

Sc₂₀C₆₀: A Volleyballene

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Section I. One of the tracks of the energy minimization for *Volleyballene* Sc₂₀C₆₀

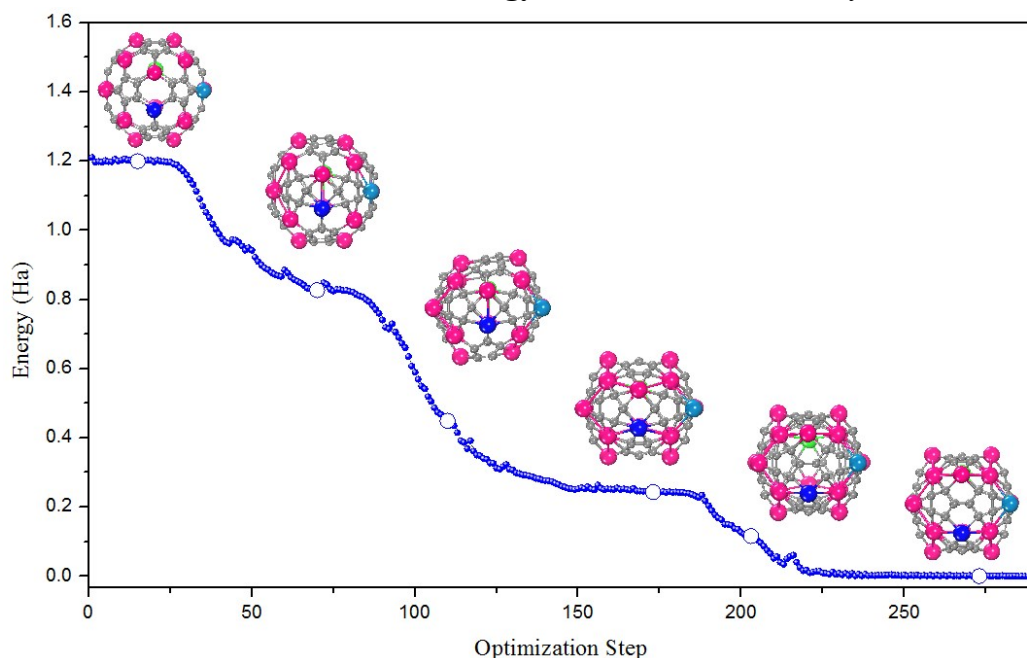


Figure S1. One of the energy minimization tracks for *Volleyballene* Sc₂₀C₆₀ based on DFT calculations at the GGA-BLYP level. The inserted configurations correspond to the highlighted steps. Here, the convergence thresholds were set to 10^{-4} hartree on the total energy, 0.02 hartree/Å for the force, 0.05 Å for the displacement, and 10^{-4} hartree for the energy change. During the course of energy minimization, the configuration, starting from the initial configuration, evolved step-by-step into the *Volleyballene* Sc₂₀C₆₀. The first highlighted structure lies on the first plateau of the energy curve and corresponds closely to the initial structure. It may be viewed as consisting of twelve Sc₅C₅ subunits with each Sc atom joining three Sc₅C₅ subunits together. One C-pentagon is surrounded by five Sc atoms to give the Sc₅C₅ subunit. The second highlighted structure lies on the second step of the energy curve. One Sc₅C₅ subunit has now clearly enlarged, leading to one neighboring C-pentagon being distorted out of its Sc₅C₅ plane. Next, the third highlighted structure corresponds to a configuration in which two Sc₈C₁₀ subunits have formed. The fourth structure lies on the third energy plateau where four Sc₈C₁₀ subunits have formed. The fifth structure corresponds to a configuration in which the fifth Sc₈C₁₀ subunit has formed. Finally, with the sixth configuration, lying on the last step of the energy curve, all six of the Sc₈C₁₀ subunits have formed and eventually evolved into the configuration of *Volleyballene* Sc₂₀C₆₀. This process, with the successive formation of Sc₈C₁₀ subunits, further verifies the stability of *Volleyballene* Sc₂₀C₆₀. The large balls, including the pink, the green, the light blue and the dark blue are Sc atoms, and the small balls (the grey) are C atoms.

