Supplementary Text

Ultra-Thin Membrane Characterization Theory

To obtain predictive estimation of the wavelength, amplitude and number of wrinkles, we consider the 1D out-of-plane displacement of an initially flat sheet of area ($W \times L$, where W is width and L is length) as a function of spatial dimension ($\xi(x,y)$) (supplementary figure 1 (b)). The thickness of the sheet, t, is much smaller than W and L, where 0 < y < W, for simplicity, W < <L. When a stretching strain ε is applied in the x direction, then the total energy of the system is:

$$U = U_B + U_S - L \tag{1}$$

Here U_B is the bending energy due to deformation in the y direction:

$$U_B = \frac{1}{2} \int B(\partial y^2 \xi)^2 dA$$
⁽²⁾

where *B* is the bending stiffness. U_S is the stretching energy in presence of tension T(x):

$$U_{S} = \frac{1}{2} \int T(x) (dx\xi)^{2} dA$$
(3)

As the sheet wrinkles in the *y* direction under the action of a small compressive stress, it satisfies the condition of inextensibility,

$$\int_{0}^{L} \left[\frac{1}{2} (\partial y^2 \xi)^2 - \frac{\Delta(x)}{w} \right] dy = 0$$

This constraint is found in the final term of equation 1,

$$L = \int_{A} b(x) \left[\left(\partial y \xi \right)^{2} - \frac{\Delta(x)}{W} \right] dA$$
(4)

where b(x) is the Lagrange multiplier and $\Delta(x)$ imposed the compressive transverse displacement. Boundary Conditions:

$$\xi(0,y) = 0 \ \xi(L,y) = 0$$

After applying boundary conditions we determine:

$$\lambda = \frac{\sqrt{2\pi L t}}{\left(3(1-v^2)\varepsilon\right)^{1/4}} \tag{5}$$

$$A = \sqrt{\nu L t} \left(\frac{16\varepsilon}{3\pi^2 (1 - \nu^2)} \right)^{1/4} \tag{6}$$

where λ is the wavelength and A is the amplitude of the sinusoidal wrinkling (supplementary figure 1 (b)), L is the length of the membrane, t is the thickness of the membrane, v is the Poisson's ratio of the membrane, and ε is the strain of the membrane (Cerda and Mahadevan, 2003). We approximated the number of wrinkles by dividing the wavelength of the wrinkle pattern by the circumference of the water droplet $(\pi d/\lambda)$, where d is the diameter of the droplet.

Cerda E., Mahadevan L., 2003. Phys. Rev. Lett. 90, 074302.



Supplementary Figures



Supplementary figure 2: Overall imaging set-up for the observation of wrinkle patterns generated by cancerous cells. Inset shows 6 devices which each contain ultra-thin membranes, culture media and cells.



-(p) healthy d μт.



Supplementary Figure 3: Wrinkle Patterns Formed by Clinical Patient Samples (a) wrinkle pattern generated by patient 1 after 24 hours (b) wrinkle pattern generated by patient 2 after 24 hours (c) wrinkle pattern generated by patient 5 after 12 hours (d) wrinkle pattern generated by patient 3 after 24 hours (e) wrinkle pattern generated by patient 4 after 12 hours (f) no wrinkle patterns generated by healthy donor control. All scale bars are 20 µm.

s are present. All scale bars are 20



