

Probing the Low-Energy Structures of Aluminum-Magnesium Alloy

Clusters: A Detailed Study

Xiaodong Xing,^{ab} Jingjing Wang,^a Xiaoyu Kuang,^{*a} Xinxin Xia,^a Cheng Lu,^{†bc} George Maroulis,^{‡d}

^a Institute of Atomic and Molecular Physics, Sichuan University, Chengdu 610065, China

^b Department of Physics, Nanyang Normal University, Nanyang 473061, China

^c Department of Physics and High Pressure Science and Engineering Center, University of Nevada,
Las Vegas, Nevada 89154, United States

^d Department of Chemistry, University of Patras, GR-26500 Patras, Greece

*Correspondence author. E-mail: scu_kuang@163.com (Xiao-Yu Kuang), lucheng@calypso.cn
(Cheng Lu) and maroulis@upatras.gr (George Maroulis)

Table S1 The electronic states, symmetries, averaged binding energy (E_b , eV), and HOMO – LUMO energy gap (E_{gap} , eV) for the lowest-energy structures of neutral and anionic Al_n ($n = 3-20$) clusters.

Cluster	State	Symm.	E_b	E_{gap}	Cluster	State	Symm.	E_b	E_{gap}
Al ₃	² A ₁ '	<i>D</i> _{3h}	0.72	1.63	Al ₃ ⁻	¹ A ₁ '	<i>D</i> _{3h}	1.10	1.57
Al ₄	¹ A _g	<i>C</i> _{2h}	1.08	1.16	Al ₄ ⁻	² A _g	<i>C</i> _{2h}	1.59	1.52
Al ₅	² B ₂	<i>C</i> _{2v}	1.62	1.86	Al ₅ ⁻	¹ A ₁	<i>C</i> _{2v}	2.08	1.35
Al ₆	¹ A _g	<i>C</i> _{2h}	1.81	1.64	Al ₆ ⁻	² A _g	<i>C</i> _{2h}	2.26	1.39
Al ₇	² A ₁	<i>C</i> _{3v}	2.03	1.80	Al ₇ ⁻	¹ A ₁	<i>C</i> _{3v}	2.36	1.61
Al ₈	¹ A _g	<i>C</i> _{2h}	2.06	1.86	Al ₈ ⁻	² B _u	<i>C</i> _{2h}	2.34	1.39
Al ₉	² A'	<i>C</i> _s	2.11	1.61	Al ₉ ⁻	¹ A	<i>C</i> ₂	2.42	1.50
Al ₁₀	¹ A'	<i>C</i> _s	2.17	1.53	Al ₁₀ ⁻	² A'	<i>C</i> _s	2.44	1.50
Al ₁₁	² A	<i>C</i> ₁	2.22	1.81	Al ₁₁ ⁻	¹ A'	<i>C</i> _s	2.48	1.79
Al ₁₂	¹ A ₁	<i>C</i> _{2v}	2.28	2.00	Al ₁₂ ⁻	² A'	<i>C</i> _s	2.51	1.19
Al ₁₃	² A	<i>C</i> ₁	2.37	2.60	Al ₁₃ ⁻	¹ A _g	<i>I</i> _h	2.64	2.74
Al ₁₄	¹ A	<i>C</i> ₂	2.40	1.61	Al ₁₄ ⁻	² B	<i>C</i> ₂	2.59	1.34
Al ₁₅	² B _{3u}	<i>D</i> _{2h}	2.41	0.29	Al ₁₅ ⁻	¹ A _g	<i>D</i> _{2h}	2.59	1.66
Al ₁₆	¹ A'	<i>C</i> _s	2.43	1.60	Al ₁₆ ⁻	² A'	<i>C</i> _s	2.61	1.48
Al ₁₇	² B _{2u}	<i>D</i> _{2h}	2.45	1.19	Al ₁₇ ⁻	¹ A _g	<i>D</i> _{2h}	2.62	1.40
Al ₁₈	¹ A'	<i>C</i> _s	2.46	1.62	Al ₁₈ ⁻	² A	<i>C</i> ₁	2.60	1.01
Al ₁₉	² A	<i>C</i> ₁	2.44	0.97	Al ₁₉ ⁻	¹ A	<i>C</i> ₁	2.59	1.23
Al ₂₀	¹ A	<i>C</i> ₁	2.50	1.55	Al ₂₀ ⁻	² A	<i>C</i> ₁	2.64	1.55

