

Electronic Supplementary Information

Improved Benzene Production from Methane Dehydroaromatization over Mo/HZSM-5 Catalysts via Hydrogen-Permselective Palladium Membrane Reactors

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Table S1 Experimental matrix of the permeation study

Effect	Gas Mixtures	$Y_{H_2, \text{feed}}$ (mol%)	$Q_{Ar, \text{sweep}}$ ($\text{cm}^3 \text{min}^{-1}$)	Q_{feed} ($\text{cm}^3 \text{min}^{-1}$)	T (°C)
Sweep gas flow rate	H ₂ /N ₂	1/5/10/25	50/350/700	50	350
Feed gas flow rate	H ₂ /N ₂	1/5/10/25	350	50/500/2000	350
Membrane temperature	H ₂ /N ₂	10	350	50	350/450/550/700
Presence of CH ₄	H ₂ /N ₂ , H ₂ /CH ₄	10	350	50	700

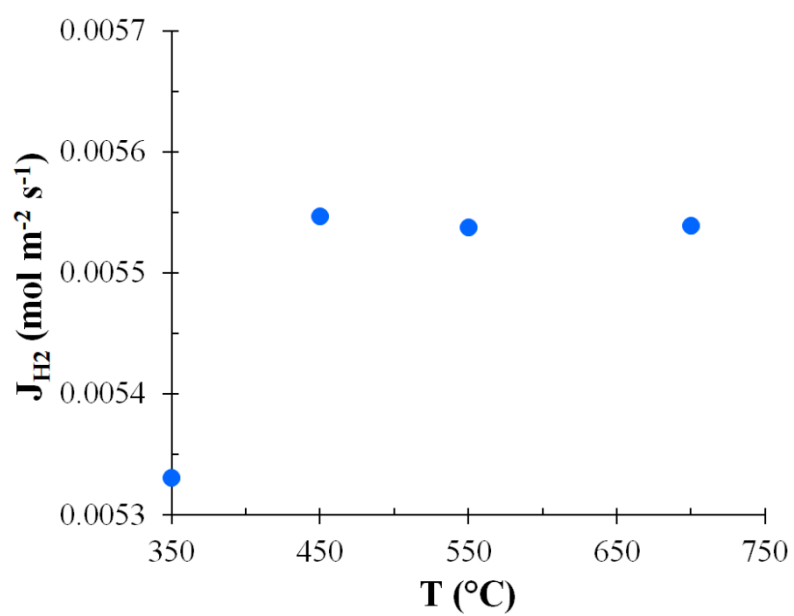


Fig. 1S Effect of temperature on H₂ flux for the Pd membrane packed with HZSM-5. Testing conditions are as follows: T = 350, 450, 550, and 700 °C, Feed = 10% H₂/N₂, Q_{Feed} = 50 cm³ min⁻¹, Q_{Ar, sweep} = 350 cm³ min⁻¹.

