## **Electronic Supplemental Information**

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**Figure S1.** Computed phonon density of states (DOS) of unstrained TMTC monolayer: (a)  $HfS_3$ , (b)  $HfSe_3$ . The linear response method, implemented in CASTEP 7.0, was adopted to compute the phonon DOS. More specifically, the PBE functional was chosen; and the energy cut off was set to 650 eV for  $HfS_3$  and 400 eV for  $HfSe_3$ , for both structural optimization and phonon DOS computation. The density of Monkhorst-Pack q-vectors  $3 \times 4 \times 1$  was selected. The vacuum space was greater than 15 Å.



**Figure S2.** Computed PDOS (optB86b-vdW functional) of unstrained TMTC monolayers: (a)  $ZrS_3$ , (b) HfS<sub>3</sub>, (c) TiS<sub>3</sub>, and (d) NbS<sub>3</sub>. The red lines denote the  $d_{z^2}$  and  $d_{x^2-y^2}$  orbitals of M atom, the green lines denote the  $d_{xz}$  orbital of M atom. The blue lines denote the  $p_x$  and  $p_y$  orbitals of X atom, and the yellow lines denote the  $p_z$  orbital of X atom. The Vertical dashed line denotes the Fermi level.



**Figure S3.** Computed band structures of strained monolayer  $\text{ZrSe}_3$  *versus* biaxial tensile strain (xy) in both x and y directions, the uniaxial tensile strain in x direction (xx) or y direction (yy). The red lines denote the  $d_z^2$  orbital of the Zr atom. The green lines denote the  $d_x^2 - y^2$  orbital of Zr atom. The cyan lines denote the  $d_{xy}$ ,  $d_{yz}$  and  $d_{xz}$  orbitals of Zr atom. The blue lines denote the  $p_x$  and  $p_y$  orbitals of Se atom, and the yellow lines denote the  $p_z$  orbital of Se atom. The dashed line indicates the Fermi level. I refers to either the VBM or CBM that is not located at the  $\Gamma$  point.



**Figure S4.** Band structures of unstrained monolayers: (a)  $HfS_3$ , (b)  $HfSe_3$ , (c)  $HfTe_3$ . The red lines denote the  $d_z^2$  orbital of Hf atom. The green lines denote the  $d_x^2 - y^2$  orbitals of Hf atom. The cyan lines denote the  $d_{xy}$ ,  $d_{yz}$  and  $d_{xz}$  orbitals of Hf atom. The blue lines denote the  $p_x$  and  $p_y$  orbitals of (a) S, (b) Se, and (c) Te atom, and the yellow lines denote the  $p_z$  obital of (a) S, (b) Se, and (c) Te atom.



**Figure S5.** Computed band structures of strained monolayer  $HfS_3$  *versus* biaxial tensile strain in both x and y directions (xy), the uniaxial tensile strain in x direction (xx) or y direction (yy). The red and green lines illustrate the  $d_z^2$  orbital and the  $d_x^2 - y^2$  orbital of Hf atom, respectively. The cyan lines denote the  $d_{xy}$ ,  $d_{yz}$  and  $d_{xz}$  orbitals of Hf atom. The blue lines denote the  $p_x$  and  $p_y$  orbitals of S atom, and the yellow lines denote the  $p_z$  obital of S atom. The dashed lines indicate the Fermi level.



**Figure S6.** Computed band structures of stained monolayer  $HfSe_3$  *versus* biaxial tensile strain (xy) in both x and y directions, the uniaxial tensile strain in x direction (xx) or y direction (yy). The red lines denote the  $d_z^2$  orbital of Hf atom. The green lines denote the  $d_{xy}$ ,  $d_{yz}$  and  $d_{xz}$  orbitals of Hf atom. The blue lines denote the  $p_x$  and  $p_y$  orbitals of Se atom, and the yellow lines denote the  $p_z$  obital of Se atom. The dashed lines indicate the Fermi level.



**Figure S7.** Computed band structures of strained monolayer HfTe<sub>3</sub> *versus* biaxial tensile strain in both x and y directions (xy), the uniaxial tensile strain in x direction (xx) or y direction (yy). The red and green lines illustrate the  $d_z^2$  orbital and the  $d_x^2 - y^2$  orbital of Hf atom, respectively. The cyan lines denote the  $d_{xy}$ ,  $d_{yz}$  and  $d_{xz}$  orbitals of Hf atom. The blue lines denote the  $p_x$  and  $p_y$  orbitals of Te atom, and the yellow lines denote the  $p_z$  obital of Te atom. The dashed lines indicate the Fermi level.



**Figure S8.** Band structures of unstrained monolayers: (a) TiS<sub>3</sub> and (b) NbSe<sub>3</sub>. The red lines denote the  $d_z^2$  orbital of (a) Ti atom and (b) Nb atom. The green lines denote the  $d_x^2 - y^2$  orbitals of (a) Ti atom and (b) Nb atom. The cyan lines denote the  $d_{xy}$ ,  $d_{yz}$  and  $d_{xz}$  orbitals of (a) Ti atom and (b) Nb atom. The cyan lines denote the  $p_x$  and  $p_y$  orbitals of S atom, and the yellow lines denote the  $p_z$  obital of the S atom. The dashed lines indicate the Fermi level.