Table S2 The electronic states, symmetries, averaged binding energy (E_b , eV), and HOMO – LUMO energy gap (E_{gap} , eV) for the lowest-energy structures of neutral and anionic Al_nMg ($n = 3-20$) clusters.

Cluster	State	Symm.	E_b	E_{gap}	Cluster	State	Symm.	E_b	E_{gap}
Al_3Mg	$^2A''$	C_s	1.09	1.56	Al_3Mg^-	3A_1	C_{3v}	1.52	1.42
Al_4Mg	1A_1	C_{4v}	1.38	1.81	Al_4Mg^-	2A	C_2	1.61	1.44
Al_5Mg	$^2A''$	C_s	1.52	1.70	Al_5Mg^-	$^1A'$	C_s	1.91	1.47
Al_6Mg	1A_1	C_{3v}	1.85	2.60	Al_6Mg^-	$^2A'$	C_s	2.12	1.38
Al_7Mg	$^2A''$	C_s	1.87	1.56	Al_7Mg^-	$^1A'$	C_1	2.13	1.55
Al_8Mg	$^3A''$	C_s	1.94	1.67	Al_8Mg^-	2A	C_1	2.22	1.49
Al_9Mg	$^2A''$	C_s	2.01	1.41	Al_9Mg^-	$^1A'$	C_s	2.27	1.41
$Al_{10}Mg$	$^1A'$	C_s	2.06	1.51	$Al_{10}Mg^-$	2A	C_1	2.30	1.24
$Al_{11}Mg$	$^2A'$	C_s	2.13	1.31	$Al_{11}Mg^-$	1A	C_1	2.37	1.85
$Al_{12}Mg$	1A_1	C_{5v}	2.20	1.19	$Al_{12}Mg^-$	2A_1	C_{5v}	2.46	1.52
$Al_{13}Mg$	$^2A'$	C_s	2.31	1.58	$Al_{13}Mg^-$	$^1A'$	C_s	2.49	1.61
$Al_{14}Mg$	$^1A'$	C_s	2.31	1.79	$Al_{14}Mg^-$	$^2A'$	C_s	2.48	1.54
$Al_{15}Mg$	$^2A'$	C_s	2.32	1.43	$Al_{15}Mg^-$	$^1A'$	C_s	2.50	1.62
$Al_{16}Mg$	$^1A'$	C_s	2.36	1.35	$Al_{16}Mg^-$	$^2A'$	C_s	2.53	1.38
$Al_{17}Mg$	2A	C_1	2.35	1.15	$Al_{17}Mg^-$	1A	C_1	2.51	1.61
$Al_{18}Mg$	1A	C_1	2.36	1.75	$Al_{18}Mg^-$	$^2A'$	C_s	2.50	1.41
$Al_{19}Mg$	2A	C_1	2.41	1.36	$Al_{19}Mg^-$	1A	C_1	2.56	1.85
$Al_{20}Mg$	1A	C_1	2.40	1.20	$Al_{20}Mg^-$	2A	C_1	2.54	1.29

Table S3 Electron Density ($\rho(r_{\text{BCP}})$), Laplacian ($\nabla^2\rho(r_{\text{BCP}})$), Bond Ellipticity (ε), and Curvature λ_3 at Bond Critical Points (BCP) for Mg-Al bond in the lowest-energy Al_nMg ($n = 3\text{-}20$) clusters.