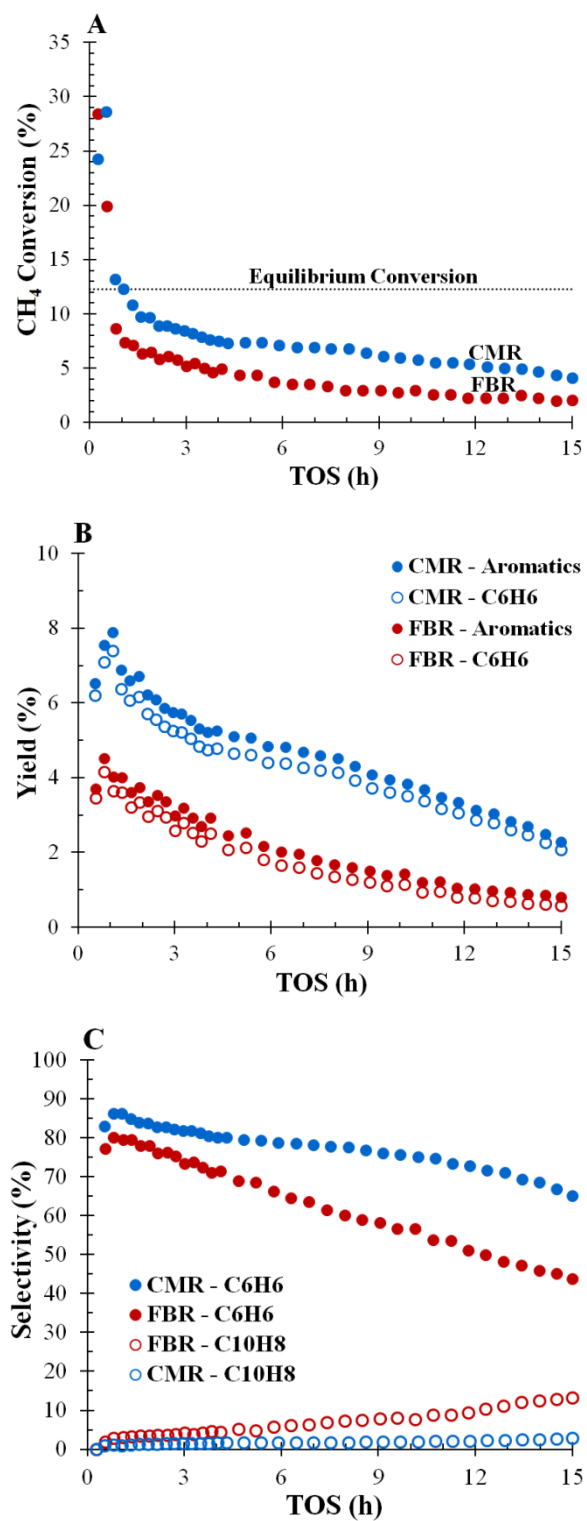


Fig. 2S Comparison of the performance of the 4% Mo/HZSM-5 catalyst in FBR and CMR at $3000 \text{ cm}^3 \text{ g}_{\text{cat}}^{-1} \text{ h}^{-1}$ (A) CH₄ conversion (B) C₆H₆ and aromatic yields (C) selectivity to C₆H₆ and C₁₀H₈.

