

Supplementary Information for

**Single-molecule imaging reveals topological isomer-dependent diffusion by 4-armed star and dicyclic 8-shaped polymers**

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**Supporting Text**

**Figure S1**

**Movie S1.avi:** An example of fluorescence images of **1** in the linear poly(THF) matrix

**Movie S2.avi:** An example of fluorescence images of **2a+2b** in the linear poly(THF) matrix

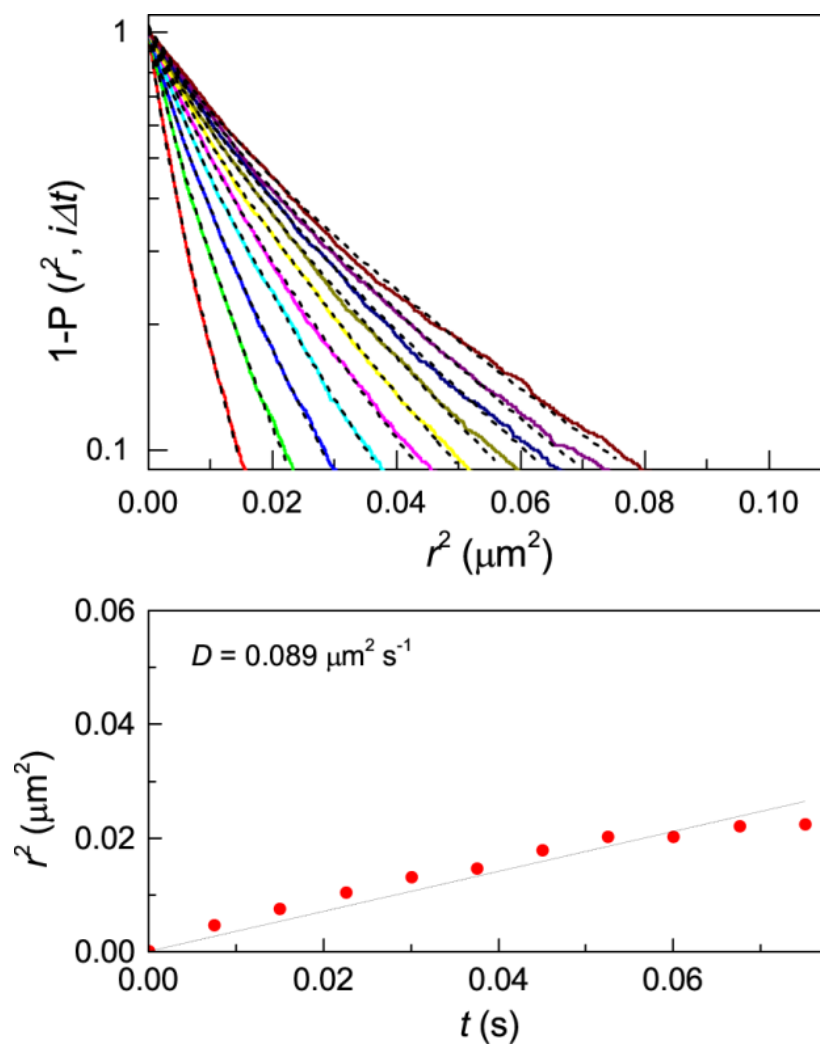
### Calculation of gyration radius

Gyration radius ( $R_G$ ) of a flexible polymer chain which has  $N$  Kuhn monomer and Kuhn length of  $b$  can be calculated by equation S12 and S13.<sup>1</sup>

$$\langle R_G^2 \rangle = \left( \frac{N}{f} \right) \frac{b^2}{6} (3 - 2/f) \quad (f - \text{arm star polymer}) \quad (\text{S1})$$

$$\langle R_G^2 \rangle = \frac{Nb^2}{12} \quad (\text{cyclic polymer}) \quad (\text{S2})$$

Assuming the physical properties of poly(THF) are similar to those of poly(ethylene oxide),  $b$  of poly(THF) is estimated to be  $b = 1.1$  nm. The Kuhn monomer numbers are 76, 58 (per ring), and 23 for **1**, **2a+2b**, and linear poly(THF), respectively. Therefore, the gyration radii of **1**, **2a+2b**, and linear poly(THF) are calculated to be 3.1 nm, 2.4 nm (per ring), and 2.2 nm, respectively.



**Figure S1.** (top) Experimentally obtained cumulative distribution functions (CDFs,  $i\Delta t = 7.5 - 75$  ms) in the form of  $1-P$  (solid lines) for **2a+2b**. Dashed lines show fittings with Eq. 2. (bottom) CDF coefficients at different time lags determined by the single Gaussian distribution model using Eq. 2. The solid line shows a linear fitting.

### Supporting references

- (1) Rubinstein, M.; Colby, R. H., *Polymer Physics*. Oxford University Press: 2003.