

## Supplementary Information

### Structure-property relationships of aromatic polyamides and polythioamides: comparative consideration with those of analogous polyesters, polythioesters and polydithioesters

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**Appendix A** Statistical Weight Matrices  $U_j$ 's ( $j$ , bond number) of PA2T and PTA2T

For the bond numbers, see Fig. 2. Here, the symbol  $\otimes$  stands for direct product.

$$U_1 = C_1 \otimes R_3 \quad (\text{A1})$$

$$U_2 = C_3 \otimes R_1 \quad (\text{A2})$$

$$U_3 = C_1 \otimes R_\gamma \quad (\text{A3})$$

$$U_4 = C_6 \otimes R_1 \quad (\text{A4})$$

$$U_5 = C_1 \otimes R_3 \quad (\text{A5})$$

$$U_6 = I_3 \otimes R_3 \quad (\text{A6})$$

$$U_7 = U_f = \begin{bmatrix} \sigma_{ttt} & \sigma_{ttg+} & \sigma_{tg-} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \sigma_{tg+t} & \sigma_{tg+g+} & \sigma_{tg+g-} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \sigma_{tg-t} & \sigma_{tg-g+} & \sigma_{tg-g-} \\ \sigma_{g+tt} & \sigma_{g+tg+} & \sigma_{g+tg-} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \sigma_{g+g+t} & \sigma_{g+g+g+} & \sigma_{g+g+g-} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \sigma_{g+g-t} & \sigma_{g+g-g+} & \sigma_{g+g-g-} \\ \sigma_{g-tt} & \sigma_{g-tg+} & \sigma_{g-tg-} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \sigma_{g-g+t} & \sigma_{g-g+g+} & \sigma_{g-g+g-} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \sigma_{g-g-t} & \sigma_{g-g-g+} & \sigma_{g-g-g-} \end{bmatrix} \quad (\text{A7})$$

$$U_a = C_3 \otimes I_3 \otimes R_1 \quad (\text{A8})$$

$$U_b = C_3 \otimes S_1 \otimes R_\gamma \quad (\text{A9})$$

$$U_c = C_1 \otimes I_6 \otimes R_1 \quad (\text{A10})$$

$$U_d = C_6 \otimes S_1 \otimes R_3 \quad (\text{A11})$$

$$U_e = C_1 \otimes I_3 \otimes R_3 \quad (\text{A12})$$

and

$$U_n = C_3 \otimes I_3 \otimes R_1 \quad (\text{A13})$$

where

$$C_1 = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \quad (\text{A14})$$

$$C_3 = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \quad (\text{A15})$$

$$C_6 = \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} \quad (\text{A16})$$

$$R_1 = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix} \quad (\text{A17})$$

$$R_3 = \begin{bmatrix} 1 & 1 & 1 \end{bmatrix} \quad (\text{A18})$$

$$R_\gamma = \begin{bmatrix} \gamma_{t-t} & \gamma_{(t-c)^+} & \gamma_{(t-c)^-} & \gamma_{(c-t)^+} & \gamma_{(c-t)^-} & \gamma_{c-c} \end{bmatrix} \quad (\text{A19})$$

$$S_1 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \quad (\text{A20})$$

and  $I_3$  and  $I_6$  are the identity matrices of sizes 3 and 6 respectively, with  $\gamma_\xi = \exp(-\Delta G_\xi/RT)$  ( $\xi$ : orientation around bond 3 or b) and  $\sigma_k = \exp(-\Delta G_k/RT)$  ( $k$ : conformations in bonds 5, 6, and 7 or bonds d, e, and f).

## Appendix B Statistical Weight Matrices $U_j$ 's ( $j$ , bond number) of PA3T and PTA3T

The  $U_1$  to  $U_6$  matrices are the same as those of PA2T and PTA2T.

$$U_7 = I_3 \otimes I_3 \otimes R_3 \quad (\text{A21})$$

$$U_a = C_3 \otimes I_3 \otimes I_3 \otimes R_1 \quad (\text{A22})$$

$$U_b = C_3 \otimes I_3 \otimes S_1 \otimes R_\gamma \quad (\text{A23})$$

$$U_c = C_1 \otimes S_1 \otimes I_6 \otimes R_1 \quad (\text{A24})$$

$$U_d = C_1 \otimes I_6 \otimes S_1 \otimes R_3 \quad (\text{A25})$$

$$U_e = C_6 \otimes S_1 \otimes I_3 \otimes R_3 \quad (\text{A26})$$

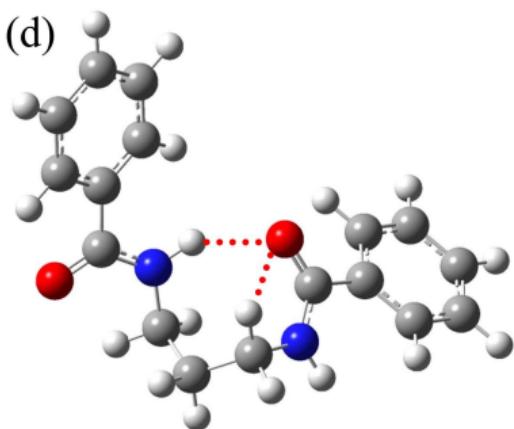
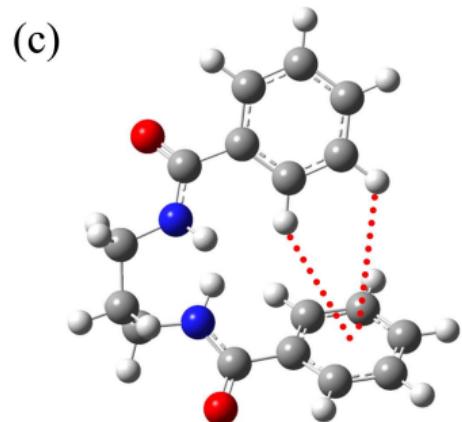
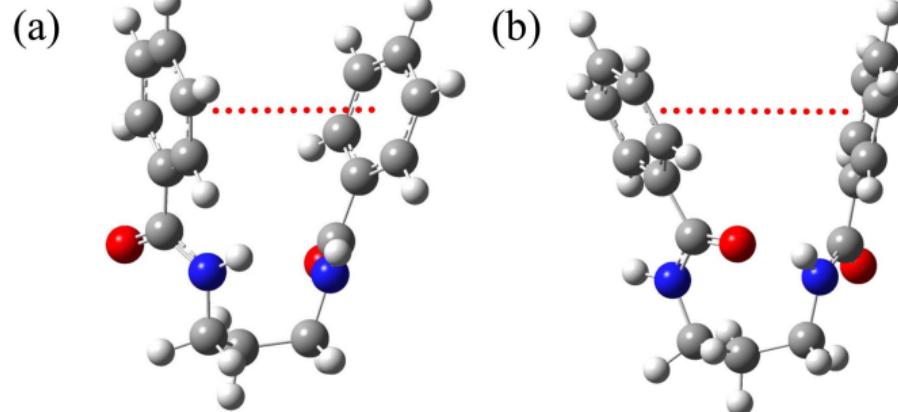
$$U_f = C_1 \otimes I_3 \otimes I_3 \otimes R_3 \quad (\text{A27})$$

