

## SUPPLEMENTARY INFORMATION

### Chemical bonding and dynamic fluxionality of $B_{15}^+$ cluster: a nanoscale double-axle tank tread†

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## SUPPLEMENTARY INFORMATION – PART I

**Table S1.** Cartesian coordinates for the global-minimum structure of  $B_{15}^+ C_{2v} (^1A_1)$  and its corresponding  $C_{2v}$  transition state at the PBE0/6-311+G\* level.

**Figure S1.** Canonical molecular orbitals (CMOs) for the subset of eleven peripheral  $\sigma$  bonds in the  $C_{2v} (^1A_1)$  global minimum of  $B_{15}^+$  cluster. These CMOs are readily localized as two-center two-electron (2c-2e)  $\sigma$  bonds.

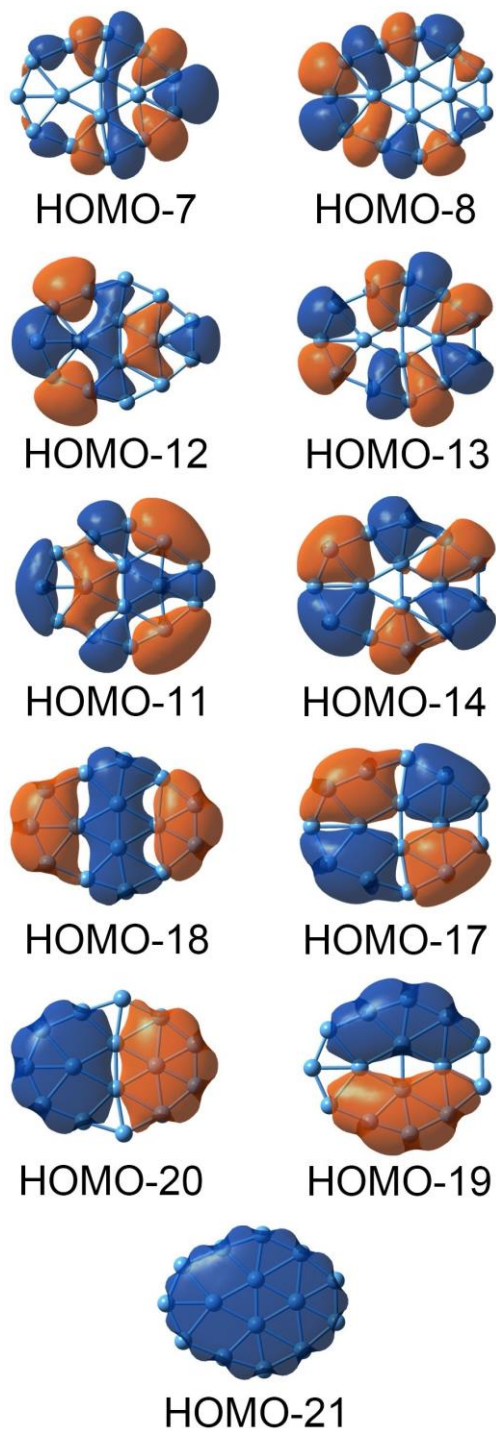
**Figure S2.** Canonical molecular orbitals (CMOs) of the  $C_{2v} (^1A_1)$  transition state of  $B_{15}^+$  cluster. (a) Eleven peripheral  $\sigma$  bonds, which can be localized as 2c-2e bonds. (b) Five delocalized  $\sigma$  bonds. (c) Two delocalized  $\sigma$  bonds associated with the inner rhombic  $B_4$  core. (d) Four delocalized  $\pi$  bonds. The CMOs for the (a), (b), and (d) subsets show one-to-one correspondence to each other, from bottom up.

- Figure S3.** Chemical bonding in the  $C_{2v}$  transition state of  $B_{15}^+$ . (a) The electron localization functions (ELFs). (b) Bonding elements as revealed from the adaptive natural density partitioning (AdNDP) analysis. The occupation numbers (ONs) are shown.
- Figure S4.** Optimized structure of the  $C_{2v}$  global minimum of  $B_{14}^-$  cluster at the PBE0/6-311+G\* level.
- Figure S5.** Evolution of electron localization function,  $ELF_{\sigma}$ , against the bifurcation value for the  $C_{2v}$  global minimum of  $B_{15}^+$  cluster. Note that for the rhombic B1B2B12B11 unit, the  $ELF_{\sigma}$  data is consistent with one four-center island only, rather than two three-center islands (B1B2B12 and B11B1B12), supporting the AdNDP scheme presented in Fig. 5(b).

