  
Setting standards  
in analytical science

**ISO/TS 21748: A new guide to uncertainty  
estimation using interlaboratory study data**

S Ellison  
LGC

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**Overview**

  
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- Reproducibility and uncertainty estimation
- Introduction to ISO TS 21748

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**What is Measurement  
Uncertainty?**

  
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“A parameter, associated with the result of a measurement,  
that characterises the dispersion of the values that could  
reasonably be attributed to the measurand”  
*(ISO Guide)*

**The number after the  $\pm$**

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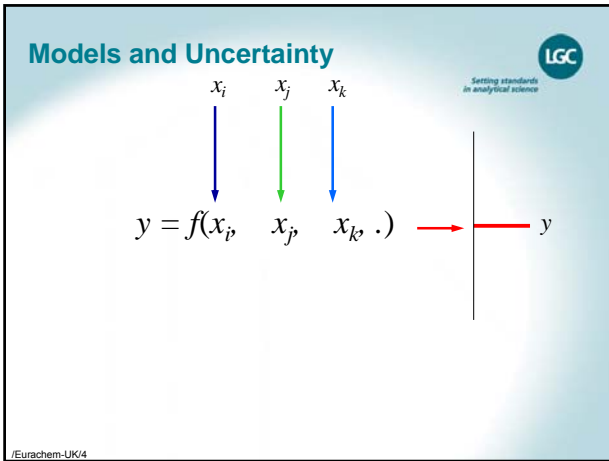
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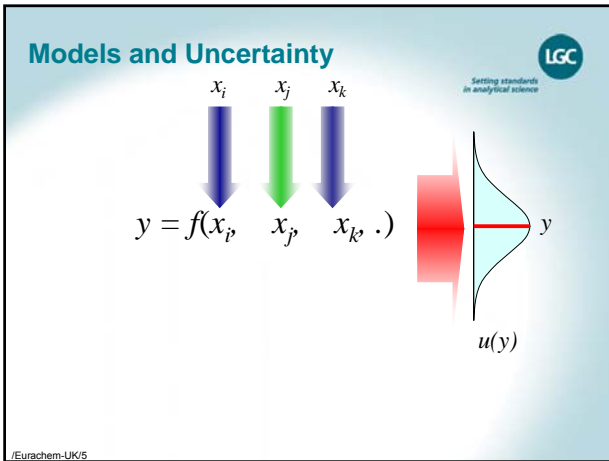
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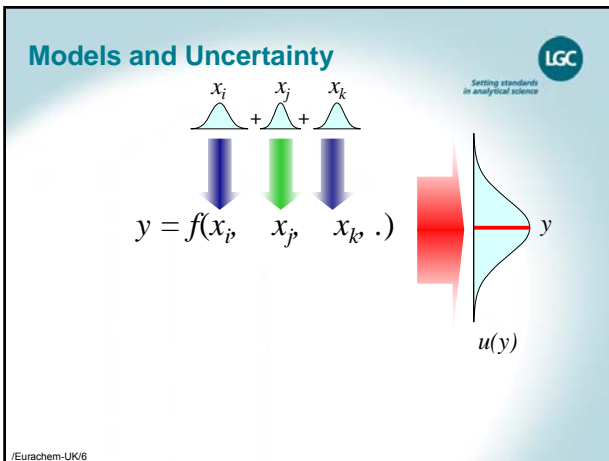
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## ISO Guide approach



- Specify the measurand
  - including complete equation
- Quantify significant uncertainties in all parameters
  - A: from statistics of repeated experiment
  - B: by any other means (theory, certificates, judgement...)
- Express as standard deviation
- Combine according to stated principles

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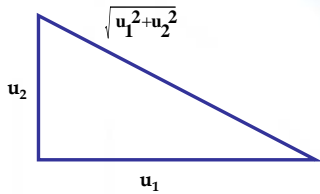
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## Combining uncertainties (ISO)



- Standard deviations
- Established error propagation theory

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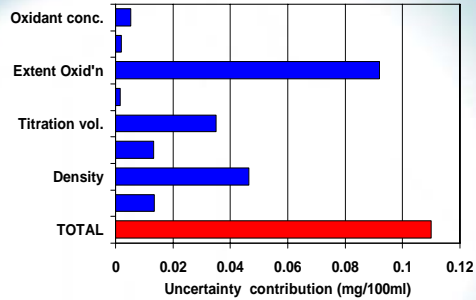
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## Example: Forensic alcohol standard titration



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## Implementing ISO in Chemistry Building models



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- Every determinant is unique
  - Every element, every molecule, every formulation
- Every 'matrix' is unique
  - Different interactions with substrate
- Interactions with environment and substrate rarely understood
- **Models are difficult to build!**

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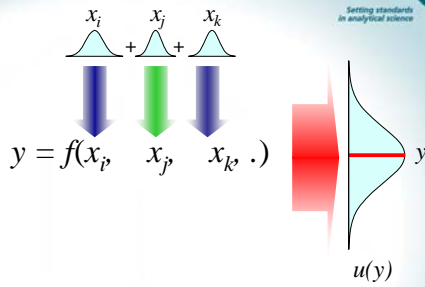
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## Two views of influence factors