Section II. Vibrational frequency analysis

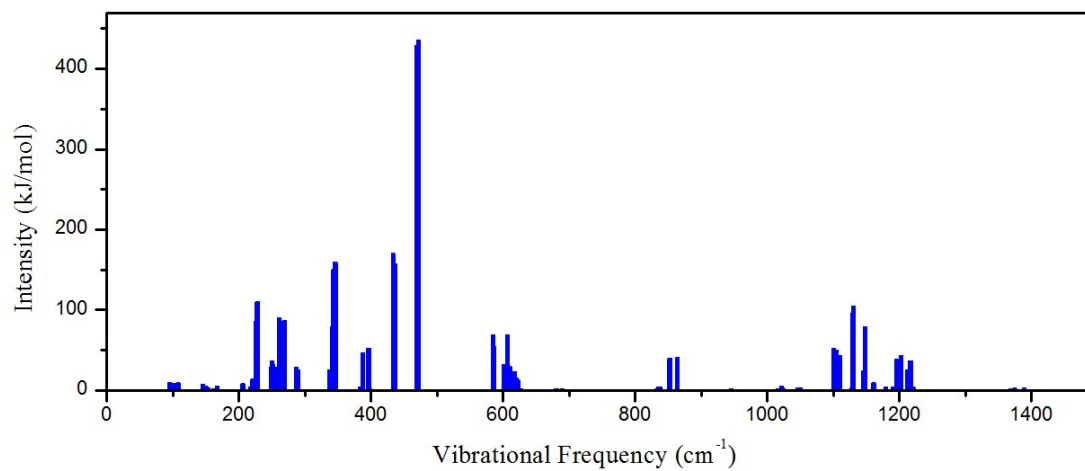


Figure S2. The vibrational frequency analysis for the *Volleyballene* Sc₂₀C₆₀. There were no imaginary frequencies and the two highest intensity frequencies were found to be 468.9 and 472.3 cm⁻¹.

Section III. Raman spectrum data

Table S1. The calculated frequencies for the *Volleyballene* Sc₂₀C₆₀ including Raman activities and intensities at a temperature of 300 K with incident light of wavelength 488.00 nm. Lorentzian smearing of 20.00 cm⁻¹ was used. This Raman spectrum is presented as Figure 5 in the text.

| Frequency (cm ⁻¹) | Raman activity(Å ⁴) | Raman intensity | Frequency (cm ⁻¹) | Raman activity(Å ⁴) | Raman intensity |
|-------------------------------|---------------------------------|-----------------|-------------------------------|---------------------------------|-----------------|
| 80.1 | 41.62 | 171.109 | 528.8 | 0.000 | 0.000 |
| 83.6 | 45.082 | 171.371 | 530.4 | 0.136 | 0.027 |
| 84.9 | 45.972 | 169.894 | 531.2 | 0.000 | 0.000 |
| 94.5 | 0.008 | 0.023 | 571.7 | 130.865 | 23.313 |
| 96.6 | 41.065 | 120.038 | 585.0 | 0.001 | 0.000 |
| 99.6 | 40.451 | 111.904 | 585.8 | 0.005 | 0.001 |
| 100.9 | 0.026 | 0.070 | 585.9 | 0.003 | 0.001 |
| 108.0 | 0.003 | 0.007 | 590.7 | 19.242 | 3.285 |
| 112.4 | 7.859 | 17.513 | 592.7 | 25.766 | 4.380 |
| 113.2 | 0.297 | 0.653 | 600.9 | 0.101 | 0.017 |
| 113.8 | 5.777 | 12.594 | 603.3 | 7.378 | 1.226 |
| 117.6 | 0.001 | 0.001 | 606.7 | 0.398 | 0.066 |
| 120.5 | 0.002 | 0.004 | 607.0 | 0.020 | 0.003 |
| 121.0 | 0.000 | 0.001 | 609.3 | 11.008 | 1.806 |
| 123.1 | 3.313 | 6.286 | 610.3 | 0.003 | 0.000 |
| 123.3 | 0.017 | 0.033 | 612.2 | 2.479 | 0.404 |
| 124.1 | 0.000 | 0.000 | 613.0 | 0.002 | 0.000 |
| 133.6 | 0.217 | 0.357 | 613.9 | 0.002 | 0.000 |
| 144.2 | 0.221 | 0.319 | 615.9 | 11.411 | 1.846 |
| 145.3 | 0.002 | 0.003 | 617.6 | 0.144 | 0.023 |
| 146.4 | 2.215 | 3.110 | 617.8 | 2.295 | 0.370 |
| 146.9 | 0.001 | 0.001 | 620.4 | 0.028 | 0.005 |
| 150.0 | 0.002 | 0.003 | 621.7 | 10.29 | 1.645 |
| 151.6 | 0.596 | 0.788 | 622.5 | 0.006 | 0.001 |
| 153.4 | 0.000 | 0.001 | 623.2 | 0.120 | 0.019 |
| 158.4 | 0.001 | 0.001 | 627.3 | 1.356 | 0.214 |
| 161.0 | 0.002 | 0.002 | 627.8 | 7.402 | 1.168 |
| 165.5 | 59.328 | 67.589 | 680.0 | 0.158 | 0.023 |
| 167.4 | 0.003 | 0.003 | 682.0 | 0.146 | 0.021 |
| 171.0 | 33.87 | 36.521 | 688.3 | 0.007 | 0.001 |
| 171.0 | 6.724 | 7.250 | 688.6 | 0.007 | 0.001 |
| 172.9 | 21.15 | 22.387 | 688.7 | 0.006 | 0.001 |
| 179.9 | 0.002 | 0.002 | 689.5 | 0.003 | 0.000 |
| 189.8 | 127.314 | 115.393 | 820.8 | 0.000 | 0.000 |
| 195.5 | 2.997 | 2.588 | 821.5 | 0.296 | 0.033 |