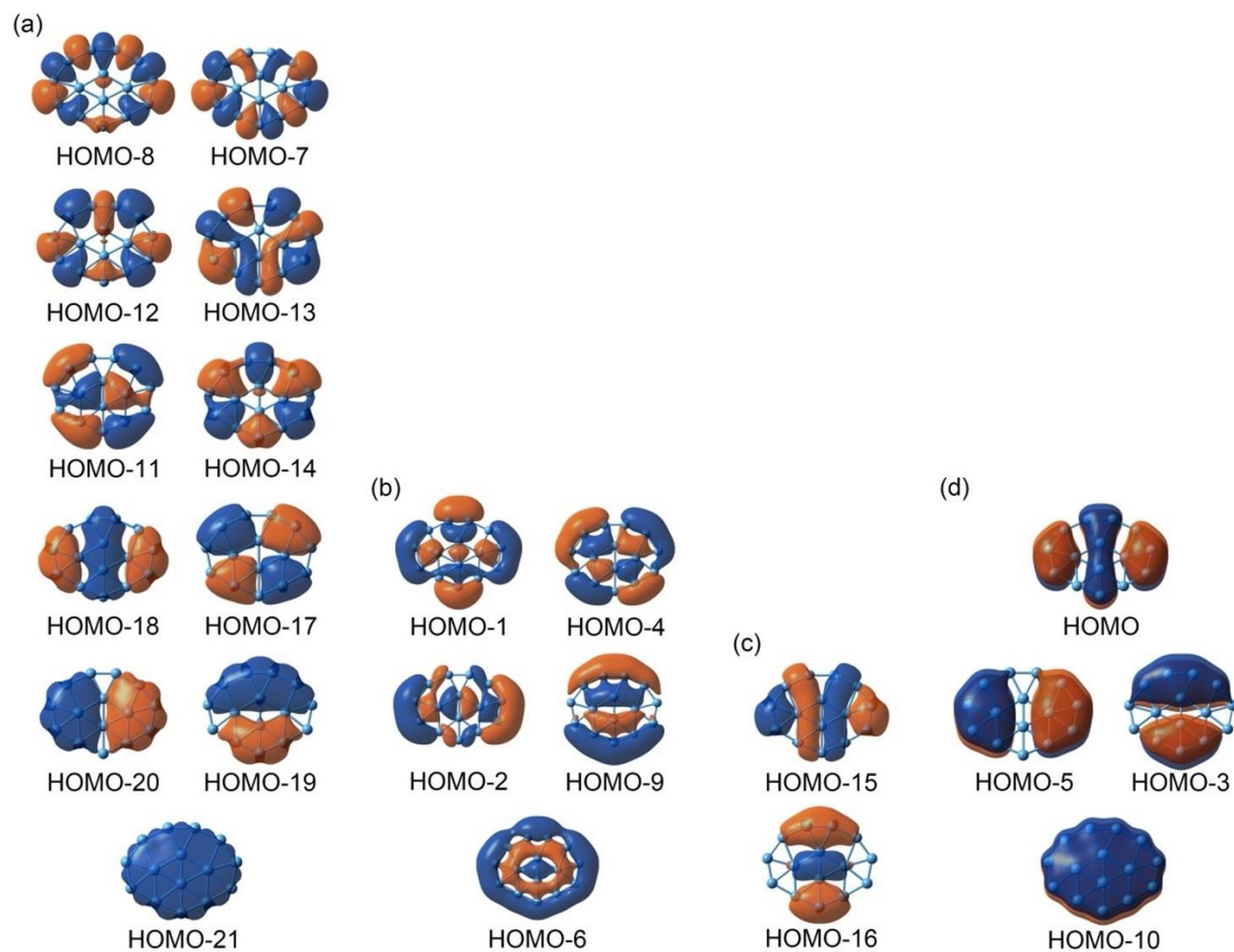
## SUPPLEMENTARY INFORMATION – PART II

**A short movie** extracted from the BOMD simulation for  $B_{15}^+$ . Each frame of the snapshot is reoriented horizontally. The simulation is performed at 500 K for over 60 ps and the movie roughly covers a time span of 30 ps.