and

$$U_n = C_3 \otimes I_3 \otimes I_3 \otimes R_1 \quad (\text{A28})$$

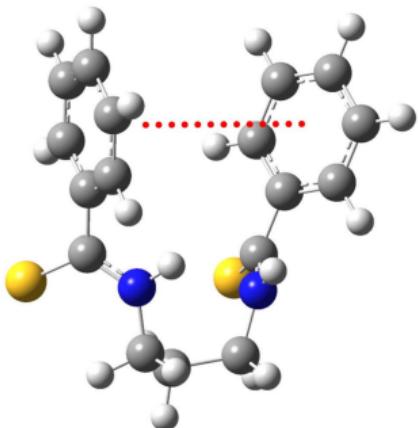
The  $U_8$  and  $U_g$  matrices are defined on the next page.

where each  $\sigma$  is the Boltzmann factor for the Gibbs free energy of the conformation expressed on the left (bonds 5, 6, and 7 or bonds d, e, and f) and upper (bond 8 or g) ends of the matrix. For example, the (6, 16) element corresponds to  $\sigma_{tg+g-t} = \exp(\Delta G_{tg+g-t}/RT)$ .

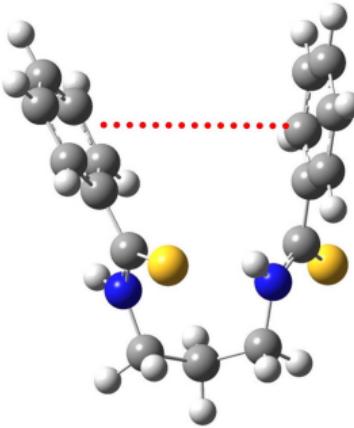


**Fig. S1** Intramolecular interactions of 3DBA:  $\pi/\pi$  of (a) g+g+g-g- and (b) g+g+g-g+; C-H... $\pi$  of (c) tg+g-g-; NH...O=C of g+g+g+g-.

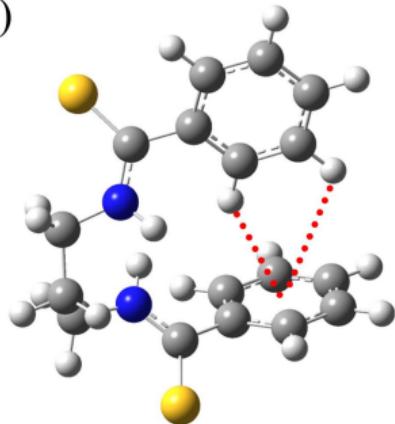
(a)



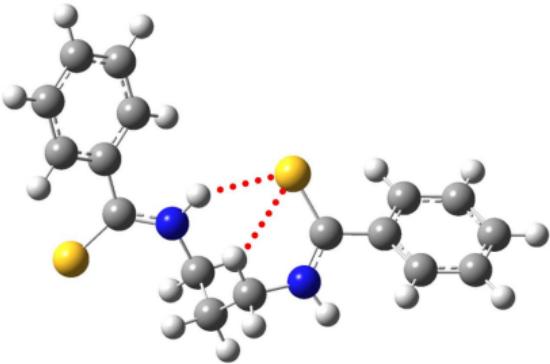
(b)



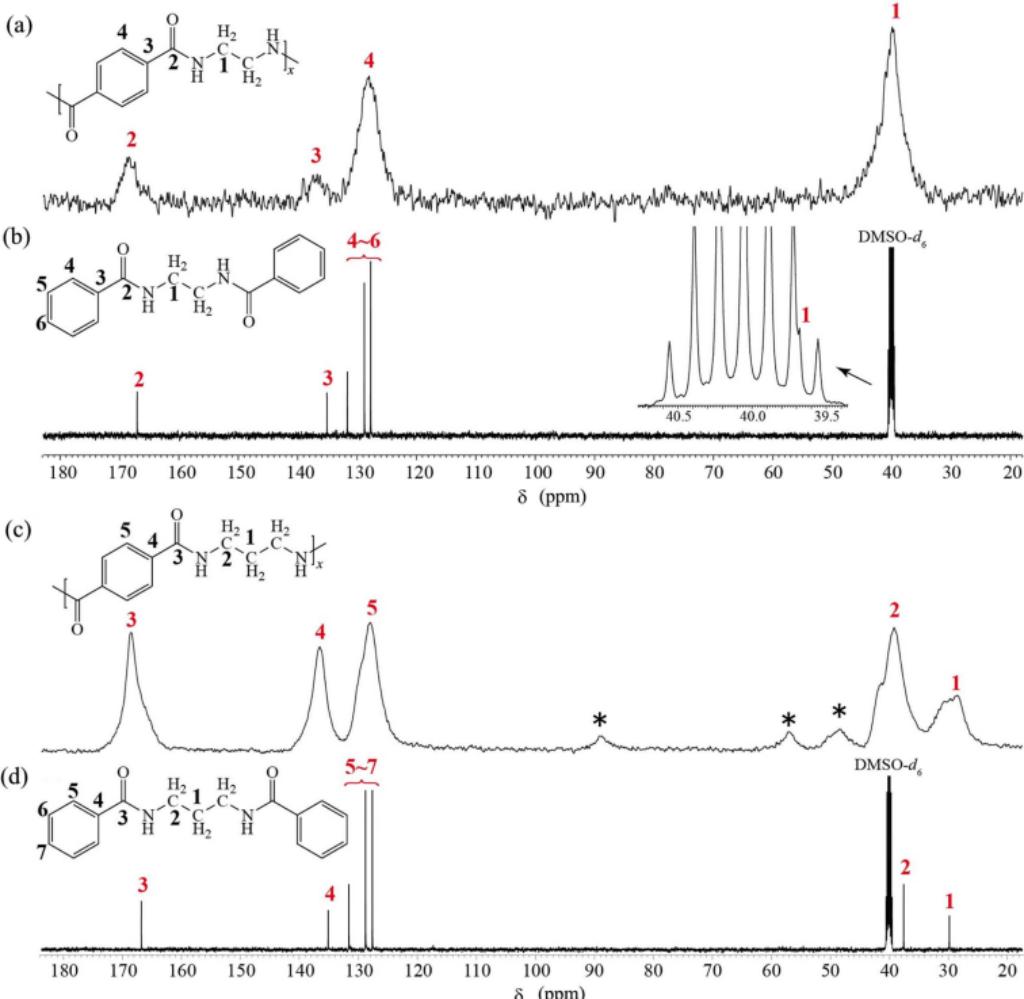
(c)



