

Structure and stability of clusters of β -alanine in the gas phase: importance of the nature of intermolecular interactions.

Electronic Supplementary Information.

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1 Thermostats

The input files to run molecular dynamic (MD) simulations with AMBER ¹⁻⁴ were prepared using antechamber tools.⁵ General Amber force field⁶ were used with RESP charges⁷ parametrized at the HF/6-31G* level of theory with the Gaussian09 program.⁸ Energy minimization was carried out to remove the possible non-physical, accidental contacts after parameterizing. Then, different thermostats were tested in order to obtain physically meaningful results. For each thermostat the different parameters were converged at each stage of the MD simulation. First, the system was heated from T=0K to the target temperature and then propagated at this temperature. Three different thermostats were checked: Berendsen,⁹ Andersen¹⁰ and Langevin.¹¹ The best results were obtained using the Berendsen thermostat for the heating stage and Langevin thermostat for the production dynamics. However, for both thermostats the results were unsatisfying since we observed high oscillations in energy and temperature and a further extensive benchmark study for thermal equilibration was performed.

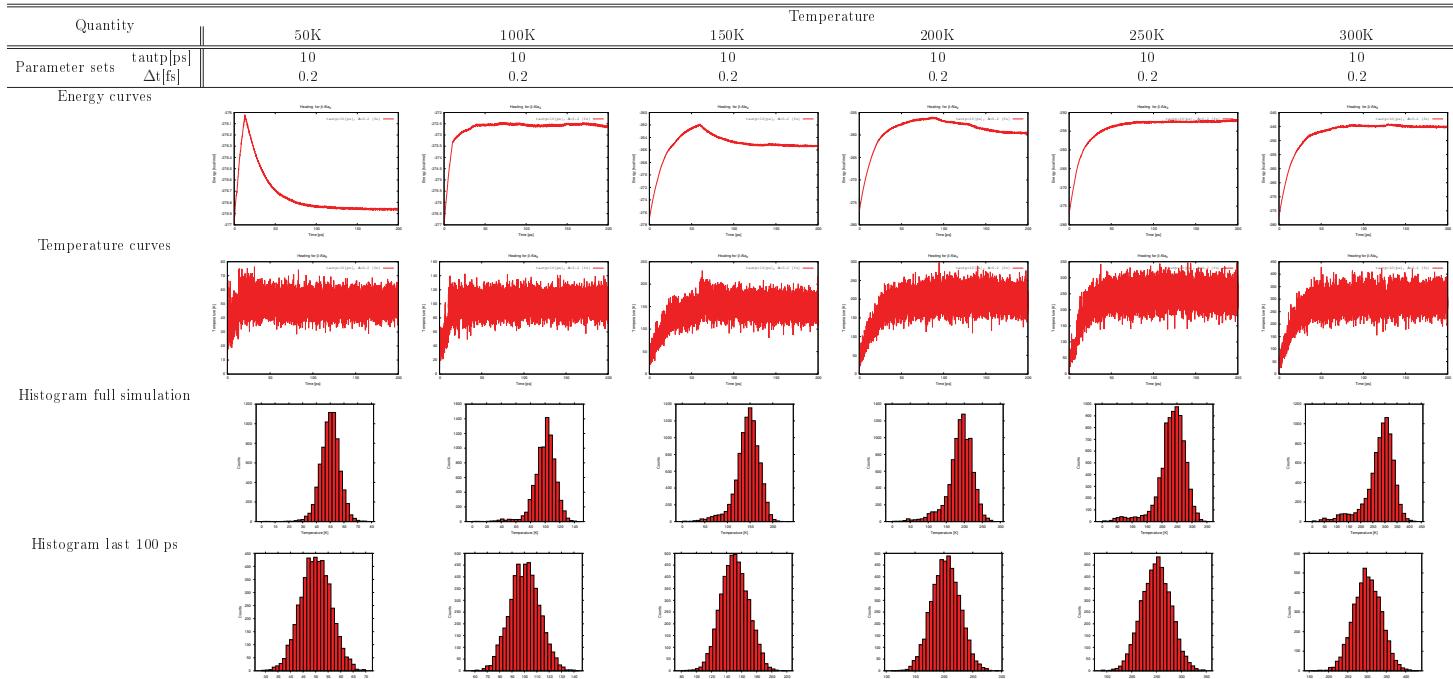
1.1 Berendsen thermostat convergence

Firstly, the conditions for the Berendsen thermostat were optimized. We performed an extensive study to choose the best set of parameters: time step, Δt (fs), and temperature coupling parameter, tautp (ps), by using the Berendsen thermostat for all clusters sizes consider in the manuscript. To

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this, during the heating stage from $T=0K$ to $T=(50, 100, 150, 200, 250, 300)K$ we checked all combination for $\text{tautp}=(0.5, 1, 1.5, 2, 2.5, 3, 5, 10, 15, 20, 25, 50, 100, 150, 200 \text{ and } 250 \text{ picoseconds})$ and $\Delta t=(0.0001, 0.0002, 0.0003, 0.0004, 0.0005, 0.0006, 0.0007, 0.0008, 0.0009 \text{ and } 0.001 \text{ fs})$; over 5000 simulations. After analyzing the simulations we concluded that $\text{tautp}=10 \text{ ps}$ and $\Delta t=0.2 \text{ fs}$ are the most appropriate parameters, since the temperature is well equilibrated for each cluster size and for each excitation energy during the propagation stage. The plots for each cluster size and temperature with the chosen parameters are presented in Tables 1-4.



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Table 1: Parametrization using Berendsen thermostat for $(\beta\text{-Ala})_2$

