

Electronic Supplementary Information

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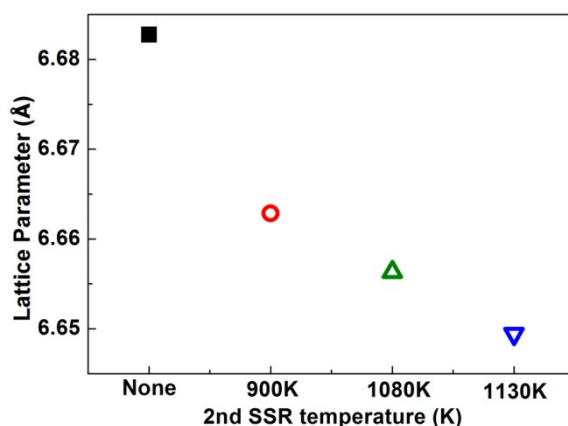


Figure SI1 Lattice parameters calculated from the data in Figure 1(b)

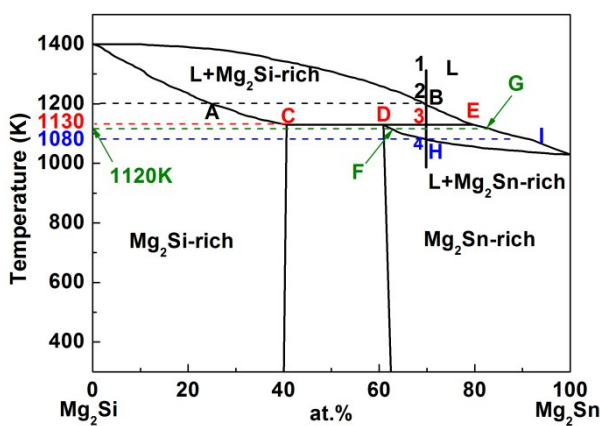


Figure SI2 Mg_2Si - Mg_2Sn pseudo-binary phase diagram, reported by E. N. Nikitin et al.¹

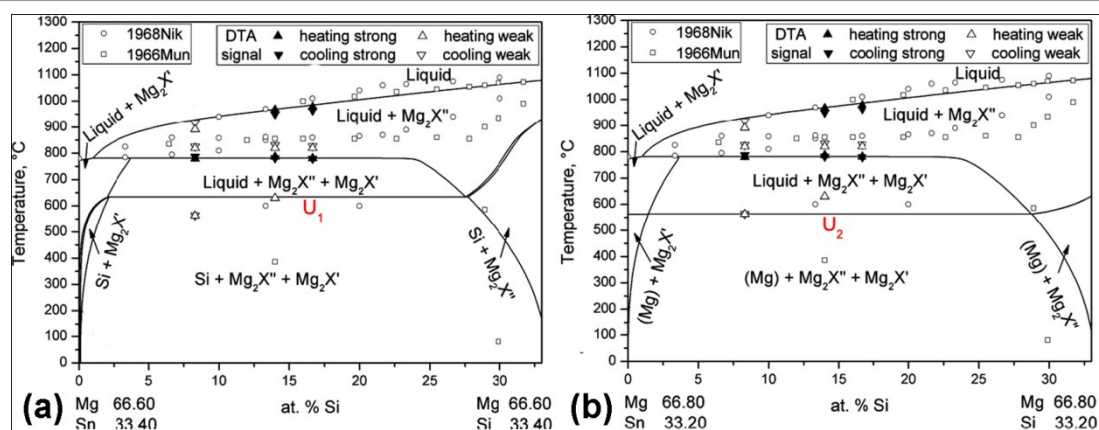


Figure S13 The peritectic reaction (a) at 900 K (U_1); (b) at 837 K (U_2). Reprinted from A. Kozlov et al.²