| | | | | | |
|-------|---------|---------|--------|--------|-------|
| 197.6 | 1.684 | 1.428 | 824.6 | 0.249 | 0.028 |
| 198.2 | 3.942 | 3.327 | 825.9 | 0.001 | 0.000 |
| 200.8 | 5.576 | 4.607 | 826.4 | 0.496 | 0.055 |
| 203.7 | 0.085 | 0.068 | 828.5 | 0.000 | 0.000 |
| 204.5 | 8.805 | 7.062 | 831.9 | 0.004 | 0.000 |
| 205.2 | 24.684 | 19.687 | 832.8 | 6.942 | 0.768 |
| 206.1 | 0.056 | 0.045 | 835.1 | 0.003 | 0.000 |
| 217.6 | 0.001 | 0.000 | 836.4 | 6.402 | 0.704 |
| 218.4 | 0.000 | 0.000 | 837.7 | 0.004 | 0.000 |
| 220.4 | 0.001 | 0.000 | 839.0 | 6.153 | 0.674 |
| 222.7 | 3.412 | 2.384 | 850.9 | 7.847 | 0.845 |
| 223.7 | 6.698 | 4.647 | 852.0 | 0.022 | 0.002 |
| 226.4 | 0.004 | 0.003 | 852.4 | 8.420 | 0.904 |
| 226.6 | 0.001 | 0.001 | 853.4 | 0.009 | 0.001 |
| 227.8 | 0.000 | 0.000 | 863.3 | 8.171 | 0.864 |
| 230.4 | 7.464 | 4.940 | 864.0 | 0.148 | 0.016 |
| 237.9 | 1.052 | 0.662 | 942.9 | 9.704 | 0.920 |
| 239.7 | 1.103 | 0.686 | 944.5 | 0.001 | 0.000 |
| 243.6 | 5.337 | 3.234 | 946.4 | 0.009 | 0.001 |
| 245.0 | 2.161 | 1.298 | 947.3 | 18.537 | 1.746 |
| 248.7 | 0.133 | 0.078 | 952.1 | 3.014 | 0.282 |
| 248.9 | 2.333 | 1.367 | 953.3 | 14.158 | 1.323 |
| 250.2 | 0.002 | 0.001 | 1015.8 | 0.664 | 0.057 |
| 251.6 | 0.002 | 0.001 | 1016.2 | 0.018 | 0.002 |
| 256.2 | 0.000 | 0.000 | 1018.8 | 0.021 | 0.002 |
| 259.6 | 0.001 | 0.001 | 1019.7 | 0.680 | 0.058 |
| 261.2 | 0.000 | 0.000 | 1020.8 | 24.261 | 2.083 |
| 263.4 | 0.001 | 0.000 | 1021.6 | 0.130 | 0.011 |
| 268.4 | 0.472 | 0.246 | 1024.0 | 0.058 | 0.005 |
| 268.6 | 0.029 | 0.015 | 1024.6 | 22.333 | 1.908 |
| 269.7 | 3.147 | 1.627 | 1045.6 | 0.889 | 0.074 |
| 269.9 | 20.344 | 10.507 | 1046.0 | 0.001 | 0.000 |
| 273.7 | 347.859 | 175.825 | 1050.0 | 0.001 | 0.000 |
| 278.0 | 0.003 | 0.002 | 1050.4 | 15.588 | 1.291 |
| 280.1 | 0.001 | 0.001 | 1099.7 | 2.496 | 0.195 |
| 283.2 | 7.337 | 3.520 | 1100.5 | 0.002 | 0.000 |
| 286.6 | 0.002 | 0.001 | 1103.6 | 4.099 | 0.319 |
| 286.7 | 1.290 | 0.607 | 1104.4 | 0.007 | 0.001 |
| 287.5 | 0.018 | 0.008 | 1108.5 | 1.818 | 0.141 |
| 288.1 | 10.643 | 4.974 | 1110.1 | 0.431 | 0.033 |
| 288.7 | 1.999 | 0.931 | 1127.7 | 5.594 | 0.424 |
| 289.6 | 0.004 | 0.002 | 1128.8 | 3.490 | 0.264 |

