

## **Theoretical Perspective of the Lone Pair Activity influencing on Band gap and SHG response in Lead borates**

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### **Electronic Supplementary Information:**

**The convergence tolerance of  $\text{Ba}_2[\text{B}_5\text{O}_9(\text{OH})]\cdot\text{H}_2\text{O}$  and  $\text{Ba}_3(\text{B}_3\text{O}_6)_2$ .**

**Figure S1.** The calculated band structure along the high symmetry lines in the Brillouin zone.

**Figure S2.** The convergence tolerance of  $\text{Ba}_2[\text{B}_5\text{O}_9(\text{OH})]\cdot\text{H}_2\text{O}$  and  $\text{Ba}_3(\text{B}_3\text{O}_6)_2$ .

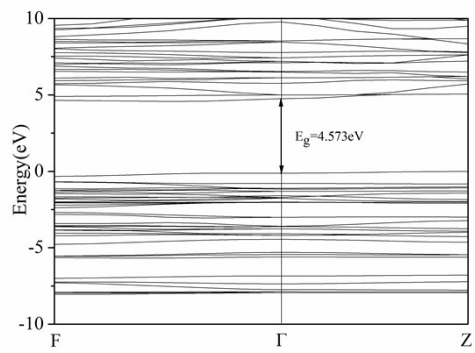
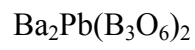
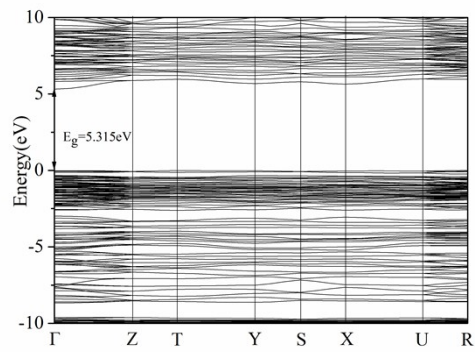
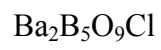
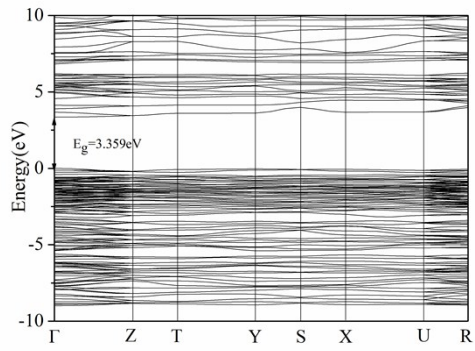
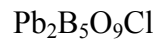
**Table S1.** The experimental lattice parameters of  $\text{Pb}_2\text{B}_5\text{O}_9\text{Cl}$ ,  $\text{Ba}_2\text{Pb}(\text{B}_3\text{O}_6)_2$ , and  $\text{BaPb}[\text{B}_5\text{O}_9(\text{OH})]\cdot\text{H}_2\text{O}$

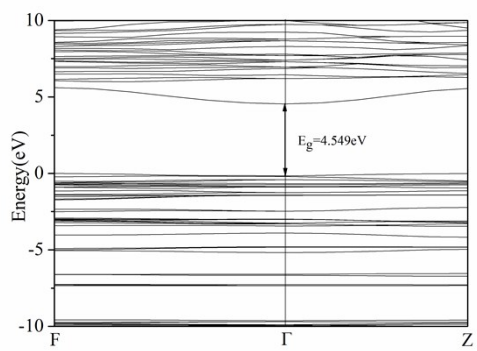
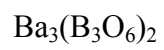
**Table S2.** The optimized parameter of  $\text{BaPb}[\text{B}_5\text{O}_9(\text{OH})]\cdot\text{H}_2\text{O}$  and  $\text{Ba}_2[\text{B}_5\text{O}_9(\text{OH})]\cdot\text{H}_2\text{O}$

**The convergence tolerance of  $\text{Ba}_2[\text{B}_5\text{O}_9(\text{OH})]\cdot\text{H}_2\text{O}$  and  $\text{Ba}_3(\text{B}_3\text{O}_6)_2$ .**

The Energy and Max. displacement of  $\text{Ba}_2[\text{B}_5\text{O}_9(\text{OH})]\cdot\text{H}_2\text{O}$  are  $5.0\times 10^{-6}$  eV/atom,  $5.0\times 10^{-4}$  Å. And the Energy and Max. displacement of  $\text{Ba}_3(\text{B}_3\text{O}_6)_2$  are  $1.0\times 10^{-5}$  eV/atom, 0.001 Å.

**Figure S1** The calculated band structure along the high symmetry lines in the Brillouin zone





**Table S1** The experimental lattice parameters of  $\text{Pb}_2\text{B}_5\text{O}_9\text{Cl}$ ,  $\text{Ba}_2\text{Pb}(\text{B}_3\text{O}_6)_2$ , and  $\text{BaPb}[\text{B}_5\text{O}_9(\text{OH})]\cdot\text{H}_2\text{O}$ .

| Compound                                                                                | a(Å)        | b(Å)        | c(Å)       | $\alpha(^{\circ})$ | $\beta(^{\circ})$ | $\gamma(^{\circ})$ |
|-----------------------------------------------------------------------------------------|-------------|-------------|------------|--------------------|-------------------|--------------------|
| <b><math>\text{Pb}_2\text{B}_5\text{O}_9\text{Cl}</math></b>                            | 11.3543(11) | 11.3629(11) | 6.5535(7)  | 90                 | 90                | 90                 |
| <b><math>\text{Ba}_2\text{Pb}(\text{B}_3\text{O}_6)_2</math></b>                        | 7.2056(8)   | 7.2056(8)   | 18.752(6)  | 90                 | 90                | 120                |
| <b><math>\text{BaPb}[\text{B}_5\text{O}_9(\text{OH})]\cdot\text{H}_2\text{O}</math></b> | 11.3194(6)  | 6.6265(3)   | 12.9256(8) | 90                 | 115.065           | 90                 |
| <b><math>\text{Ba}_2\text{B}_5\text{O}_9\text{Cl}</math></b>                            | 11.576(2)   | 11.619(9)   | 6.6874(13) | 90                 | 90                | 90                 |

**Table S2** the optimized parameter of compound  $\text{BaPb}[\text{B}_5\text{O}_9(\text{OH})]\cdot\text{H}_2\text{O}$ ,  $\text{Ba}_2[\text{B}_5\text{O}_9(\text{OH})]\cdot\text{H}_2\text{O}$ , and  $\text{Ba}_3(\text{B}_3\text{O}_6)_2$ .

| compound                                                                                | a(Å)    | b(Å)    | c(Å)    |
|-----------------------------------------------------------------------------------------|---------|---------|---------|
| <b><math>\text{BaPb}[\text{B}_5\text{O}_9(\text{OH})]\cdot\text{H}_2\text{O}</math></b> | 11.3194 | 6.6265  | 12.9256 |
| <b><math>\text{Ba}_2[\text{B}_5\text{O}_9(\text{OH})]\cdot\text{H}_2\text{O}</math></b> | 11.4074 | 6.7225  | 13.3641 |
| <b><math>\text{Ba}_3(\text{B}_3\text{O}_6)_2</math></b>                                 | 7.27809 | 7.27809 | 20.1645 |