

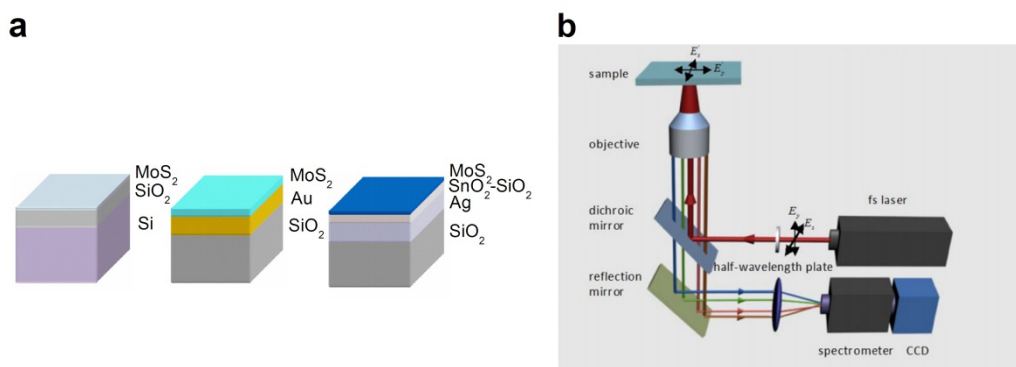
# Supporting Information

## Revealing Silent Vibration Modes of Nanomaterials by Detecting Anti-Stokes Hyper-Raman Scattering with Femtosecond Laser Pulses

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### SI-1 Sample structure and experimental setup

MoS<sub>2</sub> layers with different thicknesses were exfoliated on different substrates of SiO<sub>2</sub>/Si, Au/SiO<sub>2</sub> and SiO<sub>2</sub>-SnO<sub>2</sub>/Ag/SiO<sub>2</sub>, as schematically shown in Fig. S1(a). The color exhibited by a MoS<sub>2</sub> layer depends strongly on the thickness of the MoS<sub>2</sub> layer and the substrate used. The experimental setup used to characterize the nonlinear optical properties of the nanomaterials is schematically shown in Fig. S1(b). The fs laser pulses were reflected by a dichroic mirror and focused on the samples by using the objective lens of an inverted microscope. The nonlinear signals generated by the nanomaterials were collected by the same objective lens and directed to a spectrometer for analysis.