		ρ / a.u.	$\nabla^2\rho$ / a.u.	ε	λ_3 / a.u.
Al_3Mg	Mg4-Al1	0.042	-0.025	0.376	0.010
Al_4Mg	Mg5-Al1	0.025	0.002	3.081	0.006
	Mg5-Al2	0.025	0.002	3.081	0.006
Al_5Mg	Mg1-Al3	0.024	0.013	1.001	0.022
	Mg1-Al5	0.024	0.013	1.001	0.022
Al_6Mg	Mg7-Al2	0.025	0.019	0.148	0.037
	Mg7-Al4	0.025	0.019	0.148	0.037
	Mg7-Al5	0.025	0.019	0.148	0.037
Al_7Mg	Mg8-Al6	0.024	0.030	0.194	0.043
	Mg8-Al7	0.025	0.024	0.250	0.037
Al_8Mg	Mg1-Al2	0.023	0.023	3.128	0.031
	Mg1-Al3	0.023	0.023	3.128	0.031
	Mg1-Al5	0.023	0.027	1.795	0.036
	Mg1-Al4	0.026	0.028	0.170	0.046
Al_9Mg	Mg1-Al2	0.024	0.023	0.726	0.036
	Mg1-Al3	0.024	0.023	0.726	0.036
	Mg1-Al4	0.027	0.027	0.197	0.050
Al_{10}Mg	Mg1-Al2	0.024	0.026	1.209	0.033
	Mg1-Al3	0.025	0.026	0.542	0.043
	Mg1-Al4	0.025	0.028	0.531	0.038
	Mg1-Al5	0.025	0.026	0.542	0.043
Al_{11}Mg	Mg12-Al2	0.023	0.027	0.660	0.032
	Mg12-Al4	0.023	0.021	1.412	0.026
	Mg12-Al6	0.023	0.023	2.021	0.031
	Mg12-Al7	0.023	0.023	2.021	0.031
	Mg12-Al10	0.023	0.021	1.412	0.026
Al_{12}Mg	Mg2-Al1	0.030	0.055	0.000	0.072
Al_{13}Mg	Mg14-Al5	0.024	0.032	0.590	0.045
	Mg14-Al6	0.023	0.024	0.307	0.032
	Mg14-Al8	0.023	0.033	1.819	0.039
	Mg14-Al13	0.022	0.024	0.307	0.032
Al_{14}Mg	Mg15-Al12	0.023	0.032	0.079	0.037
Al_{15}Mg	Mg16-Al4	0.023	0.031	0.140	0.045
	Mg16-Al7	0.022	0.017	0.000	0.027
Al_{16}Mg	Mg17-Al14	0.021	0.022	1.404	0.025
	Mg17-Al15	0.022	0.032	0.754	0.039
	Mg17-Al16	0.019	0.017	0.135	0.029
Al_{17}Mg	Mg18-Al12	0.024	0.029	0.167	0.051
	Mg18-Al17	0.026	0.031	0.077	0.056
	Mg18-Al13	0.026	0.031	0.083	0.058

Al ₁₈ Mg	Mg19-Al6	0.020	0.025	3.494	0.032
	Mg19-Al11	0.021	0.013	1.839	0.018
Al ₁₉ Mg	Mg20-Al4	0.021	0.025	5.011	0.033
	Mg20-Al5	0.021	0.025	5.194	0.033
	Mg20-Al11	0.022	0.020	2.583	0.030
	Mg20-Al12	0.022	0.020	2.561	0.030
Al ₂₀ Mg	Mg21-Al12	0.021	0.020	6.452	0.030
	Mg21-Al15	0.021	0.021	7.193	0.031
	Mg21-Al11	0.025	0.023	0.272	0.045
	Mg21-Al20	0.022	0.026	8.654	0.038

Table S4 Electron Density ($\rho(r_{\text{BCP}})$), Laplacian ($\nabla^2\rho(r_{\text{BCP}})$), Bond Ellipticity (ε), and Curvature λ_3 at Bond Critical Points (BCP) for Mg-Al bond in the lowest-energy Al_nMg^- ($n = 3\text{-}20$) clusters.