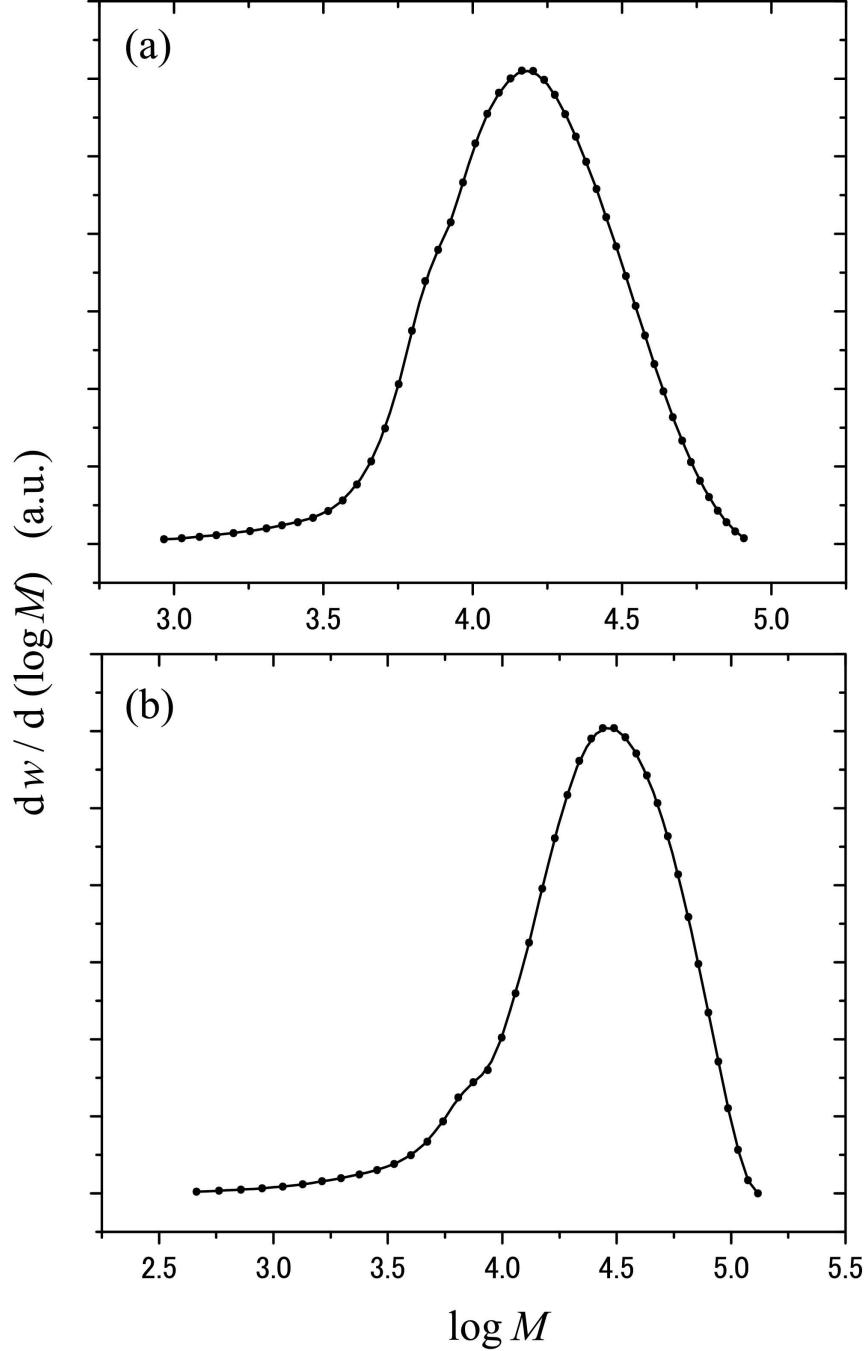
(d)



**Fig. S2** Intramolecular interactions of 3DBTA:  $\pi/\pi$  of (a) g+g+g-g- and (b) g+g+g-g+; C-H... $\pi$  of (c) tg+g-g-; NH..S=C of g+g+g+g-.



**Fig. S3** Solid-state <sup>13</sup>C NMR spectra observed from (a) PA2T and (c) PA3T, compared with solution spectra from (b) 2DBA and (d) 3DBA dissolved in DMSO-*d*<sub>6</sub>. The peaks were assigned as indicated, and the asterisk represents the spinning sideband.