| | | | | | |
|-------|--------|-------|--------|---------|--------|
| 293.0 | 8.617 | 3.925 | 1129.1 | 0.155 | 0.012 |
| 313.3 | 9.647 | 3.973 | 1130.2 | 0.023 | 0.002 |
| 314.6 | 8.298 | 3.397 | 1145.5 | 3.689 | 0.274 |
| 318.4 | 9.599 | 3.860 | 1148.2 | 1.382 | 0.102 |
| 324.8 | 5.408 | 2.111 | 1160.4 | 6.488 | 0.474 |
| 337.3 | 0.000 | 0.000 | 1160.5 | 21.428 | 1.566 |
| 339.6 | 0.000 | 0.000 | 1161.3 | 23.714 | 1.732 |
| 340.9 | 0.000 | 0.000 | 1161.4 | 0.474 | 0.035 |
| 343.2 | 0.003 | 0.001 | 1170.4 | 15.832 | 1.145 |
| 344.6 | 0.001 | 0.000 | 1170.8 | 13.742 | 0.993 |
| 346.0 | 0.000 | 0.000 | 1179.5 | 0.011 | 0.001 |
| 358.1 | 5.271 | 1.784 | 1181.5 | 35.34 | 2.525 |
| 359.7 | 5.682 | 1.911 | 1185.2 | 0.002 | 0.000 |
| 377.4 | 0.183 | 0.057 | 1186.1 | 14.15 | 1.006 |
| 381.0 | 0.000 | 0.000 | 1191.0 | 0.002 | 0.000 |
| 383.1 | 0.000 | 0.000 | 1193.2 | 124.342 | 8.776 |
| 384.4 | 0.211 | 0.065 | 1194.2 | 44.016 | 3.103 |
| 384.6 | 0.312 | 0.095 | 1196.2 | 0.035 | 0.002 |
| 387.5 | 0.003 | 0.001 | 1198.3 | 204.506 | 14.355 |
| 388.0 | 0.000 | 0.000 | 1201.4 | 0.006 | 0.000 |
| 395.8 | 0.000 | 0.000 | 1203.1 | 0.004 | 0.000 |
| 397.5 | 0.002 | 0.001 | 1208.1 | 40.375 | 2.805 |
| 398.2 | 0.116 | 0.034 | 1209.0 | 9.865 | 0.685 |
| 399.1 | 0.049 | 0.014 | 1212.5 | 0.004 | 0.000 |
| 401.6 | 0.063 | 0.018 | 1217.0 | 1.764 | 0.121 |
| 433.3 | 0.003 | 0.001 | 1217.6 | 488.91 | 33.631 |
| 435.0 | 0.973 | 0.250 | 1219.6 | 3.245 | 0.223 |
| 435.7 | 0.103 | 0.026 | 1221.3 | 0.062 | 0.004 |
| 435.8 | 0.051 | 0.013 | 1242.6 | 0.005 | 0.000 |
| 436.9 | 0.000 | 0.000 | 1243.3 | 0.746 | 0.050 |
| 437.5 | 2.533 | 0.646 | 1245.2 | 0.575 | 0.038 |
| 445.0 | 24.248 | 6.040 | 1245.7 | 0.034 | 0.002 |
| 447.3 | 28.573 | 7.067 | 1257.3 | 3.006 | 0.198 |
| 451.1 | 27.687 | 6.769 | 1258.8 | 2.963 | 0.195 |
| 468.9 | 0.000 | 0.000 | 1368.4 | 245.011 | 14.511 |
| 471.4 | 0.001 | 0.000 | 1369.2 | 282.612 | 16.725 |
| 472.3 | 0.001 | 0.000 | 1375.1 | 108.078 | 6.361 |
| 524.3 | 0.000 | 0.000 | 1375.4 | 335.574 | 19.743 |
| 525.8 | 0.032 | 0.006 | 1389.3 | 30.951 | 1.797 |
| 527.8 | 0.025 | 0.005 | 1389.5 | 406.381 | 23.595 |