		ρ / a.u.	$\nabla^2\rho$ / a.u.	ε	λ_3 / a.u.
Al_3Mg^-	Mg4-Al3	0.026	0.011	0.000	0.018
Al_4Mg^-	Mg5-Al1	0.025	0.018	1.276	0.028
	Mg5-Al3	0.025	0.018	1.276	0.028
Al_5Mg^-	Mg6-Al1	0.023	0.013	0.705	0.023
	Mg6-Al3	0.023	0.013	0.705	0.023
Al_6Mg^-	Mg7-Al2	0.024	0.020	0.570	0.033
	Mg7-Al4	0.024	0.020	0.570	0.033
	Mg7-Al5	0.025	0.022	0.208	0.041
Al_7Mg^-	Mg1-Al2	0.026	0.026	0.182	0.049
	Mg1-Al3	0.026	0.026	0.182	0.049
Al_8Mg^-	Mg1-Al4	0.026	0.029	0.002	0.047
	Mg1-Al5	0.024	0.029	0.937	0.040
Al_9Mg^-	Mg1-Al2	0.026	0.032	0.232	0.053
	Mg1-Al3	0.026	0.032	0.232	0.053
	Mg1-Al4	0.024	0.025	0.225	0.040
$\text{Al}_{10}\text{Mg}^-$	Mg1-Al3	0.024	0.024	0.506	0.042
	Mg1-Al4	0.021	0.020	12.900	0.023
	Mg1-Al5	0.023	0.023	0.567	0.040
$\text{Al}_{11}\text{Mg}^-$	Mg1-Al2	0.026	0.024	0.247	0.049
	Mg1-Al5	0.026	0.031	0.146	0.052
$\text{Al}_{12}\text{Mg}^-$	Mg2-Al1	0.026	0.044	0.000	0.055
$\text{Al}_{13}\text{Mg}^-$	Mg14-Al5	0.024	0.034	1.633	0.045
	Mg14-Al8	0.024	0.037	0.669	0.046
$\text{Al}_{14}\text{Mg}^-$	Mg15-Al12	0.023	0.034	0.175	0.041
$\text{Al}_{15}\text{Mg}^-$	Mg16-Al14	0.024	0.031	0.153	0.048
	Mg16-Al9	0.022	0.020	1.854	0.028
	Mg16-Al10	0.022	0.020	1.854	0.028
$\text{Al}_{16}\text{Mg}^-$	Mg17-Al15	0.022	0.035	0.283	0.041
	Mg17-Al16	0.020	0.012	0.772	0.017
$\text{Al}_{17}\text{Mg}^-$	Mg18-Al2	0.024	0.029	0.175	0.051
	Mg18-Al7	0.026	0.030	0.119	0.054
	Mg18-Al13	0.025	0.031	0.135	0.055
$\text{Al}_{18}\text{Mg}^-$	Mg19-Al6	0.021	0.025	0.558	0.035
	Mg19-Al11	0.023	0.021	0.140	0.041
	Mg19-Al18	0.021	0.025	0.558	0.035
$\text{Al}_{19}\text{Mg}^-$	Mg20-Al11	0.022	0.022	1.352	0.034
	Mg20-Al16	0.020	0.024	2.892	0.033
	Mg20-Al19	0.021	0.024	8.405	0.033
$\text{Al}_{20}\text{Mg}^-$	Mg21-Al12	0.022	0.023	1.790	0.037
	Mg21-Al11	0.024	0.019	0.267	0.039

