

## Supplementary Information

# The origin of a large apparent tortuosity factor for Knudsen diffusion in a samaria aerogel catalyst: a diffusion NMR study

Robert Mueller,<sup>1</sup> Suihua Zhang,<sup>1</sup> Miriam Klink,<sup>2</sup> Marcus Bäumer<sup>2</sup>  
and Sergey Vasenkov<sup>1,a</sup>

<sup>1</sup>*Department of Chemical Engineering, University of Florida, Gainesville, FL 32611 USA*

<sup>2</sup>*Institute for Applied and Physical Chemistry, University of Bremen, 28359, Bremen, Germany*

**Table S1.** Data used in the least-squares regression to Eq. 4 and the resulting values of  $D_p$  model.

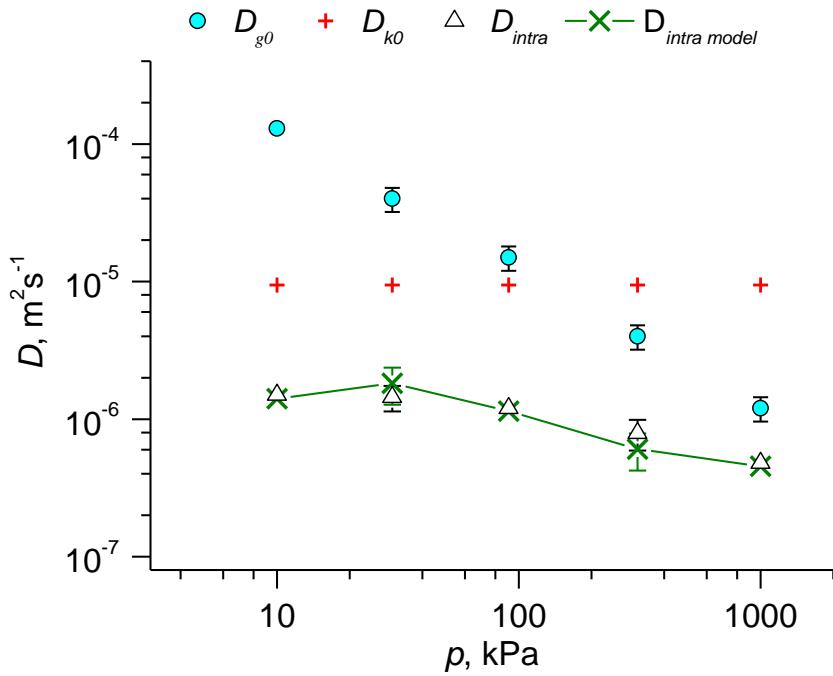
$p$ kPa	$D_{g0}$ $\text{m}^2\text{s}^{-1} (\times 10^{-5})$	$D_{K0}$ $\text{m}^2\text{s}^{-1} (\times 10^{-5})$	$D_{intra}$ $\text{m}^2\text{s}^{-1} (\times 10^{-5})$	$D_p$ model $\text{m}^2\text{s}^{-1} (\times 10^{-5})$
10	13. ± 2	0.94	0.15 ± 0.03	0.14 ± 0.04
30	4.0 ± 0.8	0.94	0.14 ± 0.03	0.14 ± 0.05
91	1.5 ± 0.3	0.94	0.12 ± 0.02	0.12 ± 0.03
310	0.4 ± 0.08	0.94	0.079 ± 0.02	0.087 ± 0.03
1000	0.12 ± 0.02	0.94	0.048 ± 0.01	0.044 ± 0.01

**Table S2.** Data used in the least-squares regression to Eq. 9 and the resulting values of  $D_{intra\ model}$ .

$p$ kPa	$D_{g0}$ $m^2 s^{-1} (\times 10^{-5})$	$D_{K0}$ $m^2 s^{-1} (\times 10^{-5})$	$(1-p_{surf})$	$D_{intra}$ $m^2 s^{-1} (\times 10^{-5})$	$D_{intra\ model}$ $m^2 s^{-1} (\times 10^{-5})$
10	13. ± 2	0.94	0.28 ± 0.06	0.15 ± 0.03	0.13 ± 0.04
30	4.0 ± 0.8	0.94	0.41 ± 0.09	0.14 ± 0.03	0.17 ± 0.05
91	1.5 ± 0.3	0.94	0.35 ± 0.07	0.12 ± 0.02	0.11 ± 0.03
310	0.4 ± 0.08	0.94	0.38 ± 0.08	0.079 ± 0.02	0.066 ± 0.02
1000	0.12 ± 0.02	0.94	0.75 ± 0.15	0.048 ± 0.01	0.052 ± 0.02

**Table S3.** Data used in the least-squares regression to the modified Eq. 9 where  $\eta_K = \eta_g \equiv \eta$  and the resulting values of  $D_{intra\ model}$ .

$p$ kPa	$D_{g0}$ $m^2 s^{-1} (\times 10^{-5})$	$D_{K0}$ $m^2 s^{-1} (\times 10^{-5})$	$(1-p_{surf})$	$D_{intra}$ $m^2 s^{-1} (\times 10^{-5})$	$D_{intra\ model}$ $m^2 s^{-1} (\times 10^{-5})$
10.	13. ± 2	0.94	0.28 ± 0.06	0.15 ± 0.03	0.14 ± 0.04
30.	4.0 ± 0.8	0.94	0.41 ± 0.09	0.14 ± 0.03	0.18 ± 0.05
91.	1.5 ± 0.3	0.94	0.35 ± 0.07	0.12 ± 0.02	0.11 ± 0.03
310 ± 50	0.4 ± 0.08	0.94	0.38 ± 0.08	0.079 ± 0.02	0.060 ± 0.02
1000 ± 150	0.12 ± 0.02	0.94	0.75 ± 0.15	0.048 ± 0.01	0.045 ± 0.01



**Figure S1.**  $\text{CO}_2$  self-diffusivity,  $D_{intra}$ , measured by  $^{13}\text{C}$  PFG NMR inside the particles of the studied samaria aerogel catalyst at 297 K and the corresponding theoretical diffusivity,  $D_{intra\ model}$ , obtained by least-squares regression of the diffusion data reported in the figure to the modified Eq. 9 where  $\eta_K = \eta_g \equiv \eta$ . Also shown for comparison are the following self-diffusivities of  $\text{CO}_2$  molecules at 297 K: self-diffusivity in the macroscopic gas volume surrounding the catalyst ( $D_{g0}$ ), and the reference self-diffusivity in the Knudsen regime estimated by using Eq. 2 with  $d = 75$  nm ( $D_{k0}$ ). All diffusivities are presented as a function of the  $\text{CO}_2$  equilibrium pressure in the gas volume surrounding the catalyst particles at 297 K.