

## Electron Work Function: A Novel Probe for Toughness

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**Table I** Calculated lattice constants, elastic constants, bulk modulus (B), shear modulus (G), Young modulus (E)

	Lattice Constants( <b>Error!</b> )		Elastic Constants and Modulus (GPa)							
	a	c	C <sub>11</sub>	C <sub>12</sub>	C <sub>13</sub>	C <sub>33</sub>	C <sub>44</sub>	B	G	E
Be	2.257	3.563	320.6	22.5	14.8	378.6	163.7	124.6	159.5	335.3
	2.286 <sup>a</sup>	3.585 <sup>a</sup>	292.3 <sup>a</sup>	26.7 <sup>a</sup>	14.0 <sup>a</sup>	336.4 <sup>a</sup>	162.5 <sup>a</sup>	100 <sup>b</sup>		303 <sup>c</sup>
Mg	3.195	5.2	68.1	21.3	19.9	61.9	12.6	35.5	18.1	46.4
	3.209 <sup>a</sup>	5.211 <sup>a</sup>	59.50 <sup>a</sup>	26.12 <sup>a</sup>	21.80 <sup>a</sup>	61.55 <sup>a</sup>	16.35 <sup>a</sup>	35.4 <sup>b</sup>		44 <sup>c</sup>
Sc	3.309	5.253	102.7	27.8	26.3	100.9	31.1	51.9	34.8	85.4
	3.309 <sup>a</sup>	5.268 <sup>a</sup>	99.3 <sup>a</sup>	39.7 <sup>a</sup>	29.4 <sup>a</sup>	107 <sup>a</sup>	27.7 <sup>a</sup>	56.6 <sup>c</sup>	29.1 <sup>c</sup>	74.4 <sup>c</sup>
V	3.0		265.5	139			28.4	181.1	39.4	110.2
	3.024 <sup>a</sup>		228.7 <sup>a</sup>	119 <sup>a</sup>			43.2 <sup>a</sup>	161.9 <sup>b</sup>	46.4 <sup>c</sup>	124 <sup>c</sup>
Fe	2.829		286.9	163.9			110	204.9	87.2	229
	2.866 <sup>a</sup>		226 <sup>a</sup>	140 <sup>a</sup>			116 <sup>a</sup>	168.3 <sup>b</sup>	80.6 <sup>c</sup>	208.2 <sup>c</sup>
Co	2.5	3.941	404.75	149.5	138.9	428.1	99.6	232.5	118.1	303.1
	2.507 <sup>a</sup>	4.069 <sup>a</sup>	307.1 <sup>a</sup>	165 <sup>a</sup>	102.7 <sup>a</sup>	358.1 <sup>a</sup>	75.5 <sup>a</sup>	191.4 <sup>b</sup>		211 <sup>c</sup>
Ni	3.525		248.8	140.8			117.7	176.8	86.1	222.1
	3.524		248.1 <sup>a</sup>	154.9 <sup>a</sup>			124.2 <sup>a</sup>	186 <sup>b</sup>	76 <sup>c</sup>	207 <sup>c</sup>
Cu	3.595		170.2	120.3			57.9	136.9	41.3	112.5
	3.615 <sup>a</sup>		168.3 <sup>a</sup>	122.1 <sup>a</sup>			75.7 <sup>a</sup>	137 <sup>b</sup>	46.8 <sup>c</sup>	128 <sup>c</sup>
Y	3.644	5.78	76.5	19	20.5	77.8	25.2	39	27.2	66.2
	3.648 <sup>a</sup>	5.732 <sup>a</sup>	77.90 <sup>a</sup>	28.50 <sup>a</sup>	21.00 <sup>a</sup>	76.90 <sup>a</sup>	24.31 <sup>a</sup>	36.6 <sup>b</sup>	25.6 <sup>c</sup>	63.5 <sup>c</sup>
Nb	3.309		240	132.3			12.7	168.2	23.7	68
	3.3 <sup>a</sup>		246.5 <sup>a</sup>	134.5 <sup>a</sup>			28.73 <sup>a</sup>	170 <sup>b</sup>	37.5 <sup>c</sup>	103 <sup>c</sup>
Mo	3.161		454	167.2			103.7	262.8	118	308
	3.147 <sup>a</sup>		463.7 <sup>a</sup>	157.8 <sup>a</sup>			109.2 <sup>a</sup>	272.5 <sup>b</sup>		329 <sup>c</sup>
Rh	3.836		337.2	145.4			148.3	209.3	124.5	311.8
	3.803 <sup>a</sup>		413 <sup>a</sup>	194 <sup>a</sup>			184 <sup>a</sup>	270.4 <sup>b</sup>		293 <sup>c</sup>
W	3.185		493.8	204			136.8	300.6	140	363.5
	3.165 <sup>a</sup>		522.4 <sup>a</sup>	204.4 <sup>a</sup>			160.83 <sup>a</sup>	323.2 <sup>b</sup>		375 <sup>c</sup>
Ir	3.873		583.9	241.9			249.59	355.9	214.5	535.85
	3.839 <sup>a</sup>		580 <sup>a</sup>	242 <sup>a</sup>			256 <sup>a</sup>	355 <sup>b</sup>		517 <sup>c</sup>
Cr	2.8778		451.2	145.03			106.3	247.1	123.1	316.7