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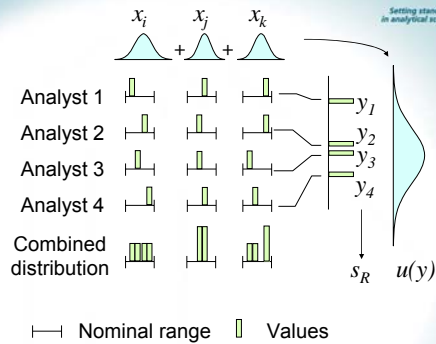
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## Two views of influence factors



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## A simpler model



- The best available estimate of precision
  - *An effect varied representatively during a precision experiment requires no further study*
- The best available estimate of bias *and its uncertainty*
- Other significant effects evaluated
  - By experiment, or from standing data

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## Collaboratively trialed methods



- Collaboratively trialed method
  - bias and precision verified in-house
- Assessed against collaborative study estimates
  - ISO/TS 21748
  - demonstrate method bias and repeatability are under control

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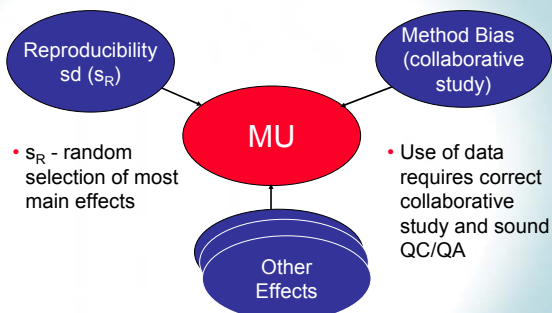
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## Collaborative trial data



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## Process for evaluating uncertainty according to ISO/TS 21748



- Obtain repeatability, reproducibility and bias estimates from collaborative study
- Establish whether laboratory bias is within that expected on the basis of the collaborative study
- Establish whether laboratory precision is within that expected on the basis of the collaborative study
- Where laboratory bias and precision are under control, combine effects appropriately to form a combined uncertainty estimate

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## TS21748 uncertainty budget



$$u_c^2(y) = \hat{s}_R^2 + u^2(\hat{\delta}) + \sum_{i=k,n} c_i^2 u^2(x_i)$$

- Combined uncertainty
  - Adjusted reproducibility estimate
    - Uncertainty associated with method bias
      - Effects not covered, e.g. sampling uncertainty

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## Demonstrating acceptable laboratory bias



- Study of CRMs
  - Simple test for significant bias
  - Ideally with small bias check uncertainty
- Comparison with known test method
  - Typically paired tests on several materials
- Comparison with other laboratories
  - Proficiency testing or other collaborative study

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**Including trueness data in an uncertainty estimate**

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$$u_c^2(y) = \hat{s}_R^2 + u^2(\hat{\delta}) + \sum_{i=k,n} c_i^2 u^2(x_i)$$

- Combined uncertainty
  - Adjusted reproducibility estimate
  - **Uncertainty associated with method bias**
    - Effects not covered, e.g. sampling uncertainty

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**Demonstrating acceptable laboratory precision**

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- Requires a check on repeatability standard deviation
  - F-test at appropriate level.
- If within-laboratory precision differs from Study  $s_r$ 
  - Replace study  $s_r$  with in-house repeatability SD
- Otherwise, continue using published  $s_R$

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**Adjusting for changes in test item**

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- Allow for inhomogeneity and sample prep via additional uncertainty contributions
- Allow for changes in precision with analyte level
  - Linear model most common
  - Often sufficient to use %RSD

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### Including reproducibility data

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$$u_c^2(y) = \hat{s}_R^2 + u^2(\hat{\delta}) + \sum_{i=k,n} c_i^2 u^2(x_i)$$

- Combined uncertainty
  - **Adjusted reproducibility estimate**
    - Uncertainty associated with method bias
      - Effects not covered, e.g. sampling uncertainty

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### Other effects

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- Simple “worst case” calculations can often show an effect is negligible
- Formal uncertainty calculations often show negligible components
- Typical criteria:
  - $u < u_{\max}/3$  (<6% effect on combined uncertainty)
  - $u < u_{\max}/5$  (<2% effect on combined uncertainty)
  - ISO/TS 21748 effects  $< 0.2S_R$

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### Numerical calculation

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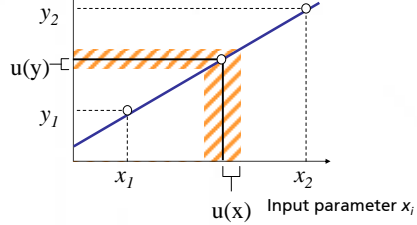


## Other effects: A simple uncertainty experiment



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Measurement  
result  $y$



$$\text{Gradient} = \frac{(y_2 - y_1)}{(x_2 - x_1)}$$

$u(x)$  Input parameter  $x_i$

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## “Other effects”



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$$u_c^2(y) = \hat{s}_R^2 + u^2(\hat{\delta}) + \sum_{i=k,n} c_i^2 u^2(x_i)$$

- Combined uncertainty
- Adjusted reproducibility estimate
  - Uncertainty associated with method bias
  - Effects not covered, e.g. sampling uncertainty

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## Conclusions



Setting standards  
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- ISO TS 21748 provides a recipe for using collaborative study data
- Requires checks for consistency with study performance
- Allows for changes in the test item type
- Often reduces to a simple reproducibility SD

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