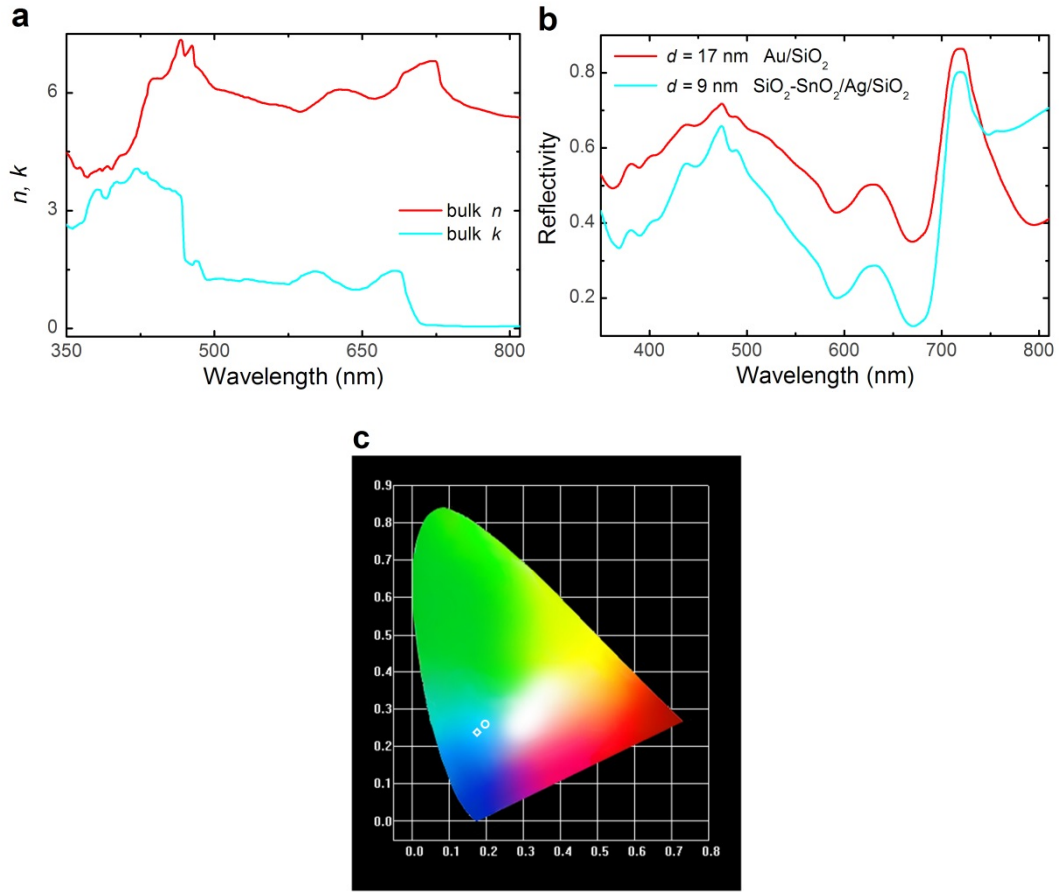


**Fig. S1** (a) MoS<sub>2</sub> layers exfoliated on a SiO<sub>2</sub>/Si, an Au/SiO<sub>2</sub> and a SiO<sub>2</sub>-SnO<sub>2</sub>/Ag/SiO<sub>2</sub> substrate. (b) Experimental setup used to characterize the nonlinear optical responses of the MoS<sub>2</sub> layers on the SiO<sub>2</sub>/Si, Au/SiO<sub>2</sub> and SiO<sub>2</sub>-SnO<sub>2</sub>/Ag/SiO<sub>2</sub> substrate and other nanomaterials.

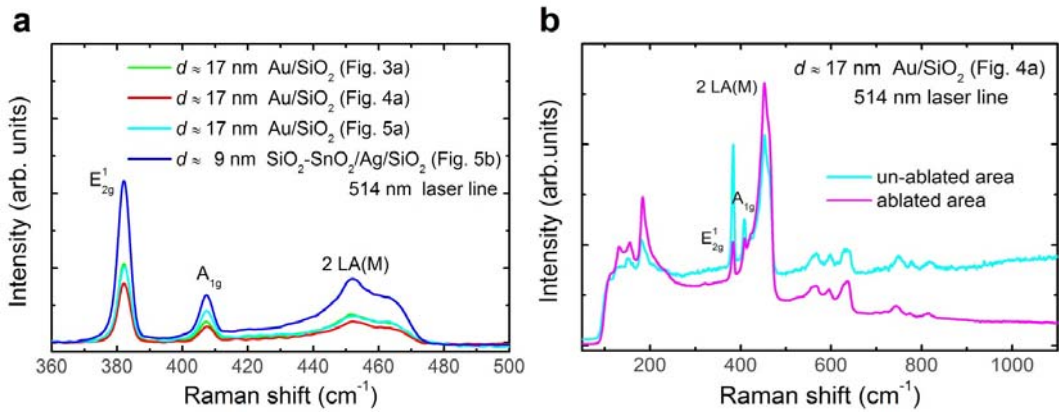
### SI-2 Linear optical properties of MoS<sub>2</sub> layers on different substrates