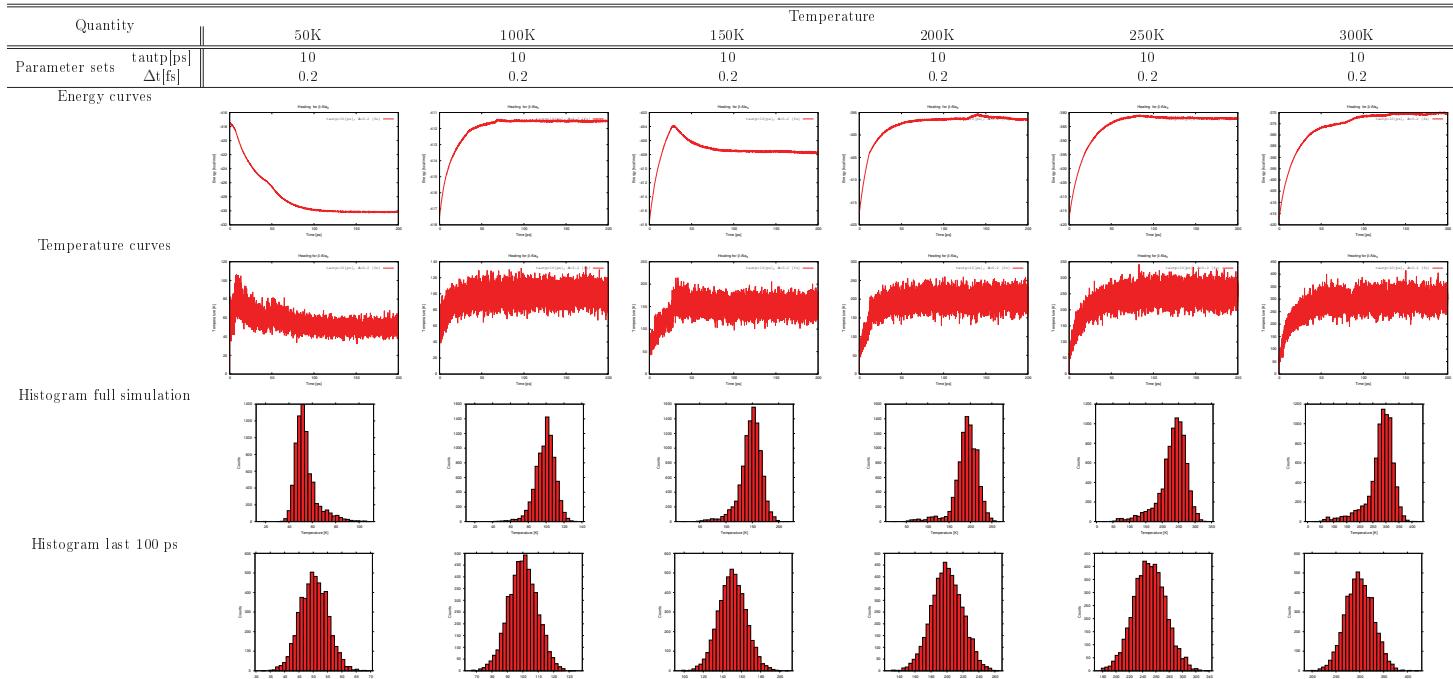
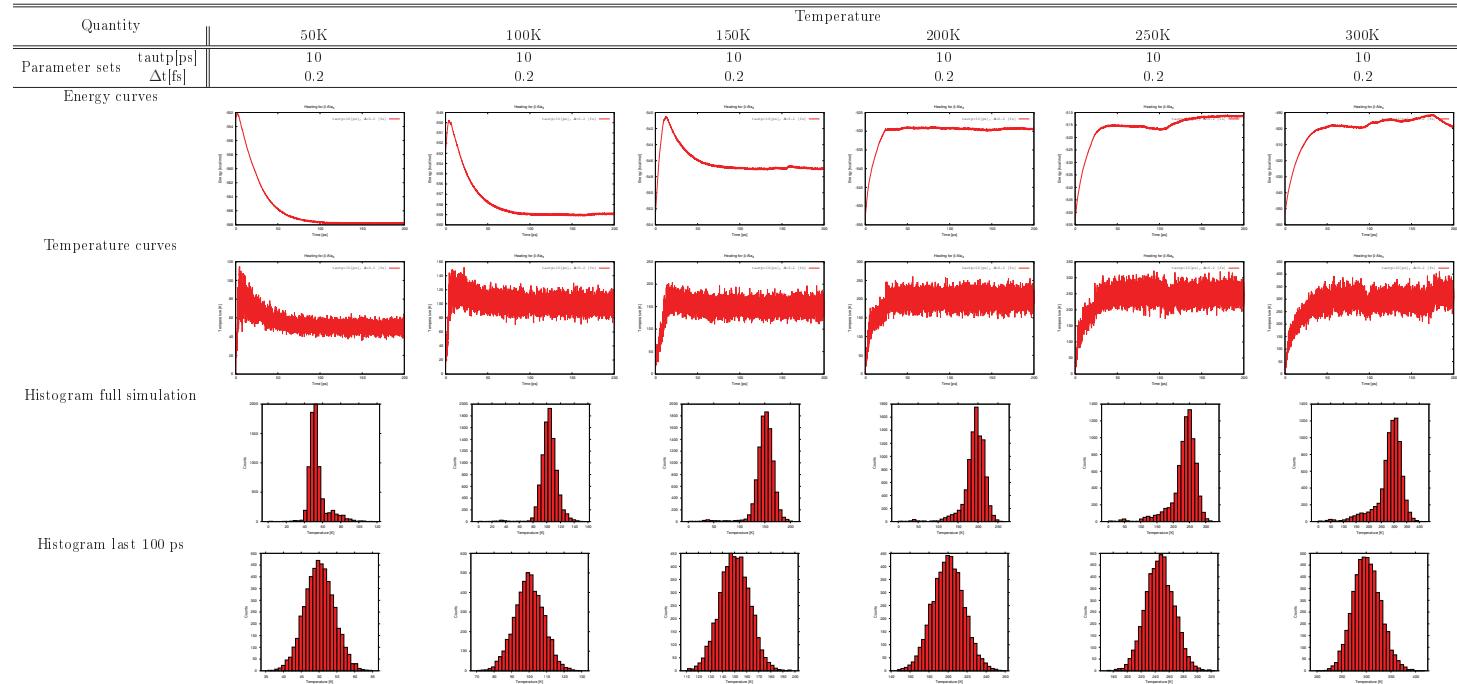


Table 2: Parametrization using Berendsen thermostat for $(\beta\text{-Ala})_3$



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Table 3: Parametrization using Berendsen thermostat for $(\beta\text{-Ala})_4$