Section IV. Relative stability

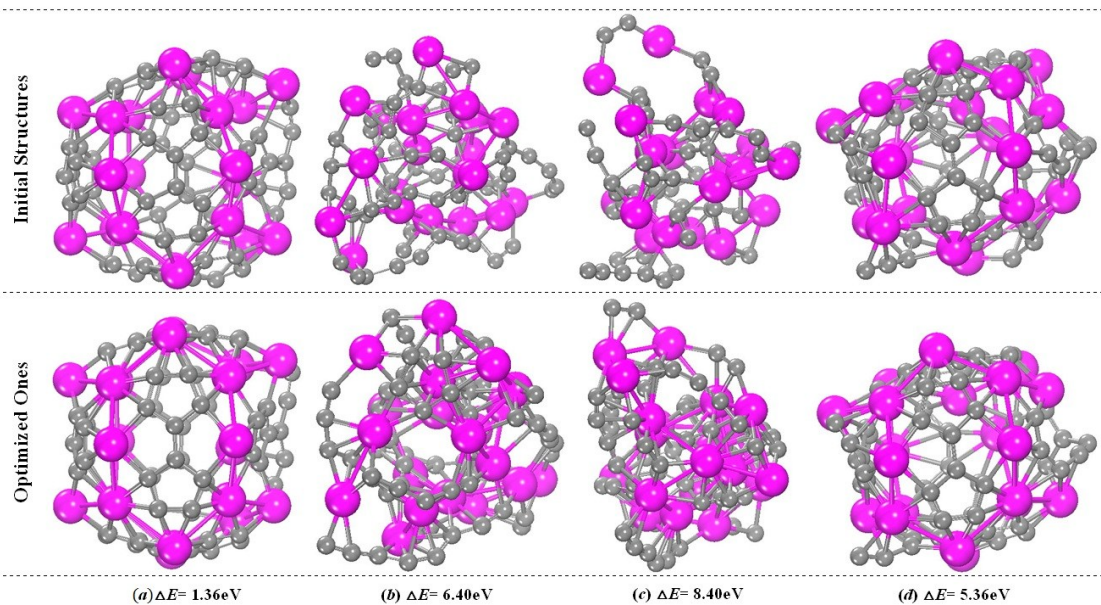


Figure S3. The initial and optimized configurations of $\text{Sc}_{20}\text{C}_{60}$ clusters selected randomly from the NVE dynamic simulations with temperatures of 4000 and 5000 K. (a), (b), (c), and (d) correspond to the 2001th step of NVE-4000K, the 463th, 1010th, and 1038th steps of NVE-5000K, respectively. Beneath each isomer is listed the relative energy (ΔE) with respect to the *Volleyballene*.

Section V. *Ab initio* molecular dynamics

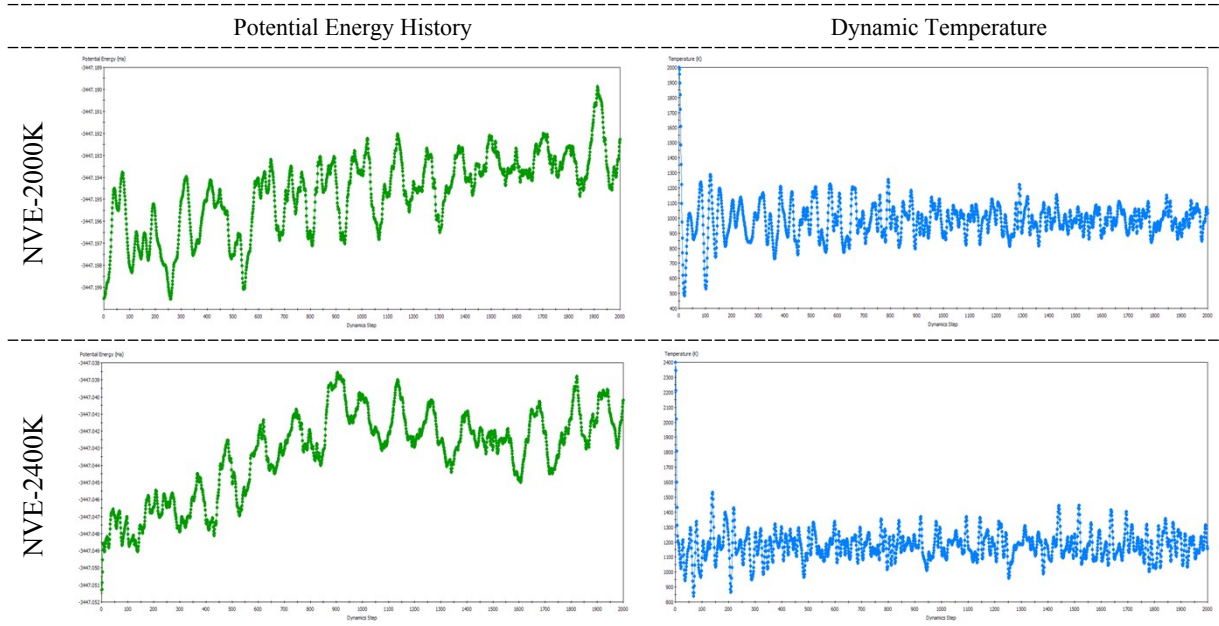


Figure S4. Results of *ab initio* molecular dynamics simulations with NVE ensembles at initial temperatures of 2000 K and 2400 K, including the dynamic potential energy history and the temperature history vs the dynamic step for the $\text{Sc}_{20}\text{C}_{60}$ *Volleyballene*. The corresponding animations are attached.