	2.8848 <sup>a</sup>		339.8 <sup>a</sup>	58.6 <sup>a</sup>			99 <sup>a</sup>	190.1 <sup>b</sup>		248 <sup>c</sup>
Ti	2.9348	4.6585	160.7	84.9	80.5	164.7	13.5	108.7	25.6	71.4
	2.9506 <sup>a</sup>	4.6835 <sup>a</sup>	162.4 <sup>a</sup>	92 <sup>a</sup>	69 <sup>a</sup>	180.7 <sup>a</sup>	46 <sup>a</sup>	105.1 <sup>b</sup>		
Zn	2.6695	4.9553	146.3	47.3	50.3	75	23.3	70.1	31.4	81.9
	2.665 <sup>a</sup>	4.947 <sup>a</sup>	163.6 <sup>a</sup>	36.4 <sup>a</sup>	53 <sup>a</sup>	63.47 <sup>a</sup>	38.79 <sup>a</sup>	59.8 <sup>b</sup>		
Zr	3.2315	5.1473	134.4	67.4	70.9	156.9	13.4	93.5	23.9	66.1
	3.2316 <sup>a</sup>	5.1475 <sup>a</sup>	143.4 <sup>a</sup>	72.8 <sup>a</sup>	65.3 <sup>a</sup>	164.8 <sup>a</sup>	32 <sup>a</sup>	83.3 <sup>b</sup>		99.2 <sup>c</sup>
Ru	2.721	4.3057	536.5	212.5	201.1	570.9	165.7	319.2	167.1	426.9
	2.7058 <sup>a</sup>	4.2816 <sup>a</sup>	562.6 <sup>a</sup>	187.8 <sup>a</sup>	168.2 <sup>a</sup>	624.2 <sup>a</sup>	180.6 <sup>a</sup>	320.8 <sup>b</sup>		

Note: the data with superscript (a) are cited from ref. [1], (b) are cited from ref.[2], (c) are cited from ref.[3]

**Table II** Surface energy ( $\gamma_s$ ), electron work function ( $\varphi$ ), elongation (El(%)), the ideal tensile strength (ITS), the ideal shear strength(ISS), the tensile strain energy density ( $W_{\text{tensile}}$ ), the shear strain energy density ( $W_{\text{shear}}$ ), the reciprocal of brittleness ( $\beta^{-1}$ ) and the fracture toughness ( $K_{IC}$ )