The complex refractive index of MoS<sub>2</sub> used to calculate the reflection spectra of the MoS<sub>2</sub> layers on different substrates is shown in Fig. S2(a). The reflection spectra calculated for the 17 nm MoS<sub>2</sub> layer on the Au/SiO<sub>2</sub> substrate and the 9 nm MoS<sub>2</sub> layer on the SiO<sub>2</sub>-SnO<sub>2</sub>/Ag/SiO<sub>2</sub> substrate are presented in Fig. S2(b). The Chromaticity coordinates derived for the 17 nm-thick MoS<sub>2</sub> on the Au/SiO<sub>2</sub> substrate and the 9 nm-thick MoS<sub>2</sub> on the SiO<sub>2</sub>-SnO<sub>2</sub>/Ag/SiO<sub>2</sub> substrate based on their reflection spectra shown in Fig. S2(b) are presented in Fig. S2(c). The Raman spectra measured for the 17 nm-thick MoS<sub>2</sub> on the Au/SiO<sub>2</sub> substrate and the 9 nm-thick MoS<sub>2</sub> on the SiO<sub>2</sub>-SnO<sub>2</sub>/Ag/SiO<sub>2</sub> substrate at an excitation wavelength of 514 nm are presented in Fig. S3(a). Two peaks located at 382.2 and 407.4 cm<sup>-1</sup>, which are attributed to the in-plane (E<sub>2g</sub><sup>1</sup>) and out-of-plane (A<sub>1g</sub>) vibration modes, were clearly resolved in the Raman spectra. The MoS<sub>2</sub> layers were confirmed to be bulk material by the frequency difference between the two modes which is estimated to be 25.2 cm<sup>-1</sup>.<sup>S3</sup> When the excitation power of the fs laser light exceeds a critical value, the ablation of the MoS<sub>2</sub> layer may occur, leading to the reduction in the thickness, as shown in Fig. 4(a). A change in both the SHG intensity and the film color was observed. In order to find out the physical origin for the change in SHG intensity and film color, we measured the Raman scattering spectra for the un-ablated and ablated areas of the 17 nm-thick MoS<sub>2</sub> layer on the Au/SiO<sub>2</sub> substrate, as

shown in Fig. S3(b). Except the signal intensity, we found no change in the Raman scattering peaks, indicating that the irradiation of fs laser pulses results in the ablation of MoS<sub>2</sub> rather than the 2H to 1T/T' phase transition.



