <sub>ff</sub> (Å)	$\epsilon_{\mathrm{ff}}/k_{\mathrm{B}}\left(\mathrm{K} ight)$	l <sub>00</sub> (Å)	$l_{q}(e)$
Oxygen	O: 3.1062	O: 43.183	0.9699	O: -0.40405 COM: 0.8081

**Table 3.** Lennard-Jones parameters and partial charges for the 2-site oxygen model:COM denotes centre of mass,  $l_{OO}$  is the O-O bond length.

	σ <sub>ff</sub> (Å)	$\epsilon_{\mathrm{ff}}/\mathrm{k}_{\mathrm{B}}\left(\mathrm{K} ight)$	l <sub>NN</sub> (Å)	$l_{q}(e)$
Nitrogen	N: 3.31	N: 36.0	1.1	N: -0.482
				COM: 0.964

**Table 4.** Lennard-Jones parameters and partial charges for the 2-site nitrogen model:COM denotes centre of mass,  $l_{NN}$  is the N-N bond length.

	σ <sub>ff</sub> (Å)	$\epsilon_{\rm ff}/k_{\rm B}\left(K ight)$	l <sub>HH</sub> (Å)	l <sub>LL</sub> (Å)	l <sub>q</sub> (e)
Hydrogen	L: 2.37031	L: 2.16726			Ц. 0 2722
	COM: 3.15528	COM: 12.76532	0.742 0.726	COM: -0.7464	
	L-COM: 2.762795	L-COM: 5.259826			

**Table 5.** Lennard-Jones parameters and partial charges for the 5-site hydrogen model: COM denotes centre of mass, L is the additional LJ site,  $l_{HH}$  is the H-H bond length,  $l_{LL}$  is the L-L bond length, L-COM denotes LJ parameters obtained from Lorentz-Berthelot mixing rule.

	$\sigma_{\rm ff}$ (Å)	$\epsilon_{\mathrm{ff}}/k_{\mathrm{B}}\left(\mathrm{K} ight)$	l <sub>CO</sub> (Å)	$l_{q}\left( e ight)$
Carbon	C: 3.49	C: 22.8		$C \cdot 0.0203$
monoxide	O: 3.13	O: 63.5	1.128	0: 0.0203
	C-O: 3.31	C-O: 38.05		00.0203

**Table 6.** Lennard-Jones parameters and partial charges for the 2-site carbon monoxide model: C-O denotes LJ parameters obtained from Lorentz-Berthelot mixing rule,  $l_{CO}$  is the C-O bond length.

## 2. Force fields validation using thermodynamics data

We estimated the average density from the following expression,

$$\rho \left( \text{mmolcm}^{-3} \right) = 10000 \left\langle \rho \right\rangle / 6.0223 \tag{18}$$

where  $\langle ... \rangle$  denotes an ensemble average,  $\langle \rho \rangle = N / \langle V(Å) \rangle$  is the average number density, and N denotes a number of molecules. Additionally, for selected adsorbates and state points, we computed isothermal compressibility and coefficient of thermal expansion from the fluctuation formulas,

$$\kappa = -1/V \left( \frac{\partial V}{\partial p} \right)_{N,T} = \left( \left\langle V^2 \right\rangle - \left\langle V \right\rangle^2 \right) / k_b T \left\langle V \right\rangle$$
(2S)

$$\alpha = 1/V \left( \frac{\partial V}{\partial T} \right)_{N,p} = \left( \langle VH \rangle - \langle V \rangle \langle H \rangle \right) / k_b T^2 \langle V \rangle$$
(38)

$$H = E(fluid) + pV = \sum_{a < b} E_{ab} + pV$$
(4S)

where  $E_{ab}$  is the total potential energy between particle *a* and *b*, *T* denotes temperature, *p* is the pressure, *H* is the enthalpy, *R* is the universal gas constant, and  $k_b$  denotes Boltzmann constant.



**Figure 1S.** Comparison of the experimental equation of states for carbon dioxide (solid lines) with the results calculated from isothermal-isobaric Monte Carlo simulations at 298 (open squares), 320 (open triangles), and 340 K (open stars).



**Figure 2S.** Comparison of the experimental equation of states for methane (solid lines) with the results calculated from isothermal-isobaric Monte Carlo simulations at 298 (open squares), 320 (open triangles), and 340 K (open stars).



**Figure 3S.** Comparison of the experimental equation of states for oxygen (solid lines) with the results calculated from isothermal-isobaric Monte Carlo simulations at 298 (open squares), 320 (open triangles), and 340 K (open stars).



**Figure 4S.** Comparison of the experimental equation of states for nitrogen (solid lines) with the results calculated from isothermal-isobaric Monte Carlo simulations at 298 (open squares), 320 (open triangles), and 340 K (open stars).



**Figure 5S.** Comparison of the experimental equation of state for hydrogen at 298 K (solid line) with the results calculated from isothermal-isobaric Monte Carlo simulations at 298 (open squares), 320 (open triangles), and 340 K (open stars).



**Figure 6S.** The comparison of the experimental thermal expansivity of oxygen (solid lines) with the results calculated from isothermal-isobaric Monte Carlo simulations at 298 (triangles), 320 (squares), and 340 K (circles).



**Figure 7S.** The comparison of the experimental thermal expansivity of carbon dioxide (solid lines) with the results calculated from isothermal-isobaric Monte Carlo simulations at 298 (triangles), 320 (squares), and 340 K (circles).



**Figure 8S.** Comparison of the experimental isothermal compressibility for carbon dioxide, methane, oxygen, and nitrogen (solid lines) at 340 K with the results calculated from isothermal-isobaric Monte Carlo simulations: triangles-carbon dioxide, stars-methane, squares-oxygen, diamonds-nitrogen, and crosses-hydrogen.



## T = 298 K and p = 20 Mpa

**Figure 9S.** Atomistic structure of  $CO_2$ ,  $H_2$ ,  $N_2$ , and  $O_2$  at 298 K and 20 MPa computed from isothermal-isobaric Monte Carlo simulations.