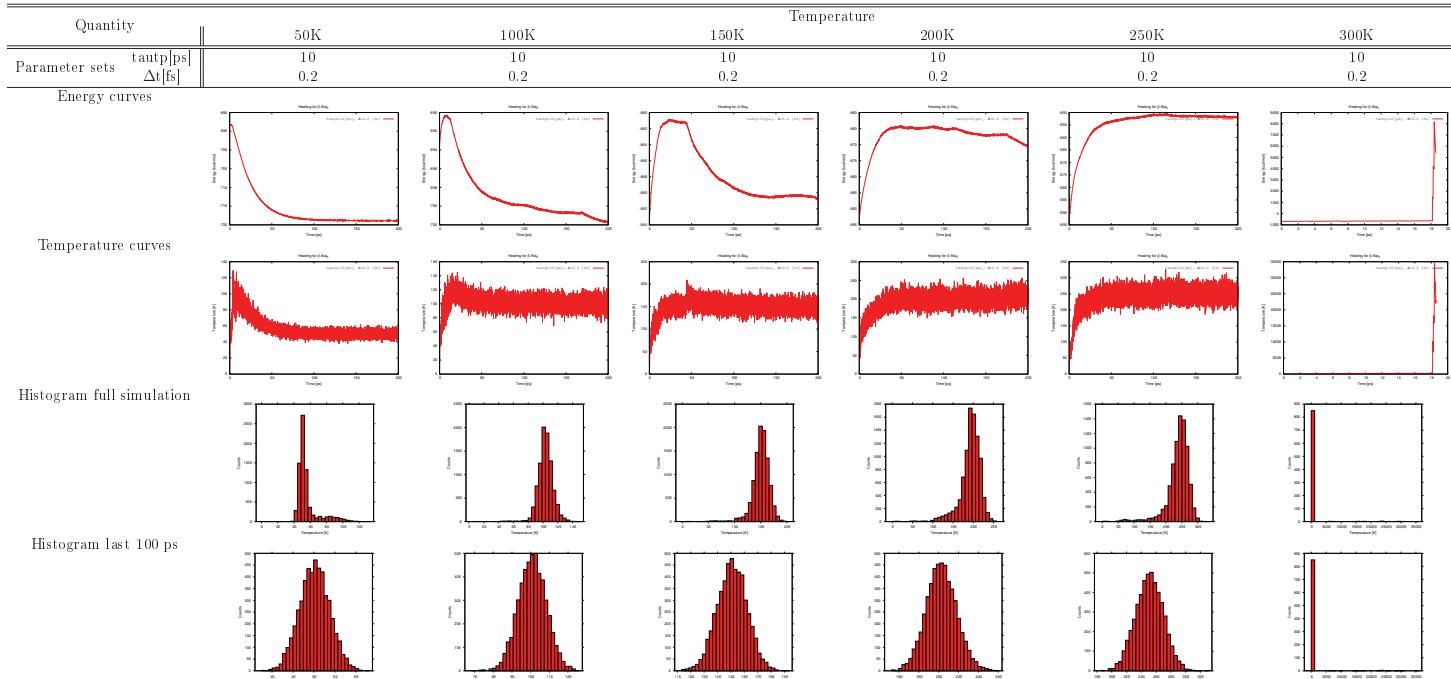
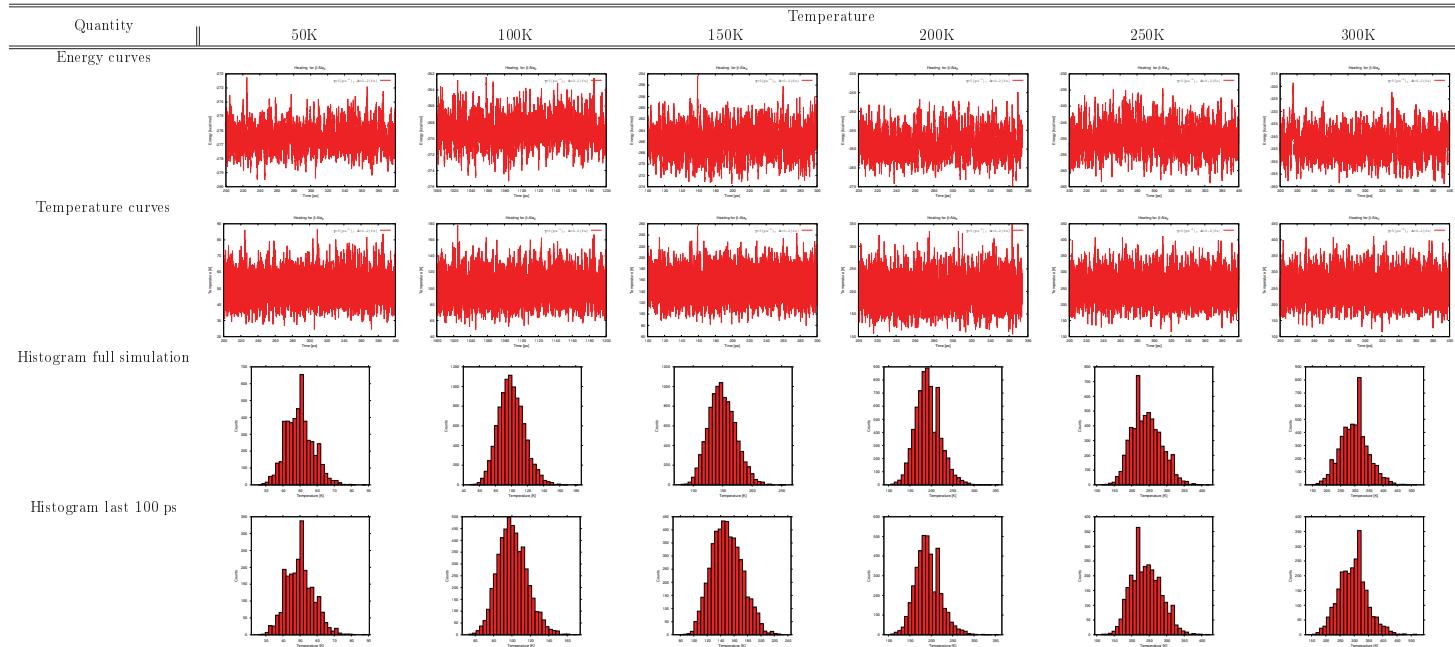


Table 4: Parametrization using Berendsen thermostat for $(\beta\text{-Ala})_5$ For 300K cluster is not stable, it thermally breaks.