**Fig. S4** Molecular weight distributions of (a) PTA2T and (b) PTA3T.

**Table S1** Geometrical parameters of PA2T, used in the refined RIS calculations

conformation					
bond <sup>a</sup>			$l_j$ <sup>b</sup>	$\theta_{j-1}$ <sup>c</sup>	$\theta_j$ <sup>d</sup>
$j-1$	$j$	$j+1$			$\phi_j$ <sup>e</sup>
bond a (c)					
t	t	t-t	1.352	121.5	116.8
$g^+$			1.362	122.3	117.8
$g^-$			1.362	122.3	117.8
t	t	(t-c) <sup>+</sup>	1.352	121.5	116.7
$g^+$			1.361	122.4	117.9
$g^-$			1.361	122.4	117.9
t	t	(t-c) <sup>-</sup>	1.352	121.5	116.7
$g^+$			1.361	122.4	117.9
$g^-$			1.361	122.4	117.9
t	t	(c-t) <sup>+</sup>			
$g^+$			1.361	122.4	119.1
$g^-$			1.361	122.4	119.1
t	t	(c-t) <sup>-</sup>			
$g^+$			1.361	122.4	119.1
$g^-$			1.361	122.4	119.1
t	t	c-c	1.352	121.5	116.7
$g^+$			1.362	122.3	119.1
$g^-$			1.362	122.3	119.1
bond b					
t	t-t	t	5.811	116.8	116.8
	(t-c) <sup>+</sup>		5.811	116.7	116.7
	(t-c) <sup>-</sup>		5.811	116.7	116.7
	(c-t) <sup>+</sup>		5.809	116.8	116.8
	(c-t) <sup>-</sup>		5.809	116.8	116.8
	c-c		5.809	116.7	116.7
bond d (f)					
t	t	t			
$g^+$			1.453	123.2	112.3
$g^-$			1.453	123.2	112.3
t	$g^+$		1.457	122.1	111.1
$g^+$			1.456	122.9	113.7
$g^-$			1.462	123.2	114.6
t	$g^-$		1.457	122.1	111.1
$g^+$			1.462	123.2	114.6
$g^-$			1.456	122.9	113.7

conformation					
bond <sup>a</sup>			$l_j$ <sup>b</sup>	$\theta_{j-1}$ <sup>c</sup>	$\theta_j$ <sup>d</sup>
$j-1$	$j$	$j+1$			$\phi_j$ <sup>e</sup>
t	t	t			
$g^+$			$g^+$		
$g^-$			$g^-$		
$g^+$			t		
$g^-$			$g^+$		
$g^+$			$g^-$	1.525	111.1
$g^-$			t	1.525	-112.7
$g^+$			$g^+$	1.525	111.1
$g^-$			$g^-$	1.525	112.7
t	t	$g^+$			
$g^+$			$g^-$	1.525	-112.7
$g^-$			t	1.538	112.3
$g^+$			$g^+$	1.534	113.7
$g^-$			$g^-$	1.532	113.6
$g^+$			t	1.538	-119.0
$g^-$			$g^+$	1.533	112.1
$g^+$			$g^-$	1.533	0.5
$g^-$			t	1.538	113.7
$g^+$			$g^+$	1.533	116.7
$g^-$			$g^-$	1.533	113.0
t	t	$g^-$			
$g^+$			$g^+$	1.525	114.6
$g^-$			$g^-$	1.525	112.7
$g^+$			t	1.538	112.1
$g^-$			$g^+$	1.533	113.0
$g^+$			$g^-$	1.533	116.7
$g^-$			t	1.538	-116.7
$g^+$			$g^+$	1.532	113.6
$g^-$			$g^-$	1.534	119.0
$g^+$			t	1.534	-116.8

<sup>a</sup> $j$  denotes the current bond. The blank line represents that the conformation is nonexistent. <sup>b</sup>Length of bond  $j$  in Å. <sup>c</sup>Angle formed between bonds  $j-1$  and  $j$  in deg. <sup>d</sup>Angle formed between bonds  $j$  and  $j+1$  in deg. <sup>e</sup>Dihedral angle of bond  $j$  in deg.

**Table S2** Geometrical parameters of PTA2T, used in the refined RIS calculations

conformation						
			bond <sup>a</sup>			
<i>j</i> - 1	<i>j</i>	<i>j</i> + 1	<i>l<sub>j</sub></i> <sup>b</sup>	$\theta_{j-1}$ <sup>c</sup>	$\theta_j$ <sup>d</sup>	$\phi_j$ <sup>e</sup>
bond a (c)						
t	t	t-t	1.336	124.3	115.4	1.8
g <sup>+</sup>			1.342	126.2	114.8	3.5
g <sup>-</sup>			1.342	126.2	114.8	-3.5
t	t	(t-c) <sup>+</sup>	1.336	124.6	115.5	2.8
g <sup>+</sup>			1.341	126.4	114.4	3.0
g <sup>-</sup>			1.341	126.4	114.4	3.0
t	t	(t-c) <sup>-</sup>	1.336	124.6	115.5	-2.8
g <sup>+</sup>			1.341	126.4	114.4	-3.0
g <sup>-</sup>			1.341	126.4	114.4	-3.0
t	t	(c-t) <sup>+</sup>	1.335	124.6	115.6	-2.4
g <sup>+</sup>			1.341	126.3	114.8	-2.9
g <sup>-</sup>			1.341	126.3	114.8	-2.9
t	t	(c-t) <sup>-</sup>	1.335	124.6	115.6	2.4
g <sup>+</sup>			1.341	126.3	114.8	2.9
g <sup>-</sup>			1.341	126.3	114.8	2.9
t	t	c-c	1.337	124.3	115.8	1.7
g <sup>+</sup>			1.342	126.2	114.9	3.7
g <sup>-</sup>			1.342	126.2	114.9	-3.7
bond b						
t	t-t	t	5.793	115.4	115.4	0.0
	(t-c) <sup>+</sup>		5.794	115.5	115.5	79.6
	(t-c) <sup>-</sup>		5.794	115.5	115.5	-79.6
	(c-t) <sup>+</sup>		5.792	115.6	115.6	98.0
	(c-t) <sup>-</sup>		5.792	115.6	115.6	-98.0
	c-c		5.792	115.8	115.8	180.0
bond d (f)						
t	t	t	1.456	125.3	109.7	-9.3
g <sup>+</sup>			1.454	126.2	111.5	89.9
g <sup>-</sup>			1.454	126.2	111.5	-89.9
t	t	g <sup>+</sup>	1.458	124.6	111.8	0.2
g <sup>+</sup>			1.457	126.2	113.6	93.1
g <sup>-</sup>			1.461	126.8	114.2	-81.8
t	t	g <sup>-</sup>	1.458	124.6	111.8	-0.2
g <sup>+</sup>			1.461	126.8	114.2	81.8
g <sup>-</sup>			1.457	126.2	113.6	-93.1