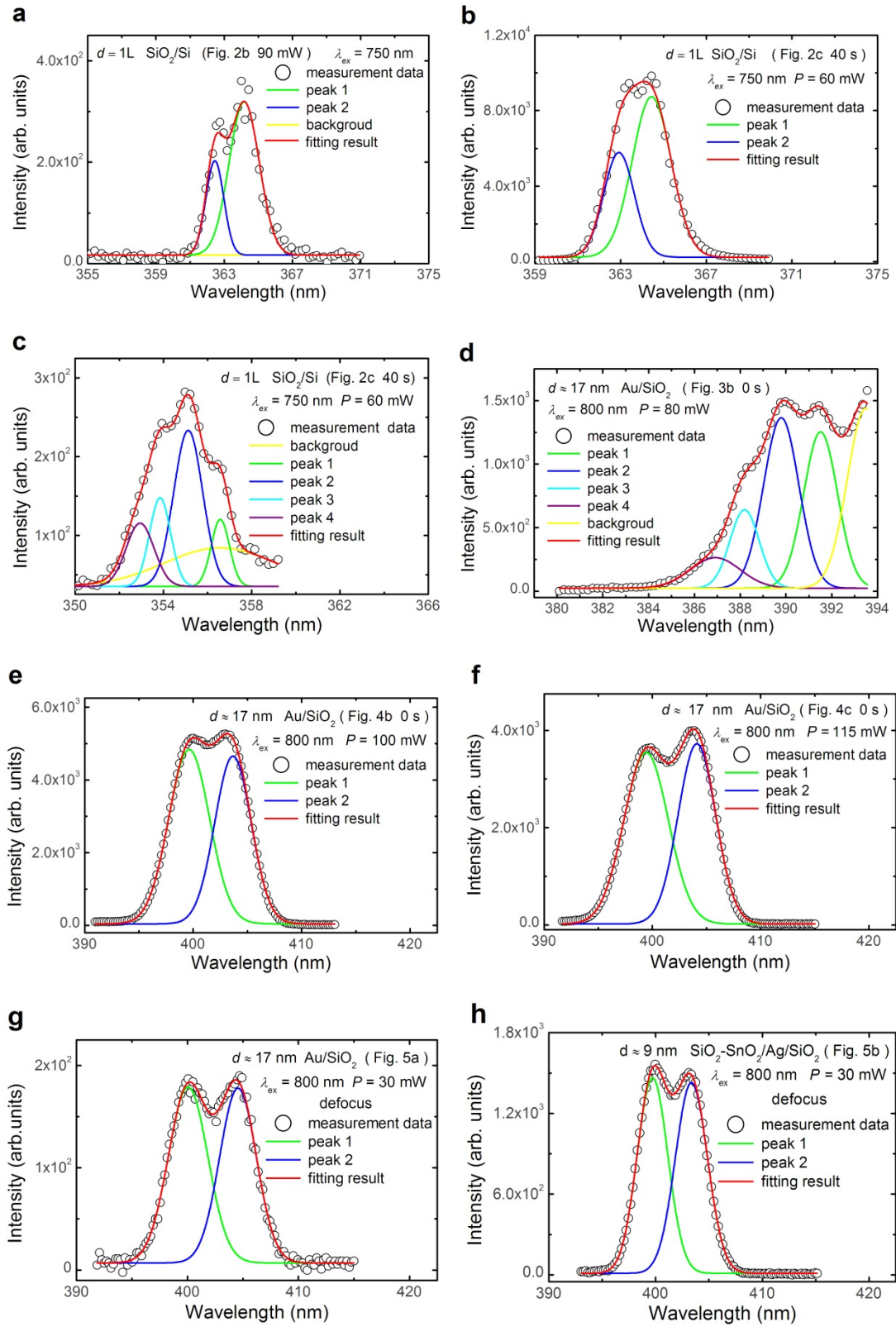
**Fig. S2** (a) Complex refractive index of MoS<sub>2</sub> used in the calculation of the reflection spectra. (b) Reflection spectra calculated for the 17 nm-thick MoS<sub>2</sub> on the Au/SiO<sub>2</sub> substrate and the 9 nm-thick MoS<sub>2</sub> on the SiO<sub>2</sub>-SnO<sub>2</sub>/Ag/SiO<sub>2</sub> substrate. (c) Chromaticity coordinates derived for the 17 nm-thick MoS<sub>2</sub> on the Au/SiO<sub>2</sub> substrate (circle) and the 9 nm-thick MoS<sub>2</sub> on the SiO<sub>2</sub>-SnO<sub>2</sub>/Ag/SiO<sub>2</sub> substrate (rhomb) based on the reflection spectra shown in (b). Complex refractive indexes of Au, Ag, Si and SiO<sub>2</sub> used in the numerical simulations are based on Refs. S1 and S2.