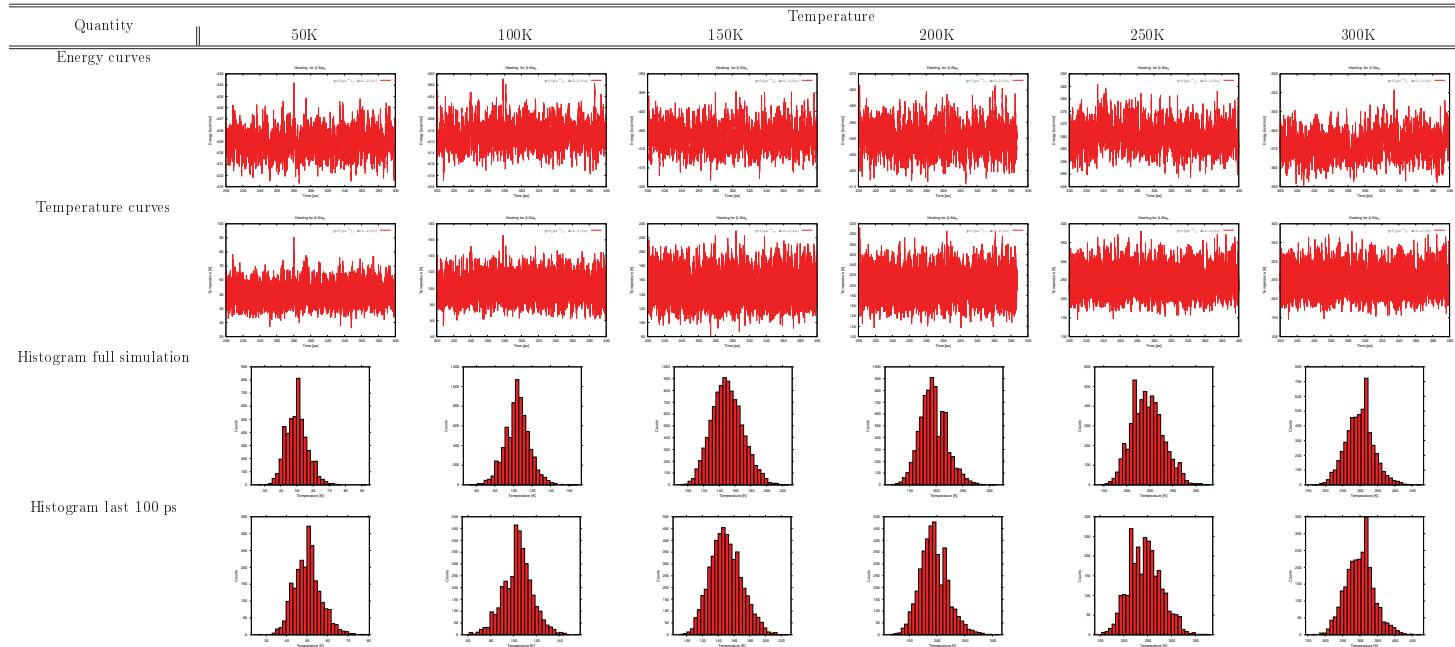
1.2 Langevin thermostat convergence

Secondly, we optimized the conditions for the Langevin thermostat. We performed an extensive study to choose the best set of parameters: time step, Δt (fs), and the collision frequency, γ (ps^{-1}). For the Langevin thermostat we considered the same cluster sizes and temperature values as for the Berendsen thermostat. Simulations were performed with $\gamma=(1, 2, 3, 4, 5, 10, 20, 25, 50, 60, 70, 80, 90, 100 \text{ ps}^{-1})$ and $\Delta t=(0.1, 0.2, \dots, 1.5, 2.0 \text{ fs})$. After these simulations we concluded that $\gamma=5 \text{ ps}^{-1}$ (weak coupling to approximate the micro-canonical ensemble, NVE) and $\Delta t=0.2 \text{ fs}$ are the most appropriate parameters, where the energy and the temperature are well equilibrated for each cluster size and for each temperature during the propagation stage. The plots for each cluster size and temperature with the chosen parameters are presented in Tables 5-8.



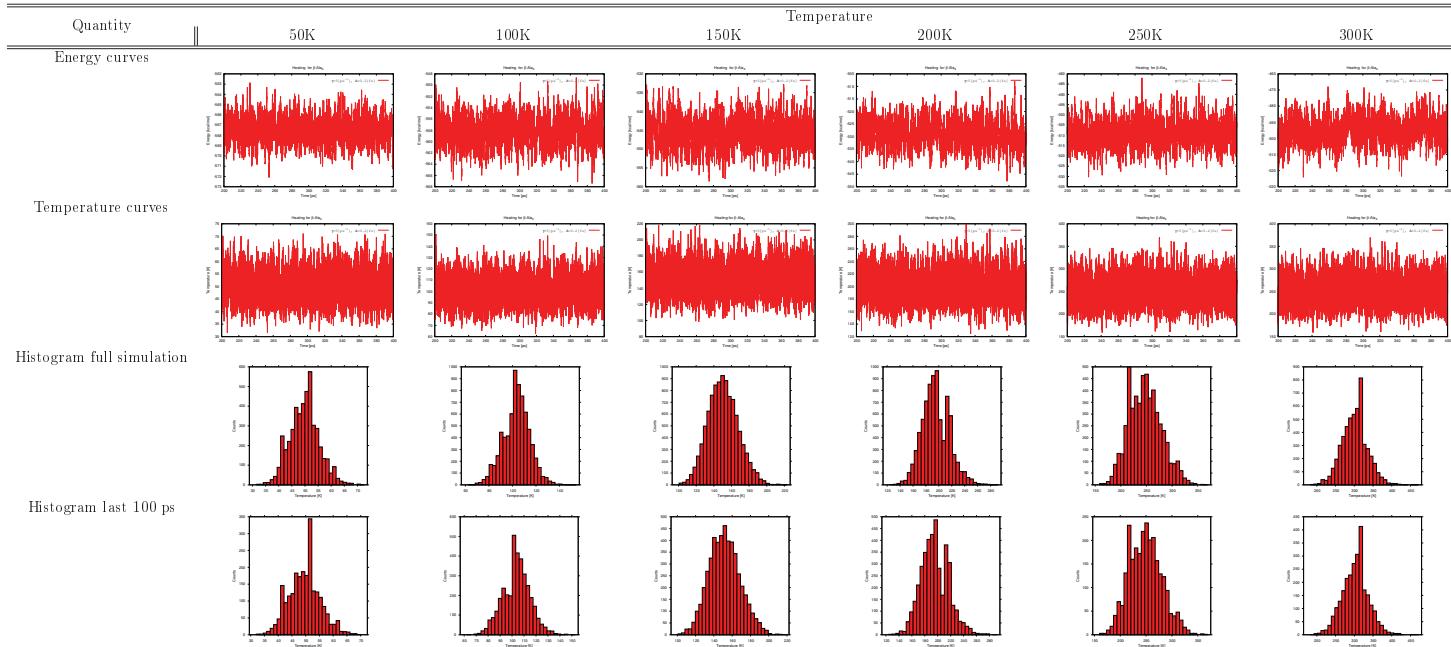
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Table 5: Parametrization using Langevin thermostat for $(\beta\text{-Ala})_2$. Parameters for each temperature are: $\gamma=5 \text{ ps}^{-1}$ and $\Delta t=0.2 \text{ fs}$.



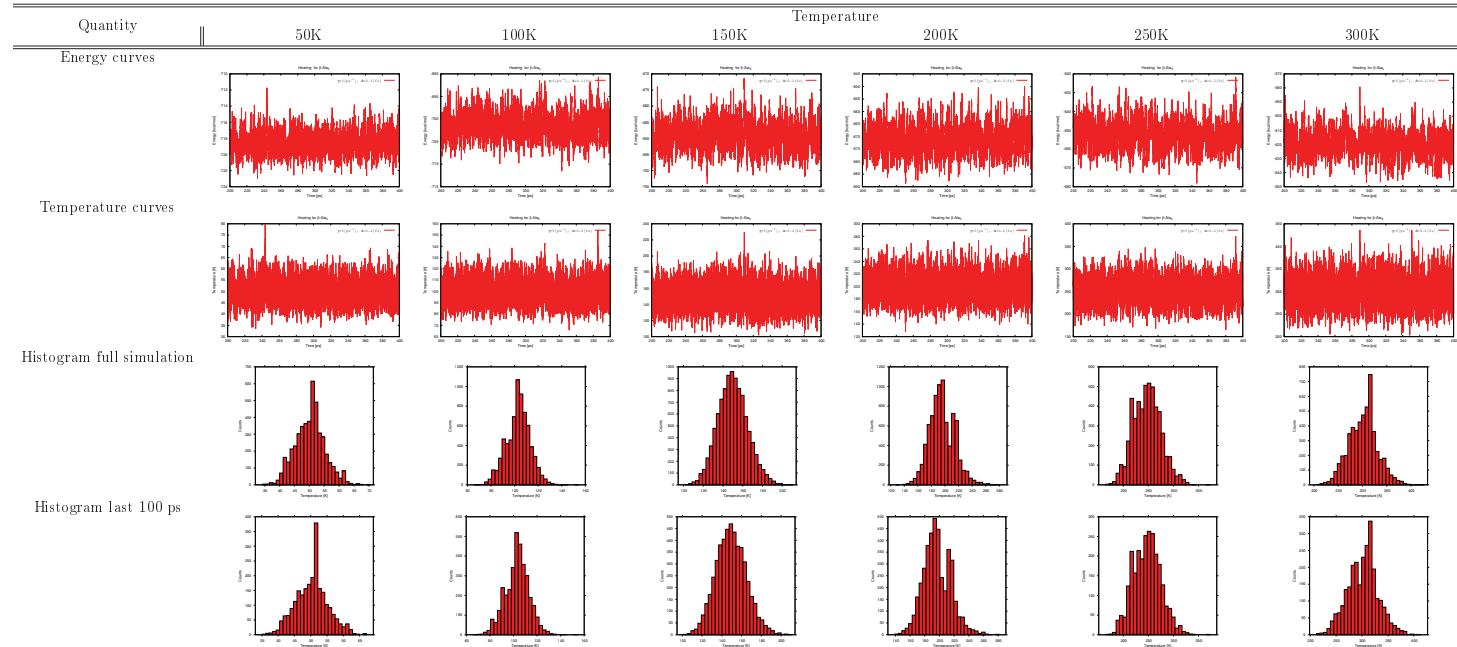
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Table 6: Parametrization using Langevin thermostat for $(\beta\text{-Ala})_3$. Parameters for each temperature are: $\gamma=5 \text{ ps}^{-1}$ and $\Delta t=0.2 \text{ fs}$.