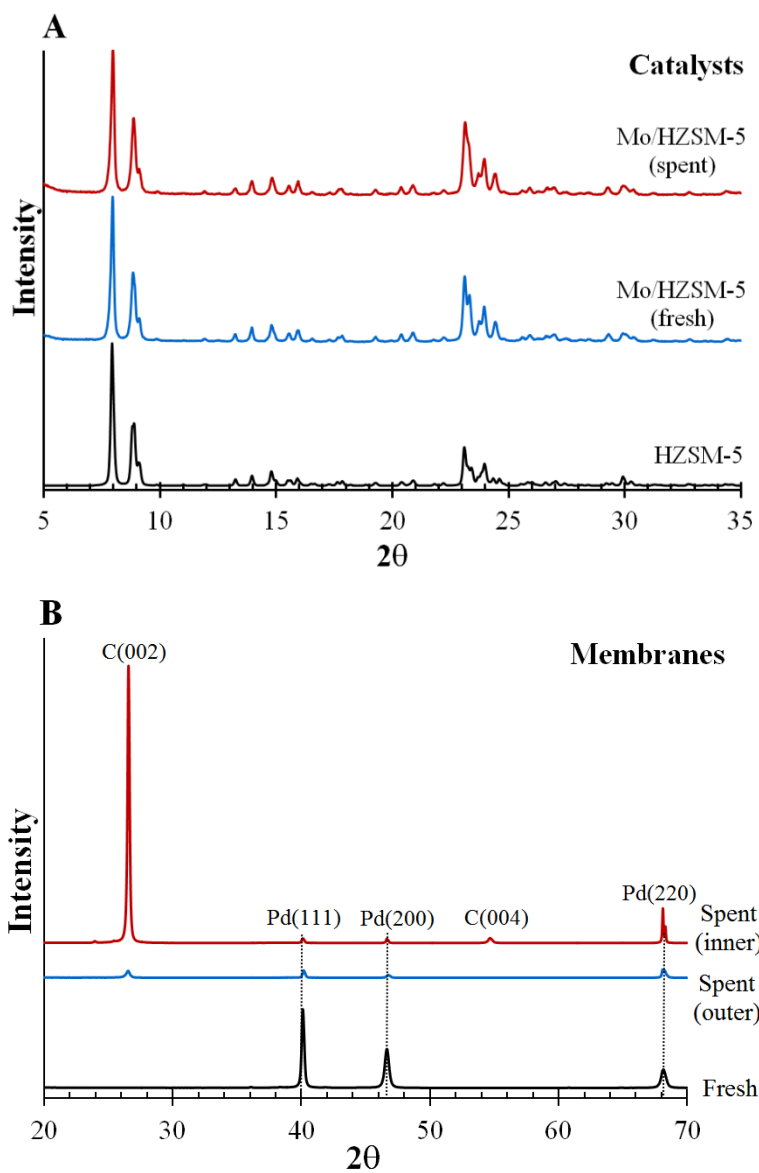


Fig. 3S XRD patterns of fresh and spent materials: (A) Mo/HZSM-5 (B) Pd membranes. The XRD pattern of HZSM-5 is included for comparison.

Mears criterion calculations*

External mass transfer limitations can be neglected if the Mears criterion listed below is satisfied.

$$\frac{-r_{A(Obs)} \times \rho_b \times R \times n}{k_c \times C_{Ab}} < 0.15$$

Where $-r_{A(Obs)}$ is the observed reaction rate ($\text{kmol kg}_{\text{cat}}^{-1} \text{s}^{-1}$), ρ_b is the catalyst bed density (kg m^{-3}), R is the catalyst pellet radius (m), n is the reaction order of reactant A, k_c is the mass transfer coefficient of reactant A, and C_{Ab} is the concentration of reactant A in the bulk gas phase (kmol m^{-3}).

In this study, $\rho_b = 1099.2 \text{ kg m}^{-3}$ and $R = 1.5 \times 10^{-4} \text{ m}$ for 4 wt% Mo/HZSM-5 catalyst. For CH_4 dehydroaromatization, $n = 6$.

For flow over a sphere with very low Reynolds number, Sherwood number (Sh) = 2:

$$Sh = \frac{k_c \times 2R}{D_e}$$

Where D_e is the estimated diffusivity of CH_4 in the bulk gas phase. At $700 \text{ }^\circ\text{C}$, $D_e = 4.33 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$.

$$k_c = \frac{2 \times 4.33 \times 10^{-5}}{2 \times 1.5 \times 10^{-4}} = 0.289 \text{ m s}^{-1}.$$

At $T = 700 \text{ }^\circ\text{C}$, $\text{WHSV} = 750 \text{ cm}^3 \text{ g}_{\text{cat}}^{-1} \text{ h}^{-1}$, $\text{TOS} = 15 \text{ h}$, $-r_{A(Obs)} = 1.014 \times 10^{-7} \text{ kmol kg}_{\text{cat}}^{-1} \text{ s}^{-1}$, $C_{Ab} = 8.878 \times 10^{-3} \text{ kmol m}^{-3}$.

$$\frac{1.014 \times 10^{-7} \times 1099.2 \times 1.5 \times 10^{-4} \times 6}{0.289 \times 8.878 \times 10^{-3}} = 3.910 \times 10^{-5} \ll 0.15$$

At $T = 700 \text{ }^\circ\text{C}$, $\text{WHSV} = 9000 \text{ cm}^3 \text{ g}_{\text{cat}}^{-1} \text{ h}^{-1}$, $\text{TOS} = 15 \text{ h}$, $-r_{A(Obs)} = 2.017 \times 10^{-7} \text{ kmol kg}_{\text{cat}}^{-1} \text{ s}^{-1}$, $C_{Ab} = 1.081 \times 10^{-2} \text{ kmol m}^{-3}$.

$$\frac{2.017 \times 10^{-7} \times 1099.2 \times 1.5 \times 10^{-4} \times 6}{0.289 \times 1.081 \times 10^{-2}} = 6.387 \times 10^{-5} \ll 0.15$$

Therefore, the Mears criterion calculations confirm the absence of external mass transfer limitations.

*Reference

W.S. Lee, Z. Wang, W. Zheng, D.G. Vlachos, A. Bhan, *Catal. Sci. Technol.*, 2014, **4**, 2340-2352.