	$\gamma_s$ (J/m <sup>2</sup> )	$\varphi$ (eV)	El(%)	ITS (GPa)	ISS (GPa)	$W_{\text{tensile}}$ (GPa)	$W_{\text{shear}}$ (GPa)	$\beta^{-1}$	$K_{IC}$ (MPam <sup>0.5</sup> )
Be	1.71	5.09	2 <sup>d</sup>	23.3	15.9	3.4	1.4	2.45	6.2
	1.68 <sup>a</sup>	4.98 <sup>c</sup>							10.9 <sup>g</sup>
Mg	0.58	3.69	5 <sup>d</sup>	5.9	1.4	1.5	0.13	11.51	18.3
	0.76 <sup>b</sup>	3.66 <sup>c</sup>						13.04 <sup>f</sup>	15~40 <sup>h</sup>
Sc	1.450	3.47	5e	13	2.8	3.8	0.24	15.75	42.1
	1.28 <sup>b</sup>	3.5 <sup>c</sup>							
V	2.399	4.12	39 <sup>d</sup>	34	6.3	10.4	0.86	12.02	90.8
	2.55 <sup>b</sup>	4.3 <sup>c</sup>							124 <sup>i</sup>
Fe	2.16	4.61	45 <sup>d</sup>	32.4	7.8	10.1	0.92	10.97	87.9
	2.48 <sup>b</sup>	4.5 <sup>c</sup>						12.89 <sup>f</sup>	50~90 <sup>j</sup>
Co	2.43	4.77	14 <sup>d</sup>	34.2	6.9	7.6	0.67	11.42	104.8
	2.55 <sup>b</sup>	5.0 <sup>c</sup>							
Ni	2.6	4.9	30 <sup>e</sup>	33.1	5.9	7.4	0.73	10.21	68.1
	2.45 <sup>b</sup>	5.15 <sup>c</sup>						22.59 <sup>f</sup>	100~`50 <sup>f</sup>
Cu	1.460	4.26	48 <sup>d</sup>	24.5	2.8	5.4	0.36	14.9	90.4
	1.83 <sup>b</sup>	4.65 <sup>c</sup>						33.86 <sup>f</sup>	100~107 <sup>f</sup>
Y	1.11	2.87	25 <sup>d</sup>	9.7	2.2	2.8	0.19	14.9	30.7
	1.13 <sup>b</sup>	3.1 <sup>c</sup>							
Nb	2.8	4.27	30 <sup>e</sup>	27.6	7.0	8.7	1.04	8.4	53.6
	2.7 <sup>b</sup>	4.3 <sup>c</sup>							37 <sup>k</sup>
Mo	2.824	4.62	20 <sup>d</sup>	41.2	15.5	10.3	2.27	4.53	34.5
	3.0 <sup>b</sup>	4.6 <sup>c</sup>						8.94 <sup>f</sup>	21 <sup>k</sup>
Rh	2.32	5.1		37.6	12.9	6.8	1.59	4.27	24.8
	2.7 <sup>b</sup>	4.98 <sup>c</sup>							

W	3.266 3.68 <sup>b</sup>	4.38 4.55 <sup>c</sup>	30 <sup>e</sup>	49.4	17.5	12.9	2.62	4.94 9.95 <sup>f</sup>	44.7 9~39 <sup>k</sup>
Ir	2.67 3.0 <sup>b</sup>	5.37 5.27 <sup>c</sup>	13 <sup>e</sup>	46	18.6	6.0	2.29	2.63	21.5
Cr	3.0 2.3 <sup>b</sup>	4.81 4.5 <sup>c</sup>	3 <sup>e</sup>	45.64	16.64	13.83	2.99	4.63	31.9
Ti	2.7 2.1 <sup>b</sup>	4.46 4.33 <sup>c</sup>	54 <sup>e</sup>	23.97	2.87	8.55	0.44	19.26 53 <sup>f</sup>	110.12
Zn	0.71 0.99 <sup>b</sup>	4.29 4.33 <sup>c</sup>		4.47	2.16	1.84	0.23	7.96 13.733 <sup>f</sup>	20.15 28.3 <sup>l</sup>
Zr	1.91 2.0 <sup>b</sup>	4.32 4.05 <sup>c</sup>	32 <sup>e</sup>	19.34	1.57	4.87	0.26	18.7	95.38 30~120 <sup>m</sup>
Ru	2.58 3.05 <sup>b</sup>	4.77 4.71 <sup>c</sup>		43.55	16.47	10.06	2.0	5.02	47.27

Note: the data with superscript (a) cited from ref. [4], (b) cited from ref. [5], (c) cited from ref.[6], (d) cited from ref. [7], (e) cited from ref.[3], (f) cited from ref.[8], (g) cited from ref. [9], (h) cited from ref. [10], (i) cited from ref. [11], (j) cited from ref.[12], (k) cited from ref.[13], (l) cited from ref[14]., (m) cited from ref.[15].

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