conformation						
			bond <sup>a</sup>			
<i>j</i> - 1	<i>j</i>	<i>j</i> + 1	<i>l<sub>j</sub></i> <sup>b</sup>	$\theta_{j-1}$ <sup>c</sup>	$\theta_j$ <sup>d</sup>	$\phi_j$ <sup>e</sup>
bond e						
t	t	t	1.526		109.6	0.4
		g <sup>+</sup>	1.520		111.7	111.5
		g <sup>-</sup>	1.520		111.7	-111.5
g <sup>+</sup>	t		1.531		109.7	-1.5
		g <sup>+</sup>	1.530		112.1	113.8
		g <sup>-</sup>	1.525		111.8	-112.1
g <sup>-</sup>	t		1.531		109.7	1.5
		g <sup>+</sup>	1.525		111.8	112.1
		g <sup>-</sup>	1.530		112.1	-113.8
t	t	g <sup>+</sup>	1.531		111.6	-1.5
		g <sup>+</sup>	1.530		113.5	113.8
		g <sup>-</sup>	1.525		114.2	-112.1
g <sup>+</sup>	t		1.539		111.6	9.8
		g <sup>+</sup>	1.533		113.6	116.8
g <sup>-</sup>	t		1.538		111.5	-0.7
		g <sup>+</sup>				
		g <sup>-</sup>				
t	t	g <sup>-</sup>	1.531		111.6	1.5
		g <sup>+</sup>	1.525		114.2	112.1
		g <sup>-</sup>	1.530		113.5	-113.8
g <sup>+</sup>	t		1.538		111.5	0.7
		g <sup>+</sup>				
		g <sup>-</sup>				
g <sup>-</sup>	t		1.539		111.6	-9.8
		g <sup>+</sup>				
		g <sup>-</sup>	1.533		113.6	-116.8

<sup>a</sup>*j* denotes the current bond. The blank line represents that the conformation is nonexistent. <sup>b</sup>Length of bond *j* in Å. <sup>c</sup>Angle formed between bonds *j* - 1 and *j* in deg. <sup>d</sup>Angle formed between bonds *j* and *j* + 1 in deg. <sup>e</sup>Dihedral angle of bond *j* in deg.

**Table S3** Geometrical parameters of PA3T, used in the refined RIS calculations

conformation						conformation				
			bond <sup>a</sup>			bond		bond <sup>a</sup>		
j - 1	j	j + 1	$l_j$ <sup>b</sup>	$\theta_{j-1}$ <sup>c</sup>	$\theta_j$ <sup>d</sup>	$l_j$ <sup>b</sup>	$\theta_{j-1}$ <sup>c</sup>	$\theta_j$ <sup>d</sup>	$\phi_j$ <sup>e</sup>	
bond a (c)										
t	t	t-t								
g <sup>+</sup>			1.360	123.4	117.6	-0.6				
g <sup>-</sup>			1.360	123.4	117.6	0.6				
t	t	(t-c) <sup>+</sup>								
g <sup>+</sup>			1.360	122.3	117.9	-1.8				
g <sup>-</sup>			1.360	122.3	117.9	-1.8				
t	t	(t-c) <sup>-</sup>								
g <sup>+</sup>			1.360	122.3	117.9	1.8				
g <sup>-</sup>			1.360	122.3	117.9	1.8				
t	t	(c-t) <sup>+</sup>								
g <sup>+</sup>			1.359	122.7	119.3	-1.6				
g <sup>-</sup>			1.359	122.7	119.3	-1.6				
t	t	(c-t) <sup>-</sup>								
g <sup>+</sup>			1.359	122.7	119.3	1.6				
g <sup>-</sup>			1.359	122.7	119.3	1.6				
t	t	c-c								
g <sup>+</sup>			1.359	122.8	119.1	-1.6				
g <sup>-</sup>			1.359	122.8	119.1	1.6				
bond b										
t	t-t	t	5.825	118.1	118.1	0.0				
	(t-c) <sup>+</sup>		5.824	118.0	118.0	46.9				
	(t-c) <sup>-</sup>		5.824	118.0	118.0	-46.9				
	(c-t) <sup>+</sup>		5.823	119.4	119.4	129.2				
	(c-t) <sup>-</sup>		5.823	119.4	119.4	-129.2				
	c-c		5.822	119.2	119.2	180.0				
bond d (g)										
t	t	t	1.458	122.6	110.9	-19.0				
g <sup>+</sup>			1.457	123.3	113.1	88.8				
g <sup>-</sup>			1.457	123.3	113.1	-88.8				
t		g <sup>+</sup>								
g <sup>+</sup>			1.456	123.8	113.6	76.9				
g <sup>-</sup>			1.461	123.5	113.3	-34.8				
t		g <sup>-</sup>								
g <sup>+</sup>			1.461	123.5	113.3	34.8				
g <sup>-</sup>			1.456	123.8	113.6	-76.9				

<sup>a</sup>*j* denotes the current bond. The blank line represents that the conformation is nonexistent. <sup>b</sup>Length of bond *j* in Å. <sup>c</sup>Angle formed between bonds *j* - 1 and *j* in deg. <sup>d</sup>Angle formed between bonds *j* and *j* + 1 in deg. <sup>e</sup>Dihedral angle of bond *j* in deg.