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Table 7: Parametrization using Langevin thermostat for $(\beta\text{-Ala})_4$. Parameters for each temperature are: $\gamma=5 \text{ ps}^{-1}$ and $\Delta t=0.2 \text{ fs}$.



11

Table 8: Parametrization using Langevin thermostat for $(\beta\text{-Ala})_5$. Parameters for each temperature are: $\gamma=5 \text{ ps}^{-1}$ and $\Delta t=0.2 \text{ fs}$.

1.3 Summary of the thermostats convergence

A large set of various parameters to run classical molecular dynamics simulations for both processes heating and propagation were considered. After the evaluation of these parameters we obtained the most stable ones for each temperature at the heating and production stages, using the Berendsen and Langevin thermostats, respectively. We checked that the total energy and temperature do not fluctuate as a function of time to be sure that system is well equilibrated. Some slight deviations in the temperature are observed due to the hydrogen bonds creation and annihilation, and due to van der Waals interactions.

2 Benchmarking

The benchmarking study has been carried out evaluating geometries, relative energies and bonding properties. Table 9 presents differences in the geometries obtained with the MP2 method and with each of the considered functionals: B3LYP, dispersion corrected B97D, M06 and its variation M06-2X and MPWB1K in combination with the 6-311++G(d,p) basis set. Benchmarking of some electron properties in the bond critical points (BCPs) of H bonds for the most stable dimer (2.1) are presented in Table 10. Figure 1 presents a general comparison of the relative energies of 19 conformers of dimers after geometry optimization with the MP2 method and all considered DFT functionals. Single point energies at the CCSD(T)/6-311++G(d,p) level of theory were obtained from geometries optimised at MP2 level of theory for the most stable 11 conformers. Figure 2 shows benchmarking of the relative energies computed with the DFT functionals and their correlation with the MP2 and CCSD(T) methods. Almost complete energetic similarity measured with the Pearson coefficient is found for the M06-2X functional in comparison with MP2 or CCSD(T).

Table 9: Root mean square deviations, $RMSD$ in Å, for the structures in $(\beta - ala)_2$ calculated for each considered functional with respect to the MP2 results. The biggest and the smallest values of $RMSD$ are highlighted in bold.

Conformer	B3LYP	B97D	M06	M06-2X	MPWB1K
2.1	0.08	0.04	0.04	0.05	0.05
2.2	0.13	0.11	0.17	0.13	0.13
2.3	0.10	0.09	0.12	0.13	0.13
2.4	0.14	0.11	0.25	0.29	0.25
2.5	0.28	0.26	0.31	0.32	0.31
2.6	0.12	0.12	0.35	0.25	0.30
2.7	0.19	0.18	0.34	0.14	0.25
2.8	0.08	0.12	0.12	0.10	0.08
2.9	0.87	0.73	0.82	0.16	0.85
2.10	0.16	0.05	0.09	0.06	0.07
2.11	0.45	0.05	0.17	0.09	0.08
2.12	0.54	0.10	0.13	0.12	0.13
2.13	0.56	0.11	0.08	0.06	0.14
2.14	0.07	0.05	0.03	0.04	0.04
2.15	0.22	0.16	0.11	0.17	0.25
2.16	0.10	0.09	0.08	0.17	0.09
2.17	0.06	0.05	0.03	0.03	0.04
2.18	0.70	0.11	0.19	0.10	0.10
2.19	0.44	0.21	0.06	0.22	0.46
Average	0.28	0.14	0.18	0.14	0.20

Table 10: Electron density and its Laplacian computed for the most stable conformer of $(\beta - ala)_2$ at the bond critical points BCP1 and BCP2 (see bonds labels in the main text).

	MP2	B3LYP	B97D	M06	M06-2X	MPWB1K
ρ (BCP1)	0.050	0.050	0.052	0.049	0.050	0.049
ρ (BCP2)	0.050	0.050	0.052	0.049	0.050	0.049
$\nabla^2\rho$ (BCP1)	0.100	0.100	0.093	0.108	0.100	0.104
$\nabla^2\rho$ (BCP2)	0.100	0.100	0.093	0.108	0.100	0.104

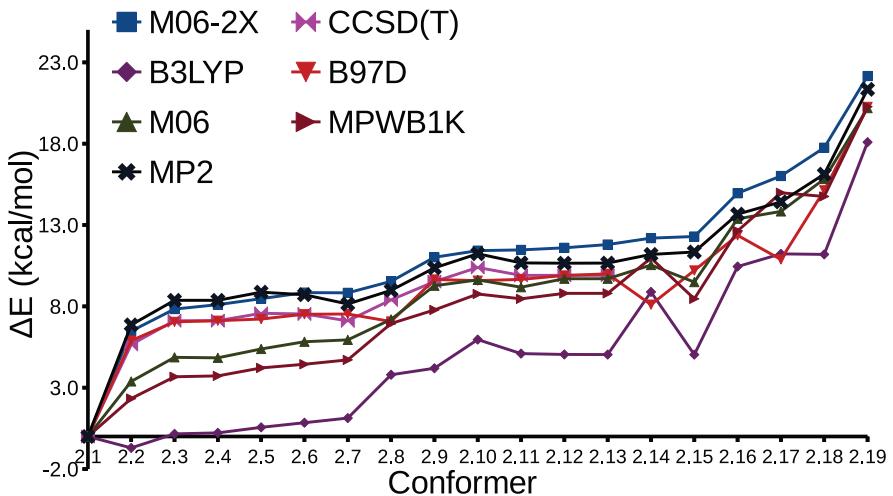


Figure 1: Benchmarking of 19 conformers of $(\beta - ala)_2$: relative stability between all conformers at the different levels of theory that we considered; Relative energies are given in kcal mol^{-1} with respect to the most stable conformer.