Mg21-Al20	0.023	0.031	1.944	0.046
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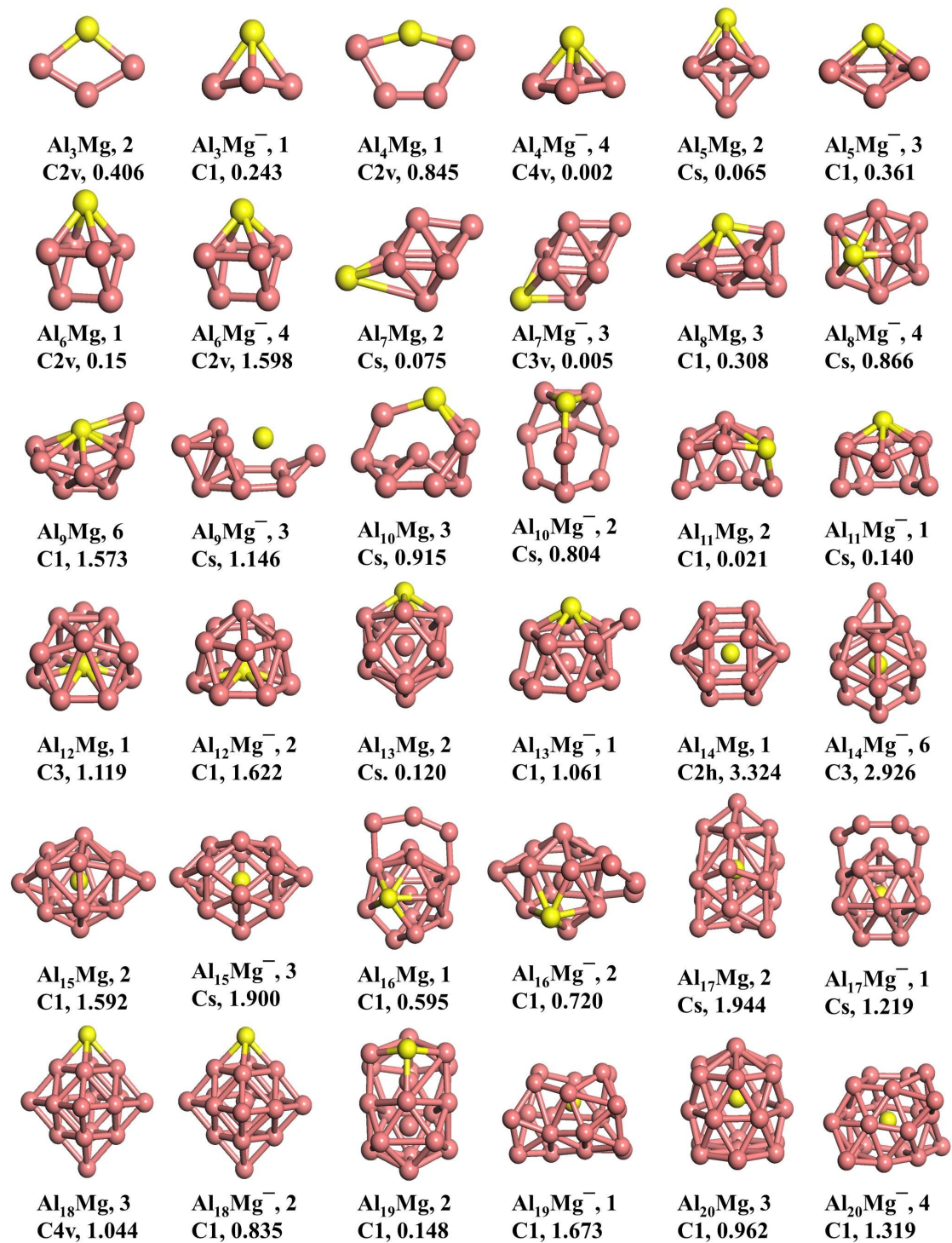


Fig S1 The metastable isomers of neutral and anionic Al_nMg ($n = 4-20$) clusters, together with spin multiplicity, point symmetry and relative energies.