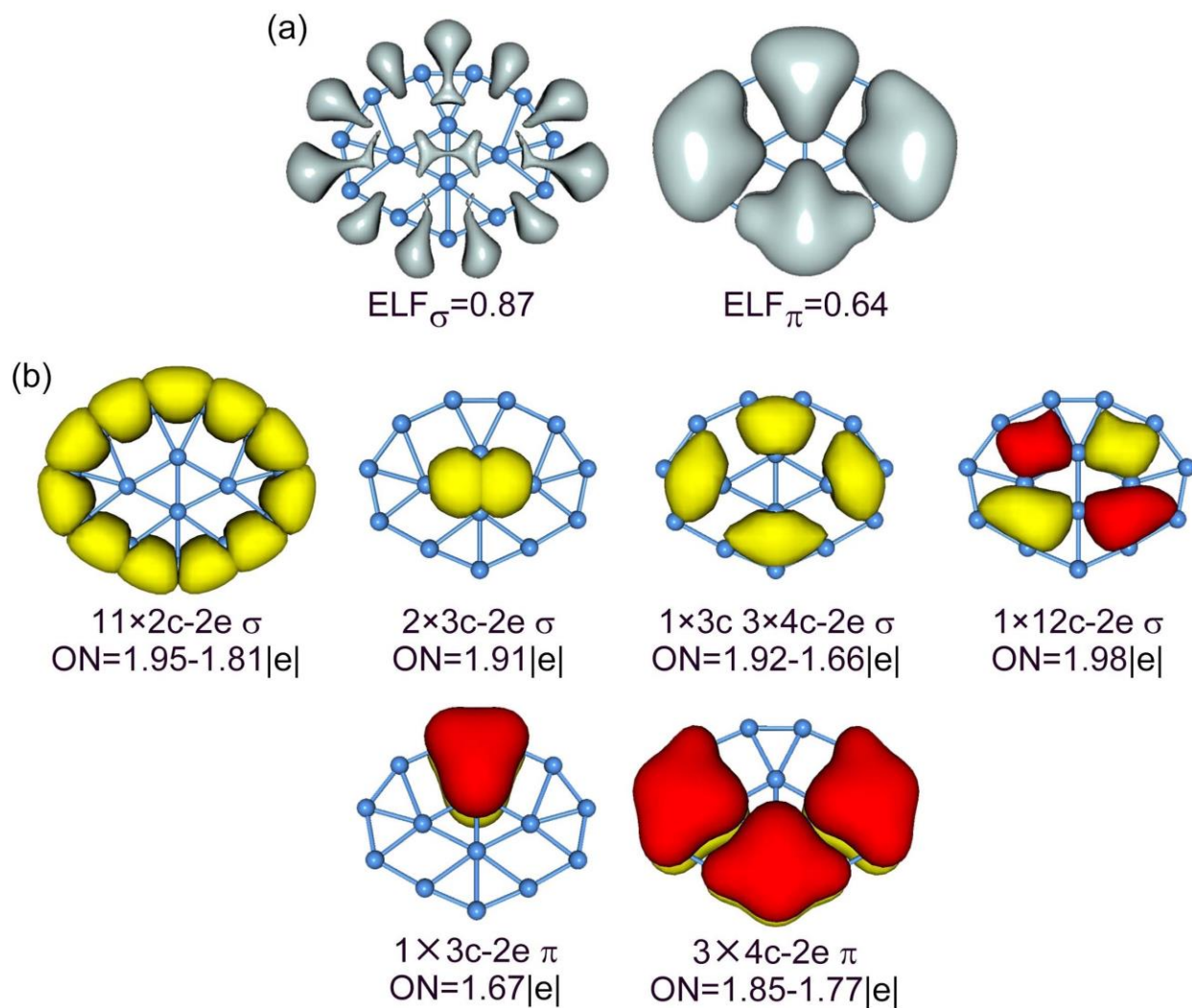
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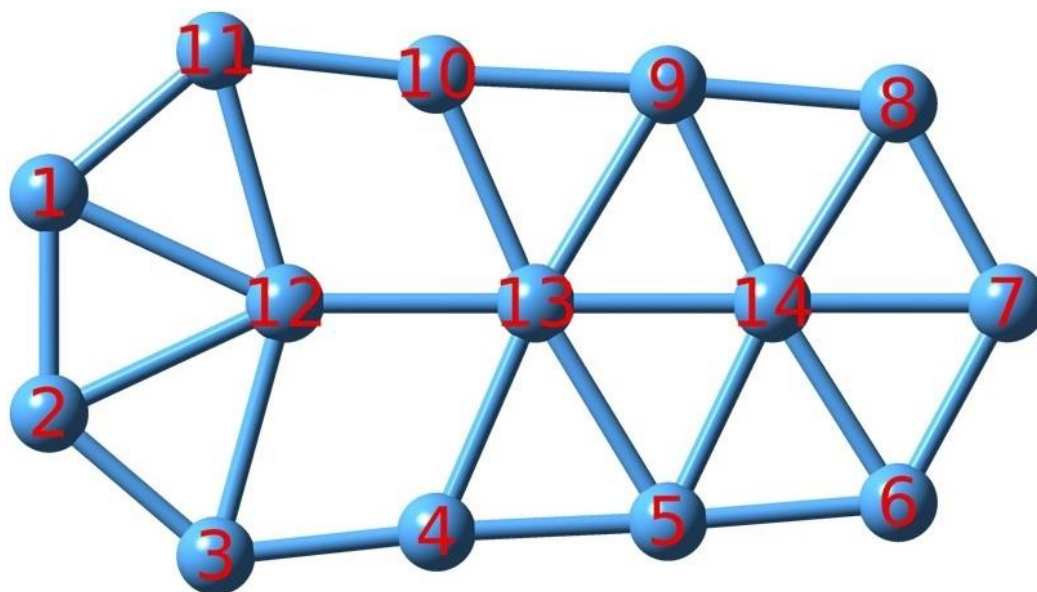
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**Figure S3.** Chemical bonding in the  $C_{2v}$  transition state of  $B_{15}^+$ . (a) The electron localization functions (ELFs). (b) Bonding elements as revealed from the adaptive natural density partitioning (AdNDP) analysis. The occupation numbers (ONs) are shown.