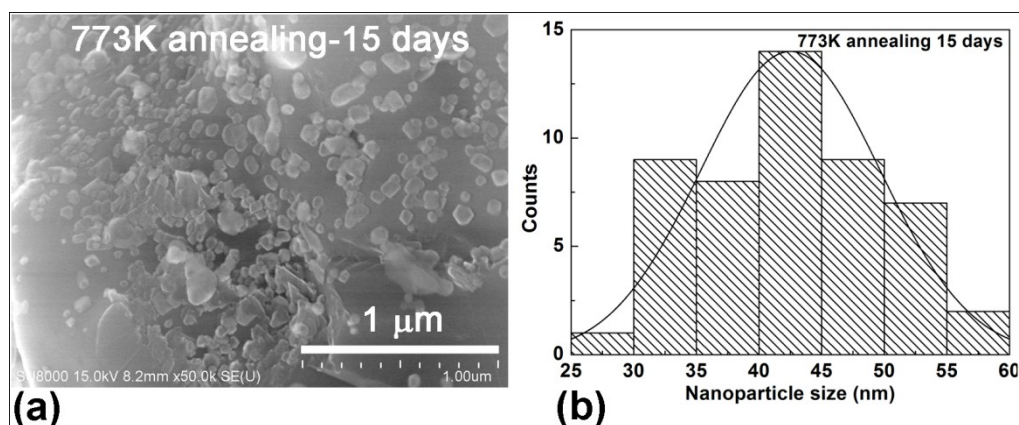


Figure S14 (a) The microstructure, (b) the nanoparticle size distribution of the sintered ingot after annealing at 773 K for 15 days (with the 2nd solid state reaction step (SSR) quenched at 1130 K).

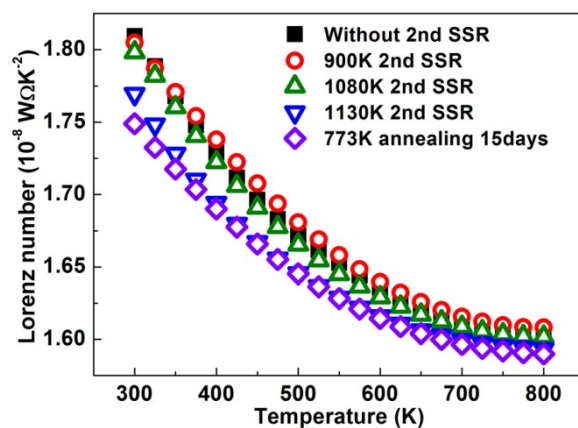


Figure S15 Lorenz number of samples with different heat treatments.

Basic equations for calculating the Lorenz number and the reduced Fermi levels are listed below³⁻⁵:

$$S = \pm \frac{k_B}{e} \left[\eta_F - \frac{(r+5/2)F_{r+3/2}(\eta_F)}{(r+3/2)F_{r+1/2}(\eta_F)} \right] \quad (1)$$

$$\eta_F = E_F / (k_B T) \quad (2)$$

$$F_i(\eta_F) = \int_0^\infty \frac{x^i dx}{1 + \exp(x - \eta_F)} \quad (3)$$

$$L = \left(\frac{k_B}{e} \right)^2 \left[\frac{3F_0(\eta_F)F_2(\eta_F) - 4F_1^2(\eta_F)}{F_0^2(\eta_F)} \right] \quad (4)$$

Here, η_F , $F_i(\eta_F)$, r , and k_B are the reduced Fermi level, the Fermi integral, the scattering factor, and the Boltzmann constant, respectively.

References

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- 2 A. Kozlov, J. Gröbner and R. Schmid-Fetzer, *Journal of Alloys and Compounds*, 2011, 509, 3326-3337.
- 3 W. Liu, H. Chi, H. Sun, Q. Zhang, K. Yin, X. Tang, Q. Zhang and C. Uher, *Physical Chemistry Chemical Physics*, 2014, 16, 6893-6897.
- 4 X. J. Tan, W. Liu, H. J. Liu, J. Shi, X. F. Tang and C. Uher, *Physical Review B*, 2012, 85, 205212.
- 5 A. May and G. Snyder, *Materials, preparation, and characterization in thermoelectrics*. CRC Press, Boca Raton, 2012, 11, 1-18.