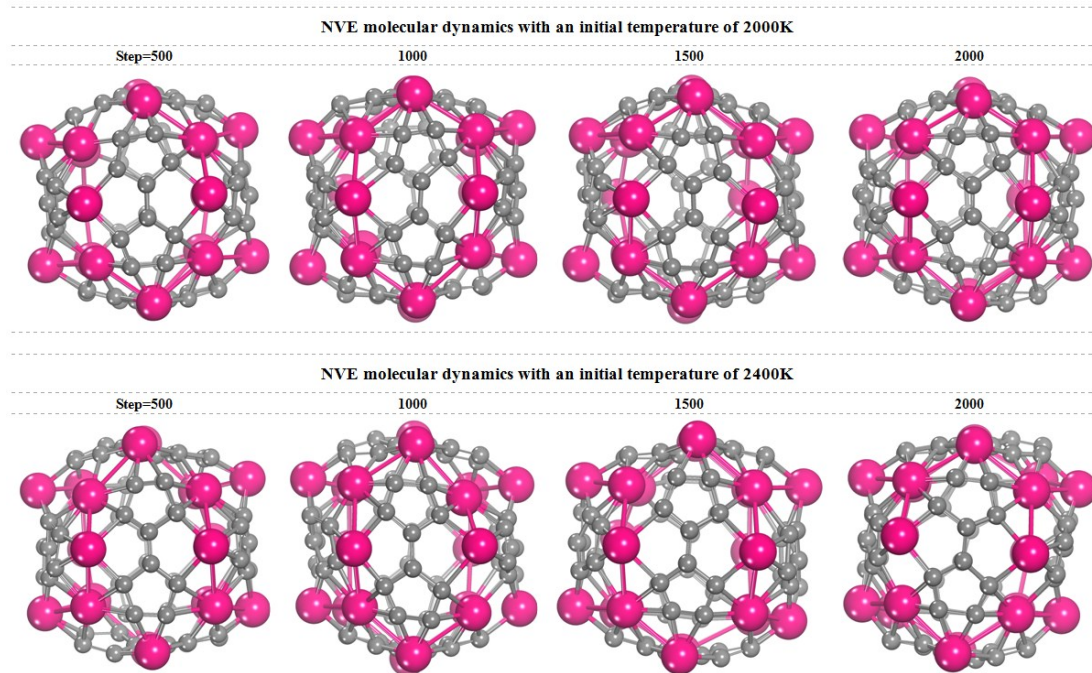


Figure S5. Selected typical frames at the 500th, 1000th, 1500th, and 2000th step from the NVE molecular dynamics simulations with initial temperatures of 2000 K and 2400 K.

Section VI. Comparison of calculated results based on three levels of optimization