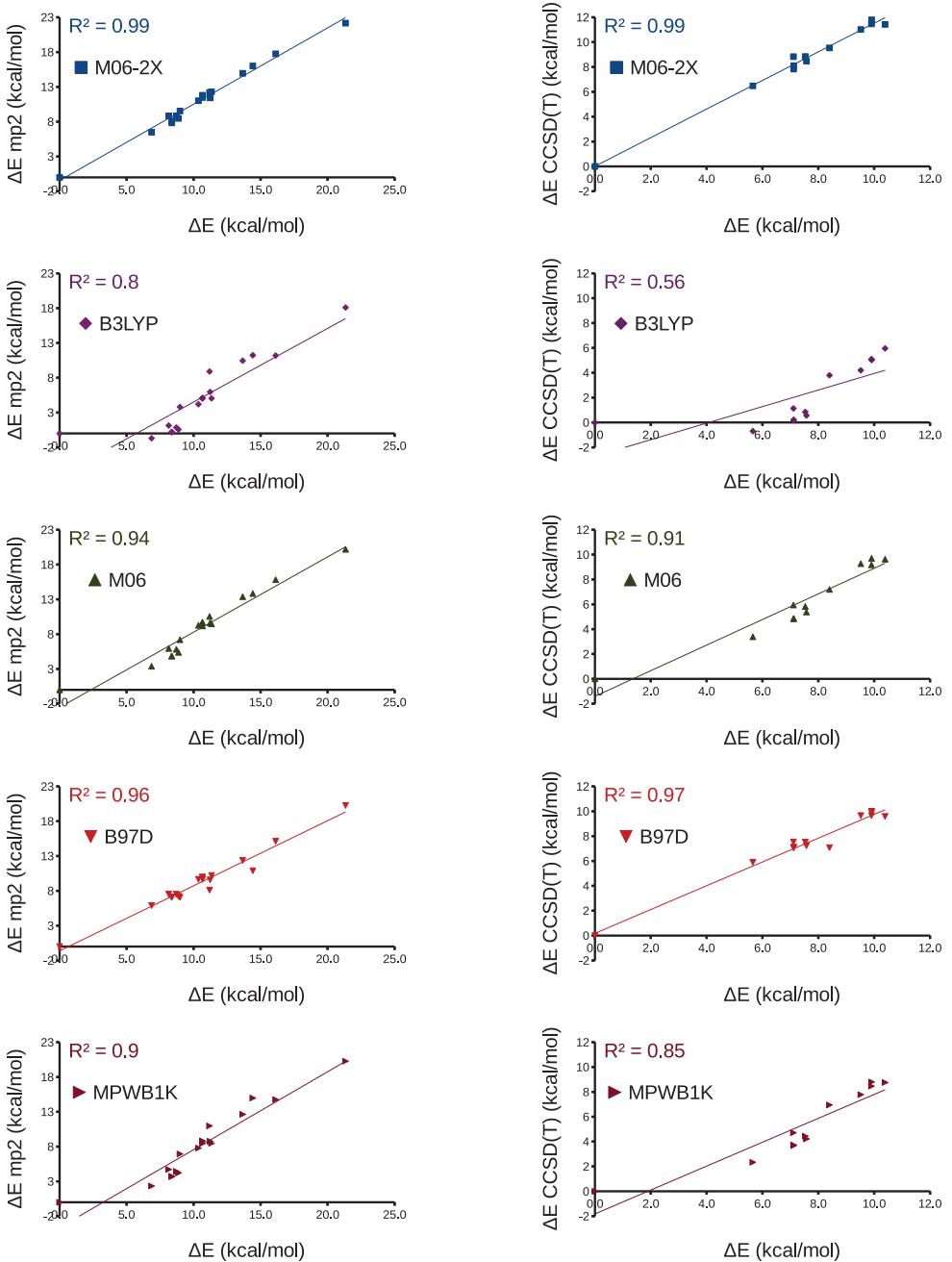


Figure 2: Benchmarking of 19 and 11 conformers of $(\beta\text{-}ala)_2$: correlations of the different functionals with the MP2 and CCSD(T) results, respectively. R is the Pearson correlation coefficient. Relative energies are given in kcal mol^{-1} with respect to the most stable conformer (see all structures in the Figure 4).

3 Isomers

Using the computational strategy described in the main manuscript and employing the M06-2X functional with the 6-311++G(d,p) basis set we evaluated the relative stability of numerous isomers (m) of different cluster sizes (n). We use the nomenclature (n,m), e.g. conformer 3.9 is the ninth conformer of a cluster with three beta-alanine residues. A complete study of the isomers of neutral β -alanine molecules is presented in Figures 3-10. We present the optimized geometries, stabilized mainly through hydrogen bonds, and their relative energies. The monomers were obtained after reoptimization of geometries taken from a previous study.¹²

