Electronic Supplementary Information

Hierarchical Nanostructures of Diblock Copolymer Thin Films

Directed by a Saw-Toothed Substrate

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Since these two morphologies only form if there is a repulsive force between A-block and the substrate, otherwise, they do not, thus we have not put them into the Figure 2.



(b)

Figure S1. The specific structures of $L_{//}$ and $C^{az}_{//}$ formed by AB diblock copolymer thin films confined on the saw-toothed substrate. The 3D isosurface graphs are also given for a clear view beside the morphologies. The red color in isosurface graphs is assigned to A-block for a good correspondence. The black color shows the substrate. (a) $L_{//}$, (b) $C^{az}_{//}$.



Figure S2. Plot of total free energy as a function of AB diblock copolymer thin film thickness with $f_A = 0.30$, N = 60, $\chi N = 15$, $\theta_1 = 17.6^\circ$, $\theta_2 = 32.4^\circ$, $H_{AS} = 0.0$, $H_{BS} = 0.0$, $L_0 = 3.80R_{g0} \sim 12.02R_{g0}$, $L_z = 2.85R_{g0} \sim 10.75R_{g0}$.



(a) CM₂





(b) CM₃







Figure S3. Some complicated structures formed by AB diblock copolymer thin films confined on the saw-toothed substrate. The isosurfaces of A-block ($f_A = 0.30$) are plotted in red color, and otherwise, the isofurfaces of B-block are plotted in green color (not shown here).

We can obtain the density profile of block copolymer along *z*-direction by Eq. (S1) as below:

$$\varphi_i(z) = \iint \phi_i(x, y, z) dx dy / \iint dx dy$$
(S1)

where *i* belongs to A-block and B-block.



Figure S4. Density distribution of A-block along *z*-axis direction with $f_A = 0.30$, N = 60, $\chi N = 15$, $\theta_1 = 17.6^\circ$, $\theta_2 = 32.4^\circ$, $H_{AS} = 0.0$, $H_{BS} = 0.0$. (a) $L_0 = 5.69R_{g0}$, $L_z = 3.48R_{g0} \sim 4.43R_{g0}$, (b) $L_0 = 6.33R_{g0}$, $L_z = 3.80R_{g0} \sim 4.74R_{g0}$.



Figure S5. Morphological phase diagram in the plane L_z vs H_{AS} for AB diblock copolymer with $f_A = 0.30$, N = 60, $\chi N = 15$, $\theta_1 = 17.6^\circ$, $\theta_2 = 32.4^\circ$, $H_{BS} = 0.0$, $L_z = 4.43R_{g0} \sim 6.64R_{g0}$. The symbols indicated distinct structures in this study have been marked in the picture, respectively. (a) $L_0 = 6.96R_{g0}$, $H_{AS} = -3.0 \sim 1.5$, (b) $L_0 = 10.12R_{g0}$, $H_{AS} = -1.0 \sim 3.0$.



Figure S6. Plot of total free energy as a function of AB diblock copolymer thin film thickness with $f_A = 0.30$, N = 60, $\chi N = 15$, $\theta_1 = 17.6^\circ$, $\theta_2 = 32.4^\circ$, $H_{BS} = 0.0$, $L_z = 4.43R_{g0} \sim 6.64R_{g0}$. (a) $L_0 = 5.69R_{g0}$, $H_{AS} = -3.0 \sim 2.5$, (b) $L_0 = 4.43R_{g0}$, $H_{AS} = -3.0 \sim 1.5$.



Figure S7. The schematic cross section of the saw-toothed substrate with only one lateral periodicity: one of the tilt angles $\theta_1 = 17.6^\circ$, and another θ_2 varies from 17.6° to 62.5°.

$\boldsymbol{L_0} \mid L_0 / R_{g0}$	$\Delta \mid \Delta / R_{\rm g0}$	$\boldsymbol{L_0} \mid L_0 / R_{g0}$	$\Delta \mid \Delta / R_{\rm g0}$
12 <i>3.80</i>	2.538 0.80	26 8.22	5.499 1.74
14 <i>4.43</i>	2.961 0.94	28 <i>8.86</i>	5.922 <i>1.87</i>
16 <i>5.06</i>	3.384 <i>1.07</i>	30 <i>9.49</i>	6.345 2.01
18 5.69	3.807 <i>1.20</i>	32 <i>10.12</i>	6.768 2.14
20 <i>6.33</i>	4.230 <i>1.34</i>	34 <i>10.75</i>	7.191 2.27
22 <i>6.96</i>	4.653 1.47	36 <i>11.39</i>	7.614 2.41
24 7.59	5.076 <i>1.61</i>	38 <i>12.02</i>	8.037 2.54

Table S1. Summary the value of Δ corresponding diblock copolymer thin film thickness with varied substrate lateral periodicities L_0 , fixed substrate tilt angles $\theta_1 = 17.6^\circ$, $\theta_2 = 32.4^\circ$.

Table S2. Summary the value of Δ corresponding diblock copolymer thin film thickness with varied substrate tilt angle θ_2 , fixed substrate lateral periodicity $L_0 = 18$ and tilt angle $\theta_1 = 17.6^{\circ}$.

$ heta_2$ (°)	$\Delta \mid \Delta / R_{g0}$	$ heta_2$ (°)	$\Delta \mid \Delta / R_{g0}$
17.6	2.855 0.90	43.0	4.261 1.35
21.8	3.184 <i>1.01</i>	48.3	4.451 <i>1.41</i>
27.1	3.524 <i>1.11</i>	53.6	4.628 1.46
32.4	3.807 <i>1.20</i>	58.9	4.793 1.52
37.7	4.048 <i>1.28</i>	62.5	4.912 1.55

The value of the Δ is calculated by $\Delta = \tan(\theta_1) \tan(\theta_2) / [\tan(\theta_1) + \tan(\theta_2)] L_0$.