**Table S4** Geometrical parameters of PTA3T, used in the refined RIS calculations

conformation						
			bond <sup>a</sup>			
<i>j</i> - 1	<i>j</i>	<i>j</i> + 1	<i>l<sub>j</sub></i> <sup>b</sup>	$\theta_{j-1}$ <sup>c</sup>	$\theta_j$ <sup>d</sup>	$\phi_j$ <sup>e</sup>
bond a (c)						
t	t	t-t	1.338	125.3	115.1	2.4
g <sup>+</sup>			1.339	126.6	114.6	2.1
g <sup>-</sup>			1.339	126.6	114.6	-2.1
t	t	(t-c) <sup>+</sup>	1.338	125.3	115.2	2.5
g <sup>+</sup>			1.339	126.6	114.5	3.9
g <sup>-</sup>			1.339	126.6	114.5	3.9
t	t	(t-c) <sup>-</sup>	1.338	125.3	115.2	-2.5
g <sup>+</sup>			1.339	126.6	114.5	-3.9
g <sup>-</sup>			1.339	126.6	114.5	-3.9
t	t	(c-t) <sup>+</sup>	1.338	125.3	115.3	-2.0
g <sup>+</sup>			1.339	126.6	114.6	-1.8
g <sup>-</sup>			1.339	126.6	114.6	-1.8
t	t	(c-t) <sup>-</sup>	1.338	125.3	115.3	2.0
g <sup>+</sup>			1.339	126.6	114.6	1.8
g <sup>-</sup>			1.339	126.6	114.6	1.8
t	t	c-c	1.338	125.4	115.1	2.2
g <sup>+</sup>			1.339	126.6	114.5	1.7
g <sup>-</sup>			1.339	126.6	114.5	-1.7
bond b						
t	t-t	t	5.809	115.1	115.1	0.0
	(t-c) <sup>+</sup>		5.809	115.2	115.2	75.8
	(t-c) <sup>-</sup>		5.809	115.2	115.2	-75.8
	(c-t) <sup>+</sup>		5.808	115.3	115.3	102.5
	(c-t) <sup>-</sup>		5.808	115.3	115.3	-102.5
	c-c		5.808	115.1	115.1	180.0
bond d (g)						
t	t	t	1.458	125.4	110.5	6.2
g <sup>+</sup>			1.458	126.4	112.3	88.9
g <sup>-</sup>			1.458	126.4	112.3	-88.9
t		g <sup>+</sup>	1.461	125.6	111.6	-9.9
g <sup>+</sup>			1.461	126.1	114.0	112.7
g <sup>-</sup>			1.460	127.4	112.5	-59.0
t		g <sup>-</sup>	1.461	125.6	111.6	9.9
g <sup>+</sup>			1.460	127.4	112.5	59.0
g <sup>-</sup>			1.461	126.1	114.0	-112.7

conformation						
			bond <sup>a</sup>			
<i>j</i> - 1	<i>j</i>	<i>j</i> + 1	<i>l<sub>j</sub></i> <sup>b</sup>	$\theta_{j-1}$ <sup>c</sup>	$\theta_j$ <sup>d</sup>	$\phi_j$ <sup>e</sup>
bond e (f)						
t	t	t	1.525	110.5	110.7	-0.6
		g <sup>+</sup>	1.525	111.6	113.1	109.8
		g <sup>-</sup>	1.525	111.6	113.1	-109.8
g <sup>+</sup>	t		1.532	112.6	110.8	-0.3
		g <sup>+</sup>	1.532	114.0	113.1	112.7
		g <sup>-</sup>	1.530	112.5	113.0	-113.0
g <sup>-</sup>	t		1.532	112.6	110.8	0.3
		g <sup>+</sup>	1.530	112.5	113.0	113.0
		g <sup>-</sup>	1.532	114.0	113.1	-112.7
t	t	g <sup>+</sup>	1.528	110.4	113.1	0.4
		g <sup>+</sup>	1.528	111.4	115.1	110.7
		g <sup>-</sup>	1.535	113.4	116.1	-91.1
g <sup>+</sup>	t		1.535	112.3	113.0	-8.2
		g <sup>+</sup>	1.534	113.8	115.3	115.2
		g <sup>-</sup>	1.535	113.4	116.1	-91.1
g <sup>-</sup>	t		1.533	112.4	113.2	-1.0
		g <sup>+</sup>				
		g <sup>-</sup>	1.533	115.3	116.0	-110.4
t	t	g <sup>-</sup>	1.528	110.4	113.1	-0.4
		g <sup>+</sup>	1.535	113.4	116.1	91.1
		g <sup>-</sup>	1.528	111.4	115.1	-110.7
g <sup>+</sup>	t		1.533	112.4	113.2	1.0
		g <sup>+</sup>	1.533	115.3	116.0	110.4
		g <sup>-</sup>				
g <sup>-</sup>	t		1.535	112.3	113.0	8.2
		g <sup>+</sup>	1.535	113.4	116.1	91.1
		g <sup>-</sup>	1.534	113.8	115.3	-115.2

<sup>a</sup>*j* denotes the current bond. The blank line represents that the conformation is nonexistent. <sup>b</sup>Length of bond *j* in Å. <sup>c</sup>Angle formed between bonds *j* - 1 and *j* in deg. <sup>d</sup>Angle formed between bonds *j* and *j* + 1 in deg. <sup>e</sup>Dihedral angle of bond *j* in deg.

**Table S5** Geometrical parameters of P3TS<sub>2</sub>, used in the refined RIS calculations

conformation						
bond <sup>a</sup>						
<i>j</i> - 1	<i>j</i>	<i>j</i> + 1	<i>l<sub>j</sub></i> <sup>b</sup>	<i>θ<sub>j-1</sub></i> <sup>c</sup>	<i>θ<sub>j</sub></i> <sup>d</sup>	<i>ϕ<sub>j</sub></i> <sup>e</sup>
bond a (c)						
t	t	trans	1.807	98.4	117.9	0.0
g <sup>+</sup>			1.809	99.0	117.7	0.2
g <sup>-</sup>			1.809	99.0	117.7	-0.2
t	t	cis	1.808	98.5	118.8	0.0
g <sup>+</sup>			1.804	99.6	118.6	-0.1
g <sup>-</sup>			1.804	99.6	118.6	0.1
bond b						
t	trans	t	5.798	117.9	117.9	0.0
	cis		5.787	118.8	118.8	180.0
bond d (g)						
t	t	t	1.838	98.4	109.7	0.0
g <sup>+</sup>			1.835	98.9	113.5	97.4
g <sup>-</sup>			1.835	98.9	113.5	-97.4
t	g <sup>+</sup>		1.841	98.6	111.4	-12.6
g <sup>+</sup>			1.838	98.7	114.7	96.9
g <sup>-</sup>			1.838	100.0	115.1	-81.1
t	g <sup>-</sup>		1.841	98.6	111.4	12.6
g <sup>+</sup>			1.838	100.0	115.1	81.1
g <sup>-</sup>			1.838	98.7	114.7	-96.9