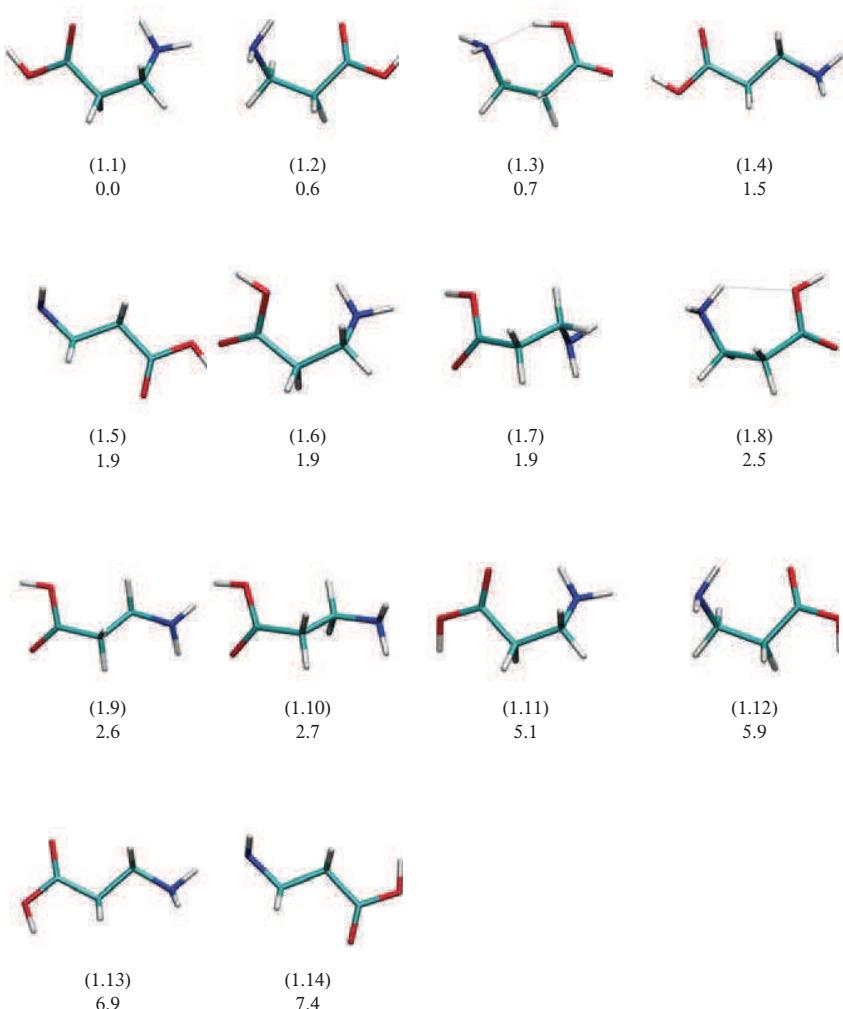


Figure 3: Optimized geometries of neutral monomers (1.1-1.14) of β -alanine at the DFT-M06-2X/6-311++G(d,p) level of theory. Relative energies with respect to the most stable neutral monomer (1.1) in kcal mol⁻¹.

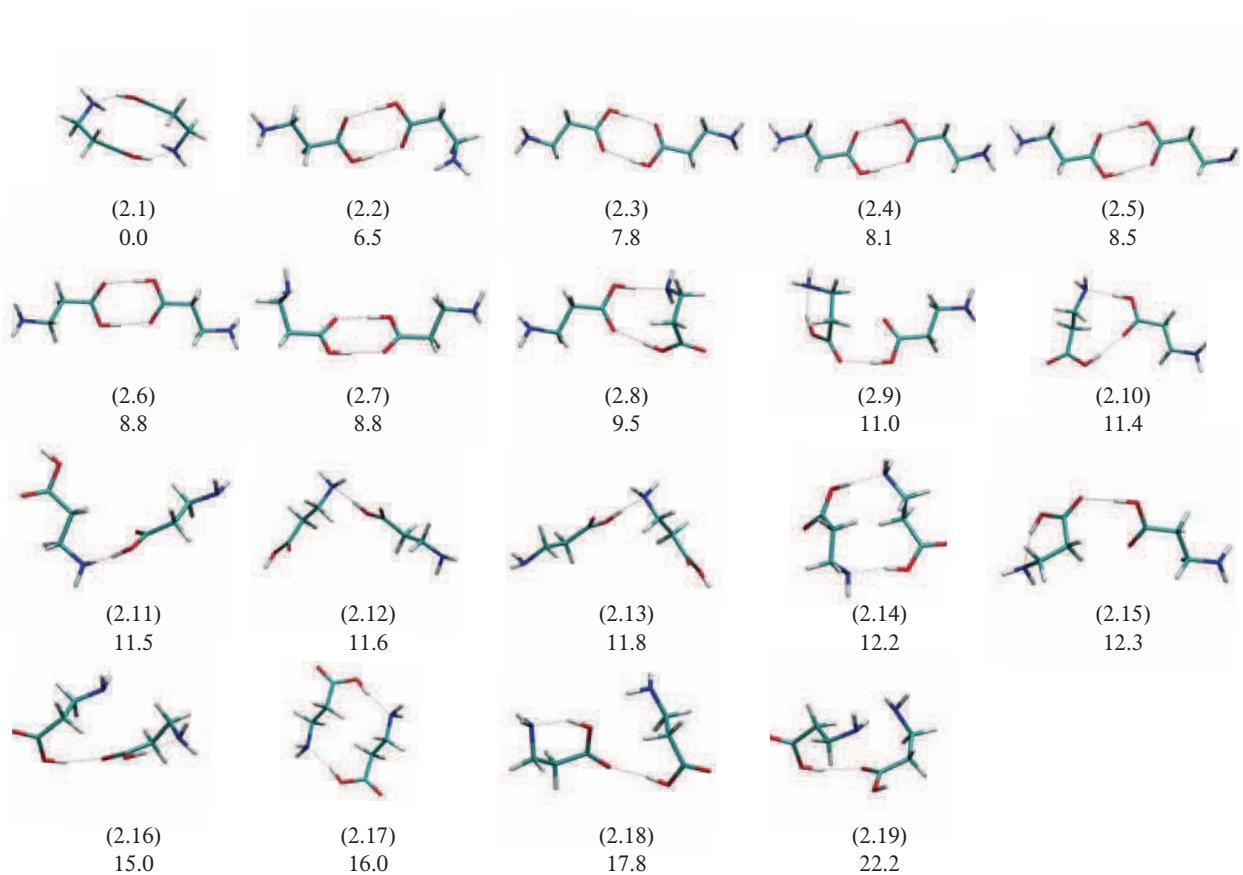


Figure 4: Optimized geometries of neutral dimers (2.1-2.19) of β -alanine at the DFT-M06-2X/6-311++G(d,p) level of theory. Relative energies with respect to the most stable neutral dimer (2.1) in kcal mol⁻¹. Dashed lines shows hydrogen (H) bonds with donor (D)-acceptor (A) atoms with the cut-off distance ≤ 3.2 and D-H-A angle ≤ 50 degree.¹³ The colors of hydrogen bond: red, blue and turquoise underline the donor atom: oxygen, nitrogen and carbon, respectively.