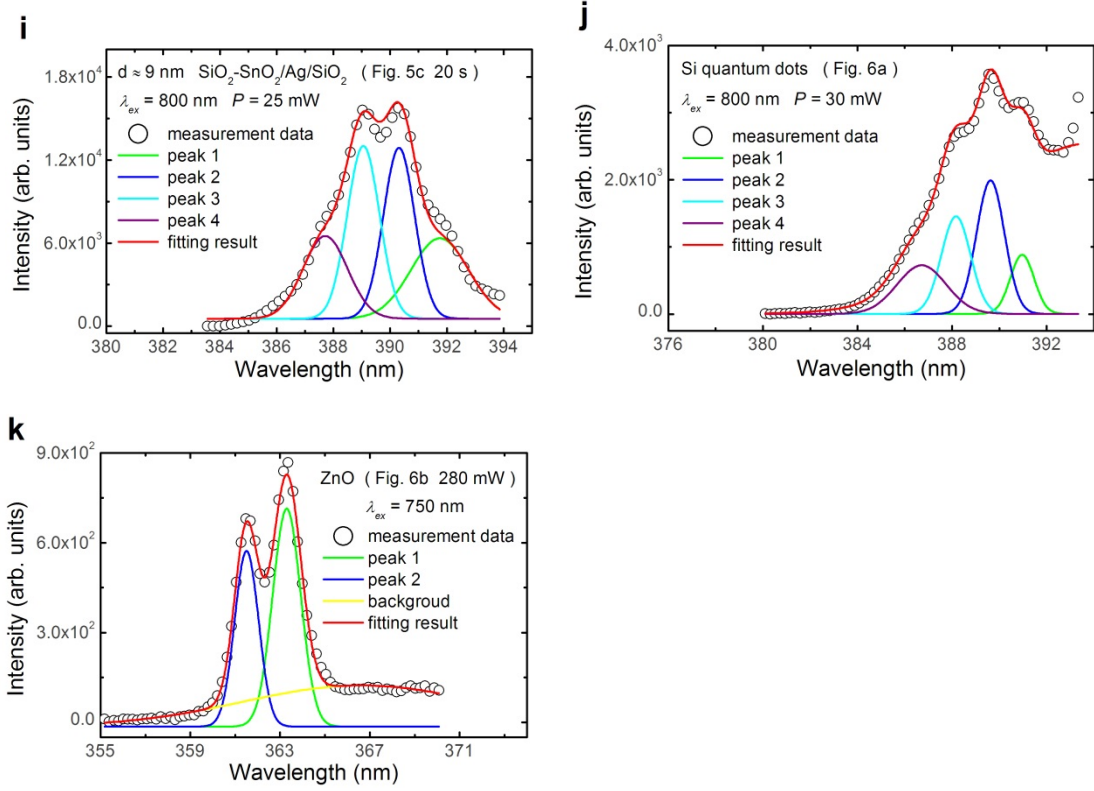


**Fig. S3** (a) Raman scattering spectra measured at 514 nm for the 17 nm-thick MoS<sub>2</sub> layer on the Au/SiO<sub>2</sub> substrate shown in Figs. 3a, 4a and 5a and the 9 nm-thick MoS<sub>2</sub> layer on the SiO<sub>2</sub>-SnO<sub>2</sub>/Ag/SiO<sub>2</sub> substrate shown in Fig. 5b. (b) Raman scattering spectra measured at 514 nm for the un-ablated and ablated areas of the 17 nm-thick MoS<sub>2</sub> layer on the Au/SiO<sub>2</sub> substrate shown in Fig. 4a.

### SI-3 Multiple Gaussian fitting of the hyper-Raman scattering spectra

In order to derive the frequencies or the Raman shifts of the vibration modes from the hyper-Raman scattering spectra, we employed multiple Gaussian fitting to decompose the hyper-Raman spectra measured for different nanomaterials, as shown in Fig. S4.

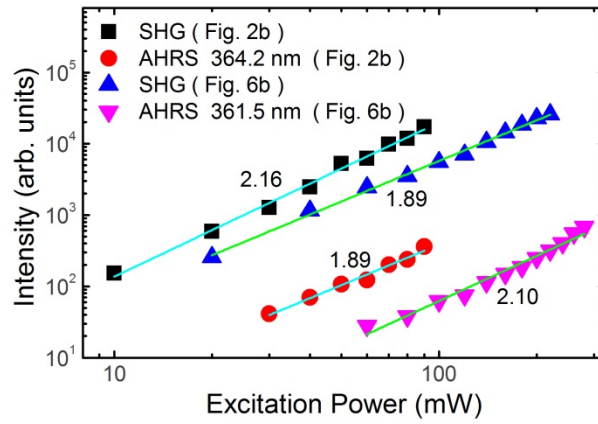




**Fig. S4** Multiple Gaussian fitting of the hyper-Raman spectra measured for different nanomaterials. (a)-(c) Single-layer MoS<sub>2</sub> on the SiO<sub>2</sub>/Si substrate (see Figs. 2b and 2c). (d)-(g) 17-nm-thick MoS<sub>2</sub> on the Au/SiO<sub>2</sub> substrate (see Figs. 3b, 4b, 4c and 5a). (h) and (i): 9-nm-thick MoS<sub>2</sub> on the SiO<sub>2</sub>-SnO<sub>2</sub>/Ag/SiO<sub>2</sub> substrate (see Figs. 5b and 5c). (j) Si QDs self-assembled into “coffee” rings (see Fig. 6a). (k) Cu-doped hollow ZnO NRs (see Fig. 6b). In each case, the circles are the measurement data while the red curve is the fitting result.