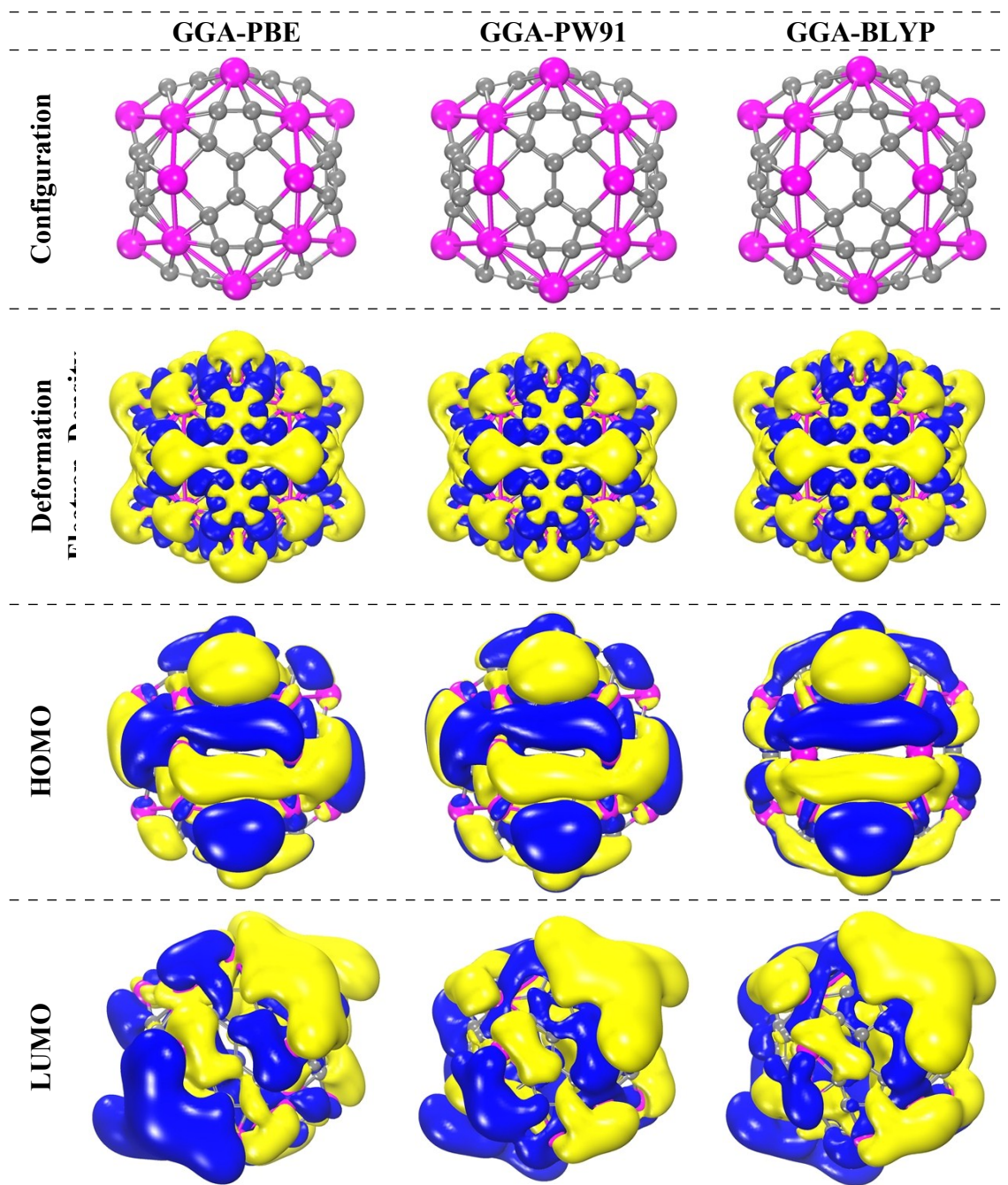


Figure S6. Calculated results for the configuration, deformation electron density, HOMO and LUMO orbitals based on the GGA-PBE, GGA-PW91, and GGA-BLYP levels of optimization. The isosurfaces for the deformation electron density are set to be $0.03 \text{ e}/\text{\AA}^3$, for the others they are taken to be $0.005 \text{ e}/\text{\AA}^3$. The three configurations obtained after the energy minimizations at the three different levels listed above are quite similar. They also have similar bonding characters. The three HOMO or LUMO orbitals are also similar. In particular, the two HOMO orbitals obtained at the GGA-PBE and GGA-PW91 levels have nearly identical characteristics and the two LUMO orbitals obtained at the GGA-PW91 and GGA-BLYP levels have very similar characteristics.

Section VII. Bond lengths and bond angles

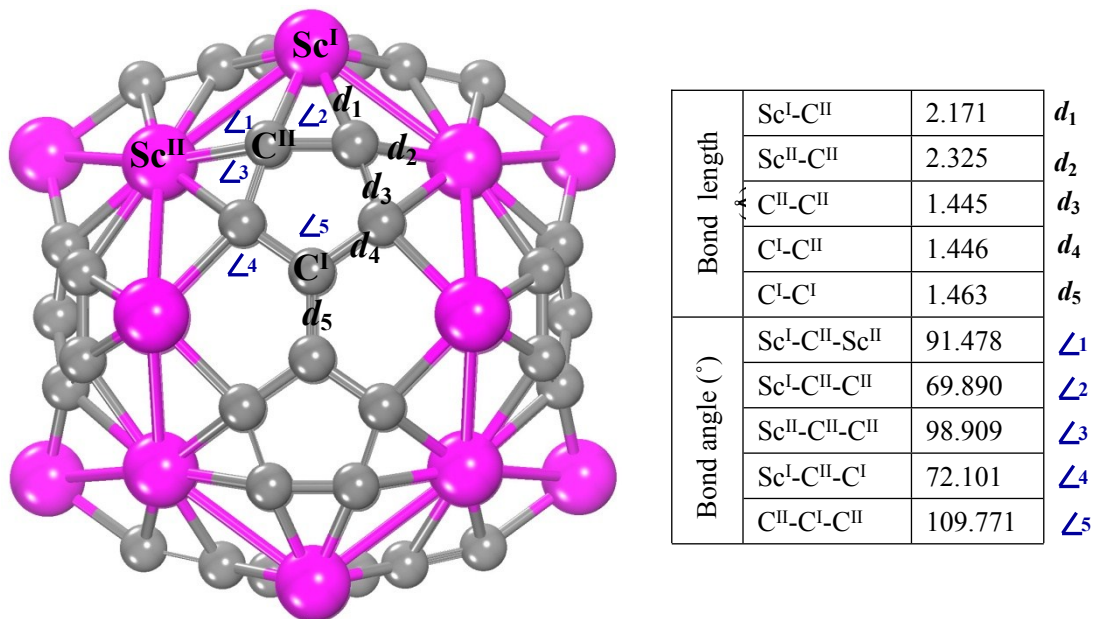


Figure S7. Some typical bond lengths and bond angles of Sc^I/Sc^{II} and C^I/C^{II} for the Sc₂₀C₆₀ Volleballene.

