



$$N(E) = \begin{cases} N & E \leq E_1 \\ 0 & E_1 < E < E_2 \\ N\mathbf{g} & E_2 \leq E \leq E_3 \\ 0 & E_3 < E < E_4 \\ N & E \geq E_4 \end{cases} \quad \begin{aligned} E_2 &= E_1 + E_{g1} \\ E_3 &= E_1 + E_{g1} + \Delta \\ E_4 &= E_1 + E_{g2} \end{aligned} \quad f(E) = \left[ 1 + \exp\left(\frac{E - E_F}{k_B T}\right) \right]^{-1}$$

$$n_e(T) = \int_{E_F=0}^{\infty} N(E)f(E)dE = N \left[ \int_{E_F=0}^{E_1} f(E)dE + \int_{E_4}^{\infty} f(E)dE + I \int_{E_2}^{E_3} f(E)dE \right]$$

$$= N \left[ \begin{aligned} & \left[ -E_{g2} - k_B T \ln \left( \exp\left(\frac{E_1}{k_B T}\right) + 1 \right) + k_B T \ln 2 + k_B T \ln \left( \exp\left(\frac{E_1 + E_{g2}}{k_B T}\right) + 1 \right) \right] \\ & + I \left[ \Delta + k_B T \ln \left( \exp\left(\frac{E_1 + E_{g1}}{k_B T}\right) + 1 \right) - k_B T \ln \left( \exp\left(\frac{E_1 + E_{g1} + \Delta}{k_B T}\right) + 1 \right) \right] \end{aligned} \right]$$

$$n_h(T) = \int_{-\infty}^{E_F=0} N(E)(1-f(E))dE = N \int_{-\infty}^{E_F=0} (1-f(E))dE$$

$$= N k_B T \ln 2$$

$$n_{ch}(T) = \sqrt{n_e(T)n_h(T)} + n_{ch}^0$$

$$\rho(T) = \frac{n_{ch}^0 (\rho_0 + \rho_{ph}(T))}{n_{ch}(T)}$$