#### SI-4 Dependence of the SHG and hyper Raman intensities on the excitation power

In our experiments, we also measured the dependence of the SHG and anti-Stokes hyper-Raman scattering (AHRS) intensities on the excitation power for different nanomaterials and plotted the experimental data in a double logarithmic coordinate, as shown in Fig. S5. The slopes extracted by fitting the experimental data were found to be  $\sim 2.0$ , which is in good agreement with the second-order nature of the nonlinear optical processes.



**Fig. S5** Dependences of the SHG and anti-Stokes hyper-Raman scattering (AHRS) intensities on the excitation power, which are plotted in a double logarithmic coordinate, measured for different nanomaterials. The straight lines with indicated slopes show the fittings of the experimental data which are represented by squares, triangles and circles.

#### SI-5 Frequencies and Raman shifts of the hyper-Raman scattering observed in different nanomaterials

Based on the multiple Gaussian fittings of the hyper-Raman scattering spectra, we have derived the frequencies and Raman shifts of the vibration modes observed for different nanomaterials. The results are summarized in Tables S1 and S2.

**Table S1** Wavelengths of the vibration modes derived by the multiple Gaussian fittings of the hyper-Raman spectra measured for different nanomaterials

Observed-peak positions (nm)						Sample, substrate	Fig.
$\lambda_1$	$\lambda_2$	$\lambda_3$	$\lambda_4$	$\lambda_5$	$\lambda_6$		
364.2	362.5					1L, SiO <sub>2</sub> /Si	2b
364.5	362.9	356.6	355.1	353.9	352.9	1L, SiO <sub>2</sub> /Si	2c
391.5	389.8	388.2	386.9			17 nm, Au/SiO <sub>2</sub>	3b
399.6	403.7					17 nm, Au/SiO <sub>2</sub>	4b
399.4	404.1					17 nm, Au/SiO <sub>2</sub>	4c
400.1	404.6					17 nm, Au/SiO <sub>2</sub>	5a
399.7	403.4					9 nm, SiO <sub>2</sub> -SnO <sub>2</sub> /Ag/SiO <sub>2</sub>	5b
391.8	390.3	389.1	387.7			9 nm, SiO <sub>2</sub> -SnO <sub>2</sub> /Ag/SiO <sub>2</sub>	5c
391.0	389.6	388.2	386.7			Si QDs	6a
363.3	361.5					Cu-doped ZnO NRs	6b

**Table S2** Raman shifts of the vibration modes derived by the multiple Gaussian fittings of the hyper-Raman spectra measured for different nanomaterials

Observed peaks positions (cm <sup>-1</sup> )						Sample, substrate	Fig.
$\omega_1$	$\omega_2$	$\omega_3$	$\omega_4$	$\omega_5$	$\omega_6$		
-793.04	-923.4					1L, SiO <sub>2</sub> /Si	2b
-771.94	-887.6	-1377.5	-1492.0	-1593.9	-1666.8	1L, SiO <sub>2</sub> /Si	2c
-542.1	-654.8	-760.6	-845.8			17 nm, Au/SiO <sub>2</sub>	3b
SHG	250.4					17 nm, Au/SiO <sub>2</sub>	4b
SHG	290.6					17 nm, Au/SiO <sub>2</sub>	4c
SHG	278.0					17 nm, Au/SiO <sub>2</sub>	5a
SHG	225.8					9 nm, SiO <sub>2</sub> -SnO <sub>2</sub> /Ag/SiO <sub>2</sub>	5b
-526.5	-620.0	-703.0	-791.8			9 nm, SiO <sub>2</sub> -SnO <sub>2</sub> /Ag/SiO <sub>2</sub>	5c
-578.1	-666.0	-762.6	-858.5			Si QDs	6a
-858.8	-995.1					Cu-doped ZnO NRs	6b

## References

- S1 P. B. Johnson and R. W. Christy, *Phys. Rev. B*, 1972, **6**, 4370-4379.  
S2 E. D. Palik, *Handbook of Optical Constants of Solids*, Academic, New York, 1985.  
S3 H. Li, Q. Zhang, C. C. R. Yap, B. K. Tay, T. H. T. Edwin, A. Olivier and D. Baillargeat, *Adv. Funct. Mater.*, 2012, **22**, 1385-1390.