Section VIII. Natural bond orbitals

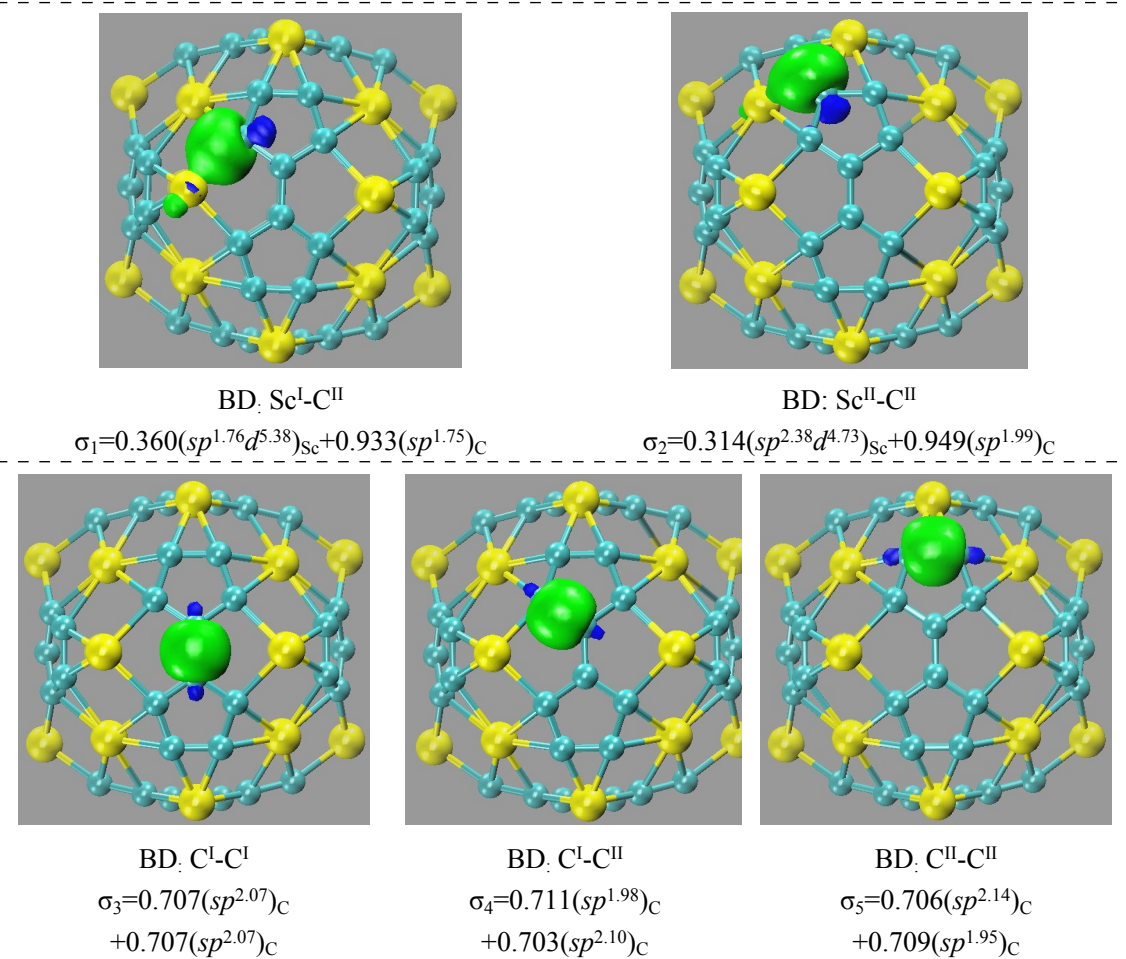


Figure S8. Some typical natural bond orbitals for the $Sc_{20}C_{60}$ Volleyballene. Below each configurations, the first lines list the bond types (BD for 2-center bond) and the next lines summarize the natural atomic hybrids of this natural bond orbital. The results indicate that Sc-C bond are mainly composed $sp-d$ of Sc and sp hybrid of C. For C^I and C^{II}, both are characterized by sp^2 hybridization.