# Supplemental material:

## Enhancement of thermoelectric performance of β-Zn<sub>4</sub>Sb<sub>3</sub> through resonant

## distortion of electronic density of states doped with Gd

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#### (1) Microstructural characterization



**Fig. S1** (a) XRD patterns and (b) lattice constant of the  $\beta$ -(Zn<sub>1-x</sub>Gd<sub>x</sub>)<sub>4</sub>Sb<sub>3</sub> (*x*=0, 0.001, 0.002 and 0.003) samples.

#### (2) Lattice thermal conductivity



Fig. S2 Temperature dependences of lattice thermal conductivity  $\kappa_L$ .

### (3) The heat capacity of part samples



Fig. S3 Temperature dependences of heat capacity  $C_p$  for x = 0 and 0.002 compounds.

## (4) The magnetic contributions C<sub>m</sub> from Gd

The magnetic contributions  $C_m$  from 4f electrons of Gd cannot be ignored in Gd-doped samples. M.J. Parsons *et al.*<sup>1, 2</sup> have calculated the magnetic entropy  $S_m$  of Gd, which has proportional relationship with both temperature and Gd content at T<9 K. According to

relationship between entropy  $S_m$  and heat capacity  $C_m$ :  $C_m = T \frac{dS_m}{dT}$ , the magnetic heat capacity contribution  $C_m$  for the sample with *x*=0.002 can be derived as:  $C_m=3.6T$  (*mJ/mol. K*). Then total heat capacity for the Gd-doped samples should be written as  $C_p=\gamma T+bT^3+C_m$ , or  $C_p-C_m=\gamma T+bT^3$ . (see Fig. S4)



**Fig. S4** Temperature dependence of  $C_p$ ,  $C_m$  and  $C_p$ - $C_m$  for x=0.002 sample.

#### Reference

- M. J. Parsons, J. Crangle, B. Dennis, K. U. Neumann and K. R. A. Ziebeck, *Czech J Phys*, 1996, 46, 2057-2058.
- M. J. Parsons, J. Crangle, K. U. Neumann and K. R. A. Ziebeck, *J Magn Magn Mater*, 1998, **184**, 184-192.