Supplementary information

Ten-fold Coordinated Polymorph and Metallization of TiO₂ under High Pressure

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Computational details

Our structural prediction approach is based on a global minimization of free energy surfaces merging ab initio total-energy calculations through CALYPSO (Crystal structure AnaLYsis by Particle Swarm Optimization) methodology as implemented in its same-name CALYPSO code.^{1,2} The structures of TiO₂ were searched with simulation cell sizes of 1-4 formula units (f.u.) at 0~800 GPa, respectively. In the first step, random structures with certain symmetry are constructed in which the atomic coordinates are generated by the crystallographic symmetry operations. Local optimizations using VASP code,³ were done with the conjugate gradients method and were stopped when the enthalpy changes became smaller than 1×10^{-5} eV per cell. After processing the first generation structures, 60% of them with lower enthalpies are selected to produce the next generation structures by PSO. 40% of the structures in the new generation are randomly generated. A structure fingerprinting technique of bond characterization matrix is applied to the generated structures, so that identical structures are strictly forbidden. These procedures significantly enhance the diversity of the structures, which is crucial for the efficiency of the global search of structures. For most of the cases, the structure searching simulation for each calculation was stopped after we generated 1000 ~ 1200 structures (e.g., about 20 ~ 30 generations).

To further analyze the structures with higher accuracy, we select a number of structures with lower enthalpies and perform structural optimization using density functional theory within the generalized gradient approximation⁴ as implemented in the VASP code. The cut-off energy for the expansion of wavefunctions into plane waves is set to 1000 eV in all calculations, and the Monkhorst–Pack *k*-mesh with a maximum spacing of 0.03 Å⁻¹ was individually adjusted in reciprocal space with respect to the size of each computational cell. This usually gives total energy well converged within ~ 1 meV/atom. The electron-ion interaction was described by means of projector augmented wave with $3d^24s^23p^63s^2$ and $2s^22p^4$ electrons as valence for Ti and O atoms, respectively.

The electron-phonon coupling calculations are carried out by linear response

density functional theory as implemented in the QUANTUM ESPRESSO package.⁵The norm-conserving pseudopotentials for Ti and O are adopted. The kinetic energy cutoffs of 80 Ry are chosen for all phases. And 24 x 24 x 8 *k* meshes and 6 x 6 x 2 q meshes in the Brillouin zone are used for TiO₂ in CaC₂-type.

In order to test the validity of the PAW potentials for Ti and O provided by the VASP PAW library, we calculated the equation of states (EOS) for TiO₂ in CaC₂-type structure. The calculations are performed by use of PAW method as implemented in VASP code as well as a full-potential linearized augmented plane wave (FP-LAPW) method as implemented in the ELK code.⁶ Thus, our adopted pseudopotentials are feasible under high pressure.



Figure S1. Comparing the Birch-Murnaghan equation of state by PAW potentials and ELK methods for Fe_2P -type structure (top) and CaC_2 -type structure (bottom). These results indicate that the PAW potentials are applicable to TiO_2 under high pressure.



Figure S2. Calculated phonon dispersions (left panel) and projected phonon density of states (right panel) at 700 GPa. The motions of Ti atom dominate mainly the low frequency regimes, while O atoms contribute to the high frequency regimes,



Figure S3 (a) and (b) Electron localization function (ELF) plots for CaC_2 -type and Fe₂P-type structures at 700 GPa, respectively. (c) difference charge density plot of

 CaC_2 -type structure at 700 GPa. The difference charge density plot is further supported the charge transfer from Ti atoms to the O atoms.



Figure S4 (color online) (a) and (b) PV curve and U curve for CaC_2 -type and Fe₂P-type of TiO₂ structures, respectively.

Supplementary Tables

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Fe ₂ P-type	TiO_2 at the te	emperature $T =$	0 K and se	elected pre	ssures.		

Table	S1.	Optumized	cell	parameters	а,	b,	c (Å)	and	volume	of	Cotunnite	and
Fe ₂ P-t	ype]	ΓiO_2 at the te	mper	rature $T = 0$	K a	nd	selecte	ed pre	essures.			

Phase	Ref.	Pressure	Latti	Volume(Å ³)		
		(GPa)	а	b	С	
Cotunnite	This work(GGA)	100	4.923	2.856	5.795	40.76
<i>Pnma</i> (62)	This work(GGA)	60	5.049	2.938	5.955	44.18
	Expt.[7]	61	5.163	2.989	5.966	46.03
	Other calc.[8]	60	5.028	2.933	5.896	44.28
Fe ₂ P-type	This work(GGA)	160	4.91		2.750	19.12
P-62m (189)	Expt.[9]	160	4.863		2.744	
	This work(GGA)	0	5.319		3.126	25.53
	Other calc.[10]	0	5.330		3.127	25.53

Table S2. Calculated structural parameters of the CaC_2 -type, Fe₂P-type and CotunniteTiO₂ at selected pressures.

Phase	Pressure	Lattice parameters	Atomic coordinates			
	(GPa)	(Å,)	(fractional)			
CaC ₂ -type	700	a = b = 2.1985	Ti(2b) 0.000 0.000			0.500
I4/mmm		<i>c</i> = 5.3617	O(4e)	0.000	0.000	0.837
		$\alpha = \beta = \gamma = 90.000$				
Fe ₂ P-type	200	a = b = 4.8061	Ti(2d)	0.333	0.667	0.500
P-62m		<i>c</i> = 2.6976	Ti(1a)	0.000	0.000	0.000
		$\alpha = \beta = 90.000$	O(3g)	0.000	0.259	0.500
		$\gamma = 120.000$	O(3f)	0.406	0.406	0.000
Cotunnite	100	<i>a</i> = 4.9233	Ti(4c)	-0.758	0.250	-0.625
Pnma		<i>b</i> = 2.8563	O(4c)	-0.643	0.250	-0.931
		<i>c</i> = 5.7946	O(4c)	-0.471	0.750	-0.665
		$\alpha = \beta = \gamma = 90.000$				

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