conformation						
bond <sup>a</sup>						
<i>j</i> - 1	<i>j</i>	<i>j</i> + 1	<i>l<sub>j</sub></i> <sup>b</sup>	<i>θ<sub>j-1</sub></i> <sup>c</sup>	<i>θ<sub>j</sub></i> <sup>d</sup>	<i>ϕ<sub>j</sub></i> <sup>e</sup>
bond e (f)						
t	t	t	1.532	109.7	110.3	0.0
		g <sup>+</sup>	1.534	111.4	113.3	111.8
		g <sup>-</sup>	1.534	111.4	113.3	-111.8
g <sup>+</sup>	t		1.532	113.5	110.5	-1.6
		g <sup>+</sup>	1.533	114.7	113.1	113.4
		g <sup>-</sup>	1.535	115.1	113.6	-114.2
g <sup>-</sup>	t		1.532	113.5	110.5	1.6
		g <sup>+</sup>	1.535	115.1	113.6	114.2
		g <sup>-</sup>	1.533	114.7	113.1	-113.4
t	t	g <sup>+</sup>	1.530	109.6	113.1	-0.1
		g <sup>+</sup>	1.532	111.0	116.0	114.2
		g <sup>-</sup>	1.533	115.9	116.5	-92.7
g <sup>+</sup>	t		1.528	113.6	113.4	6.2
		g <sup>+</sup>	1.533	114.0	115.2	107.4
		g <sup>-</sup>	1.534	117.1	116.8	-105.2
g <sup>-</sup>	t		1.530	113.3	113.2	-0.3
		g <sup>+</sup>	1.533	114.0	115.2	107.4
		g <sup>-</sup>	1.536	116.1	116.8	-96.4
t	t	g <sup>-</sup>	1.530	109.6	113.1	0.1
		g <sup>+</sup>	1.533	115.9	116.5	92.7
		g <sup>-</sup>	1.532	111.0	116.0	-114.2
g <sup>+</sup>	t		1.530	113.3	113.2	0.3
		g <sup>+</sup>	1.536	116.1	116.8	96.4
		g <sup>-</sup>	1.533	114.0	115.2	-107.4
g <sup>-</sup>	t		1.528	113.6	113.4	-6.2
		g <sup>+</sup>	1.534	117.1	116.8	105.2
		g <sup>-</sup>	1.533	114.0	115.2	-107.4

<sup>a</sup> *j* denotes the current bond. The blank line represents that the conformation is nonexistent. <sup>b</sup>Length of bond *j* in Å. <sup>c</sup>Angle formed between bonds *j* - 1 and *j* in deg. <sup>d</sup>Angle formed between bonds *j* and *j* + 1 in deg. <sup>e</sup>Dihedral angle of bond *j* in deg.

**Table S6** Geometrical parameters of P3TS<sub>4</sub>, used in the refined RIS calculations

conformation						
			bond <sup>a</sup>			
<i>j</i> - 1	<i>j</i>	<i>j</i> + 1	<i>l<sub>j</sub></i> <sup>b</sup>	$\theta_{j-1}$ <sup>c</sup>	$\theta_j$ <sup>d</sup>	$\phi_j$ <sup>e</sup>
bond a (c)						
t	t	t-t	1.758	103.9	113.0	3.1
g <sup>+</sup>			1.770	104.7	112.7	2.1
g <sup>-</sup>			1.770	104.7	112.7	-2.1
t	t	(t-c) <sup>+</sup>	1.759	103.9	113.2	4.0
g <sup>+</sup>			1.772	104.2	112.1	5.9
g <sup>-</sup>			1.772	104.2	112.1	5.9
t	t	(t-c) <sup>-</sup>	1.759	103.9	113.2	-4.0
g <sup>+</sup>			1.772	104.2	112.1	-5.9
g <sup>-</sup>			1.772	104.2	112.1	-5.9
t	t	(c-t) <sup>+</sup>	1.758	103.9	113.4	-3.1
g <sup>+</sup>			1.771	104.7	113.0	-5.5
g <sup>-</sup>			1.771	104.7	113.0	-5.5
t	t	(c-t) <sup>-</sup>	1.758	103.9	113.4	3.1
g <sup>+</sup>			1.771	104.7	113.0	5.5
g <sup>-</sup>			1.771	104.7	113.0	5.5
t	t	c-c	1.759	103.8	113.3	-3.1
g <sup>+</sup>			1.771	104.7	112.9	2.0
g <sup>-</sup>			1.771	104.7	112.9	-2.0
bond b						
t	t-t	t	5.789	113.0	113.0	0.0
	(t-c) <sup>+</sup>		5.789	113.2	113.2	70.8
	(t-c) <sup>-</sup>		5.789	113.2	113.2	-70.8
	(c-t) <sup>+</sup>		5.787	113.4	113.4	106.3
	(c-t) <sup>-</sup>		5.787	113.4	113.4	-106.3
	c-c		5.788	113.3	113.3	180.0
bond d (g)						
t	t	t	1.831	103.6	109.1	3.7
g <sup>+</sup>			1.830	104.4	113.5	96.9
g <sup>-</sup>			1.830	104.4	113.5	-96.9
t	g <sup>+</sup>		1.834	103.5	110.7	1.3
g <sup>+</sup>			1.833	104.2	114.8	96.0
g <sup>-</sup>			1.835	105.4	113.7	-68.8
t	g <sup>-</sup>		1.834	103.5	110.7	-1.3
g <sup>+</sup>			1.835	105.4	113.7	68.8
g <sup>-</sup>			1.833	104.2	114.8	-96.0