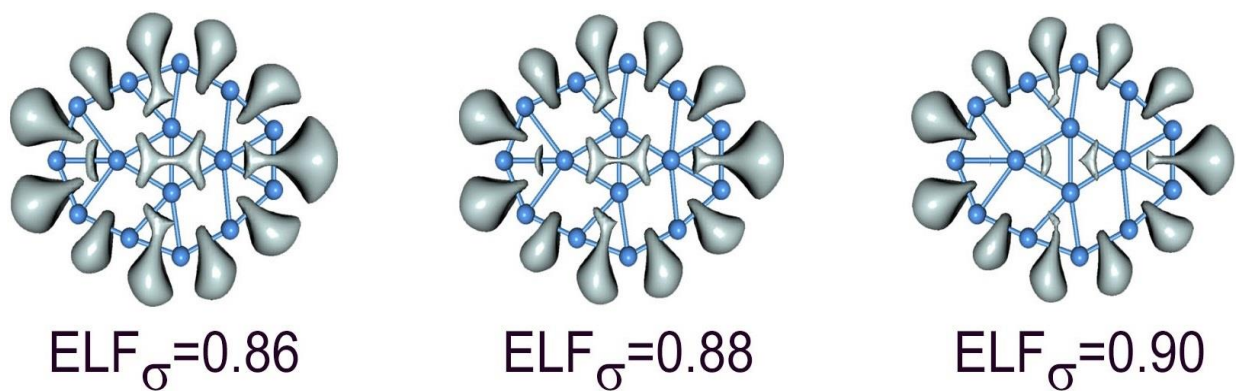


**Figure S4.** Optimized structure of the  $C_{2v}$  global minimum of  $B_{14}^-$  cluster at the PBE0/6-311+G\* level.



GM,  $C_{2v}$

**Figure S5.** Evolution of electron localization function,  $\text{ELF}_\sigma$ , against the bifurcation value for the  $C_{2v}$  global minimum of  $\text{B}_{15}^+$  cluster. Note that for the rhombic B1B2B12B11 unit, the  $\text{ELF}_\sigma$  data is consistent with one four-center island only, rather than two three-center islands (B1B2B12 and B11B1B12), supporting the AdNDP scheme presented in Fig. 5(b).



**Table S1.** Cartesian coordinates for the global-minimum structure of  $\text{B}_{15}^+ \text{C}_{2v} (^1\text{A}_1)$  and its corresponding  $\text{C}_{2v}$  transition state at the PBE0/6-311+G\* level.

**(a) GM of  $\text{B}_{15}^+ \text{C}_{2v}$**

B	0.00000000	0.00000000	3.22413600
B	0.00000000	1.38650300	2.60984100
B	0.00000000	2.00601300	1.12463900
B	0.00000000	2.47696800	-0.35955800
B	0.00000000	1.78165400	-1.78525600
B	0.00000000	0.76156000	-3.03970000
B	0.00000000	-0.76156000	-3.03970000
B	0.00000000	-1.78165400	-1.78525600
B	0.00000000	-2.47696800	-0.35955800
B	0.00000000	-2.00601300	1.12463900
B	0.00000000	-1.38650300	2.60984100
B	0.00000000	0.00000000	1.46918600
B	0.00000000	0.82890700	-0.10000900
B	0.00000000	0.00000000	-1.59323600
B	0.00000000	-0.82890700	-0.10000900

**(b) TS of  $\text{B}_{15}^+ \text{C}_{2v}$**

B	0.00000000	3.14286300	-0.38330400
B	0.00000000	2.85508000	1.10302000
B	0.00000000	1.44316400	1.89486400
B	0.00000000	0.00000000	2.51837900

B	0.00000000	-1.44316400	1.89486400
B	0.00000000	-2.85508000	1.10302000
B	0.00000000	-3.14286300	-0.38330400
B	0.00000000	-2.21793000	-1.64214700
B	0.00000000	-0.76617000	-2.32396200
B	0.00000000	0.76617000	-2.32396200
B	0.00000000	2.21793000	-1.64214700
B	0.00000000	1.52931900	0.06796100
B	0.00000000	0.00000000	0.85279500
B	0.00000000	-1.52931900	0.06796100
B	0.00000000	0.00000000	-0.80403700