conformation						
			bond <sup>a</sup>			
<i>j</i> - 1	<i>j</i>	<i>j</i> + 1	<i>l<sub>j</sub></i> <sup>b</sup>	$\theta_{j-1}$ <sup>c</sup>	$\theta_j$ <sup>d</sup>	$\phi_j$ <sup>e</sup>
bond e (f)						
t	t	t	1.534	109.1	110.1	-0.8
		g <sup>+</sup>	1.535	110.7	113.2	112.6
		g <sup>-</sup>	1.535	110.7	113.2	-112.6
g <sup>+</sup>	t		1.533	113.5	110.2	1.5
		g <sup>+</sup>	1.535	114.8	112.6	113.2
		g <sup>-</sup>	1.536	113.7	113.2	-112.5
g <sup>-</sup>	t		1.533	113.5	110.2	-1.5
		g <sup>+</sup>	1.536	113.7	113.2	112.5
		g <sup>-</sup>	1.535	114.8	112.6	-113.2
t	t	g <sup>+</sup>	1.534	109.1	113.2	4.3
		g <sup>+</sup>	1.535	110.4	116.2	114.0
		g <sup>-</sup>	1.536	112.5	117.1	-101.3
g <sup>+</sup>	t		1.533	113.6	113.2	5.9
		g <sup>+</sup>	1.534	114.6	115.9	117.8
		g <sup>-</sup>	1.535	115.6	117.1	-104.7
g <sup>-</sup>	t		1.533	113.2	113.2	2.8
		g <sup>+</sup>	1.534	113.0	115.1	107.4
		g <sup>-</sup>	1.536	115.9	116.3	-98.2
t	t	g <sup>-</sup>	1.534	109.1	113.2	-4.3
		g <sup>+</sup>	1.536	112.5	117.1	101.3
		g <sup>-</sup>	1.535	110.4	116.2	-114.0
g <sup>+</sup>	t		1.533	113.2	113.2	-2.8
		g <sup>+</sup>	1.536	115.9	116.3	98.2
		g <sup>-</sup>	1.534	113.0	115.1	-107.4
g <sup>-</sup>	t		1.533	113.6	113.2	-5.9
		g <sup>+</sup>	1.535	115.6	117.1	104.7
		g <sup>-</sup>	1.534	114.6	115.9	-117.8

<sup>a</sup>*j* denotes the current bond. The blank line represents that the conformation is nonexistent. <sup>b</sup>Length of bond *j* in Å. <sup>c</sup>Angle formed between bonds *j* - 1 and *j* in deg. <sup>d</sup>Angle formed between bonds *j* and *j* + 1 in deg. <sup>e</sup>Dihedral angle of bond *j* in deg.

**Table S7** Average geometrical parameters of PA2T, PA3T, PTA2T, and PTA3T

	bond	bond length (Å)	bond angle (°)	dihedral angle (°)			
				$\phi_t$ or $\phi_{t-t}$	$\phi_{g^\pm}$ or $\phi_{(t-c)^\pm}$	$\phi_{(c-t)^\pm}$	$\phi_{c-c}$
PA2T	a	1.360	117.5	0.1			
	b	5.810	117.5	0.0	$\pm 53.6$	$\pm 123.0$	180.0
	c	1.360	122.5	0.1			
	d	1.458	112.9	0.0	$\pm 92.2$		
	e	1.529	112.9	0.2	$\pm 113.9$		
	f	1.458	122.5	0.0	$\pm 92.2$		
PA3T	a	1.359	118.7	0.0			
	b	5.823	118.7	0.0	$\pm 46.9$	$\pm 129.2$	180.0
	c	1.359	123.0	0.0			
	d	1.458	112.8	-19.0	$\pm 72.1$		
	e	1.531	112.8	-0.2	$\pm 116.2$		
	f	1.531	112.8	-0.2	$\pm 116.2$		
	g	1.458	123.0	-19.0	$\pm 72.1$		
PTA2T	a	1.340	115.3	0.1			
	b	5.793	115.3	0.0	$\pm 79.6$	$\pm 98.0$	180.0
	c	1.340	125.8	0.1			
	d	1.457	112.4	-2.2	$\pm 88.4$		
	e	1.529	112.4	0.0	$\pm 113.3$		
	f	1.457	125.8	-2.2	$\pm 88.4$		
PTA3T	a	1.338	115.1	0.3			
	b	5.808	115.1	0.0	$\pm 75.8$	$\pm 102.5$	180.0
	c	1.338	125.9	0.3			
	d	1.459	111.7	4.0	$\pm 88.4$		
	e	1.529	112.4	-0.2	$\pm 111.3$		
	f	1.529	111.7	-0.2	$\pm 111.3$		
	g	1.459	125.9	4.0	$\pm 88.4$		

**Table S8** Average geometrical parameters of P2TS<sub>2</sub>, P3TS<sub>2</sub>, P2TS<sub>4</sub>, and P3TS<sub>4</sub>

	bond	bond length (Å)	bond angle (°)	dihedral angle (°)			
				$\phi_t$ or $\phi_{t-t}$	$\phi_{g^\pm}$ or $\phi_{(t-c)^\pm}$	$\phi_{(c-t)^\pm}$	$\phi_{c-c}$
P2TS <sub>2</sub>	a	1.802	117.9	0.0			
	b	5.787	117.9	0.0			180.0
	c	1.802	99.4	0.0			
	d	1.832	113.1	-0.2	$\pm 97.3$		
	e	1.523	113.1	0.0	$\pm 115.0$		
	f	1.832	99.4	-0.2	$\pm 97.3$		
P3TS <sub>2</sub>	a	1.807	118.2	0.0			
	b	5.793	118.2	0.0			180.0
	c	1.807	99.0	0.0			
	d	1.837	113.6	0.0	$\pm 95.2$		
	e	1.532	113.3	0.0	$\pm 110.8$		
	f	1.532	113.6	0.0	$\pm 110.8$		
	g	1.837	99.0	0.0	$\pm 95.2$		
P2TS <sub>4</sub>	a	1.762	113.0	0.1			
	b	5.787	113.0	0.0	$\pm 71.5$	$\pm 106.3$	180.0
	c	1.762	104.5	0.1			
	d	1.826	113.3	1.2	$\pm 85.1$		
	e	1.525	113.3	0.0	$\pm 112.8$		
	f	1.826	104.5	1.2	$\pm 85.1$		
P3TS <sub>4</sub>	a	1.768	113.0	0.0			
	b	5.788	113.0	0.0	$\pm 70.8$	$\pm 106.3$	180.0
	c	1.768	104.3	0.0			
	d	1.832	113.3	0.8	$\pm 91.3$		
	e	1.534	113.7	0.0	$\pm 110.4$		
	f	1.534	113.3	0.0	$\pm 110.4$		
	g	1.832	104.3	0.8	$\pm 91.3$		