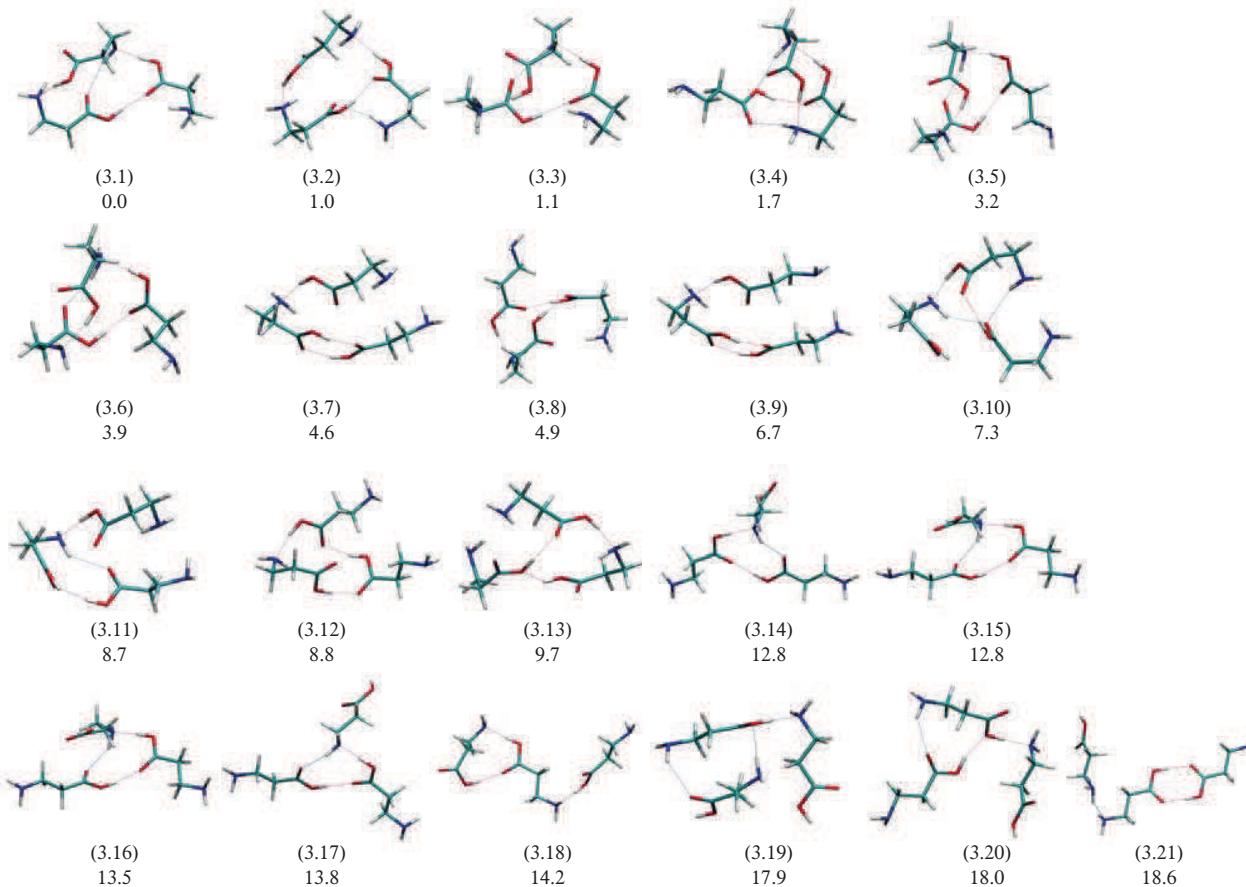


Figure 5: Optimized geometries of neutral trimers (3.1-3.21) of β -alanine at the DFT-M06-2X/6-311++G(d,p) level of theory. Relative energies with respect to the most stable neutral trimer (3.1) in kcal mol⁻¹. Dashed lines shows hydrogen (H) bonds with donor (D)-acceptor (A) atoms with the cut-off distance ≤ 3.2 and D-H-A angle ≤ 50 degree.¹³ The colors of hydrogen bond: red, blue and turquoise underline the donor atom: oxygen, nitrogen and carbon, respectively.

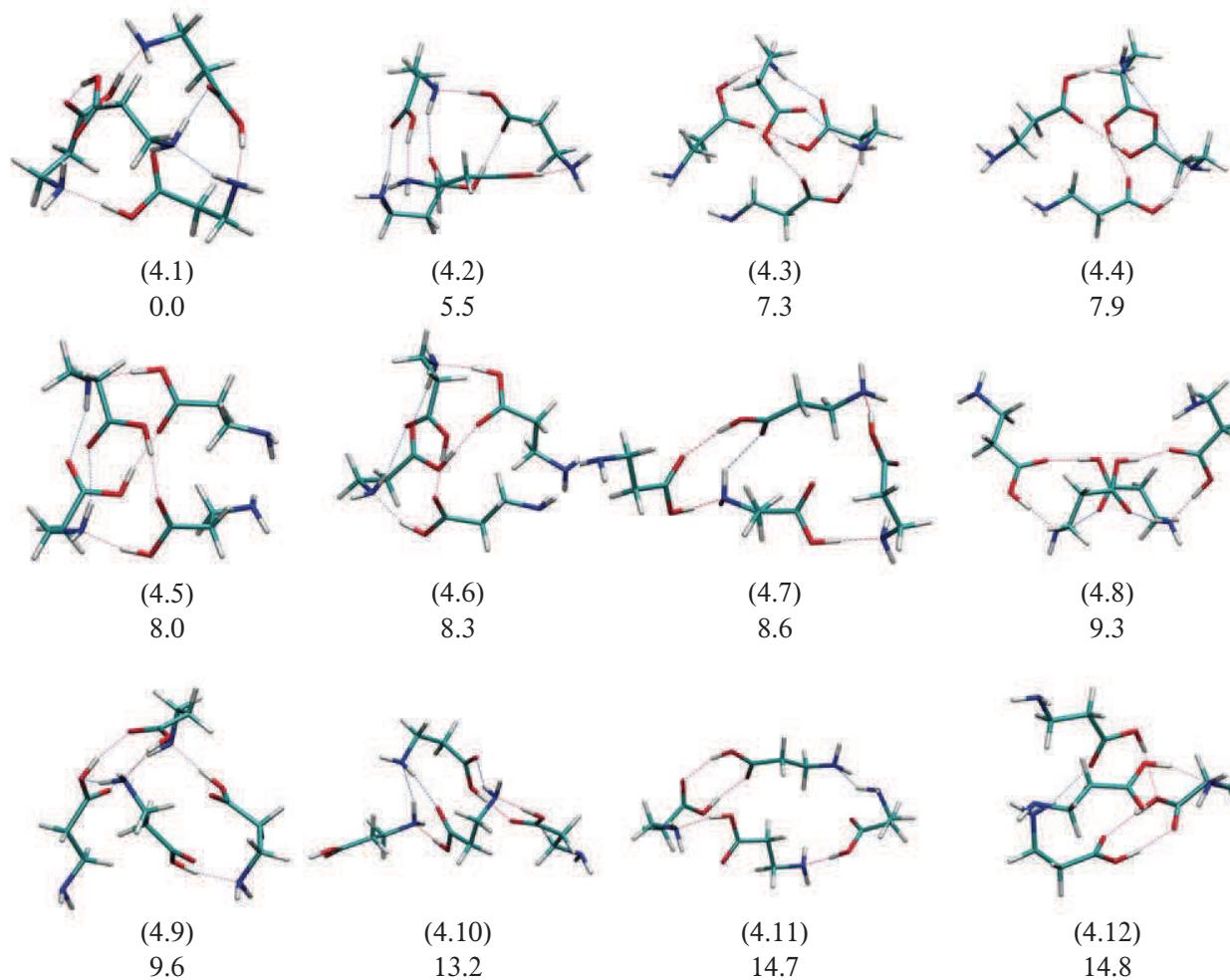


Figure 6: Optimized geometries of neutral tetramers (4.1-4.12) of β -alanine at the DFT-M06-2X/6-311++G(d,p) level of theory. Relative energies with respect to the most stable neutral tetramer (4.1) in kcal mol^{-1} . Dashed lines shows hydrogen (H) bonds with donor (D)-acceptor (A) atoms with the cut-off distance ≤ 3.2 and D-H-A angle ≤ 50 degree.¹³ The colors of hydrogen bond: red, blue and turquoise underline the donor atom: oxygen, nitrogen and carbon, respectively.

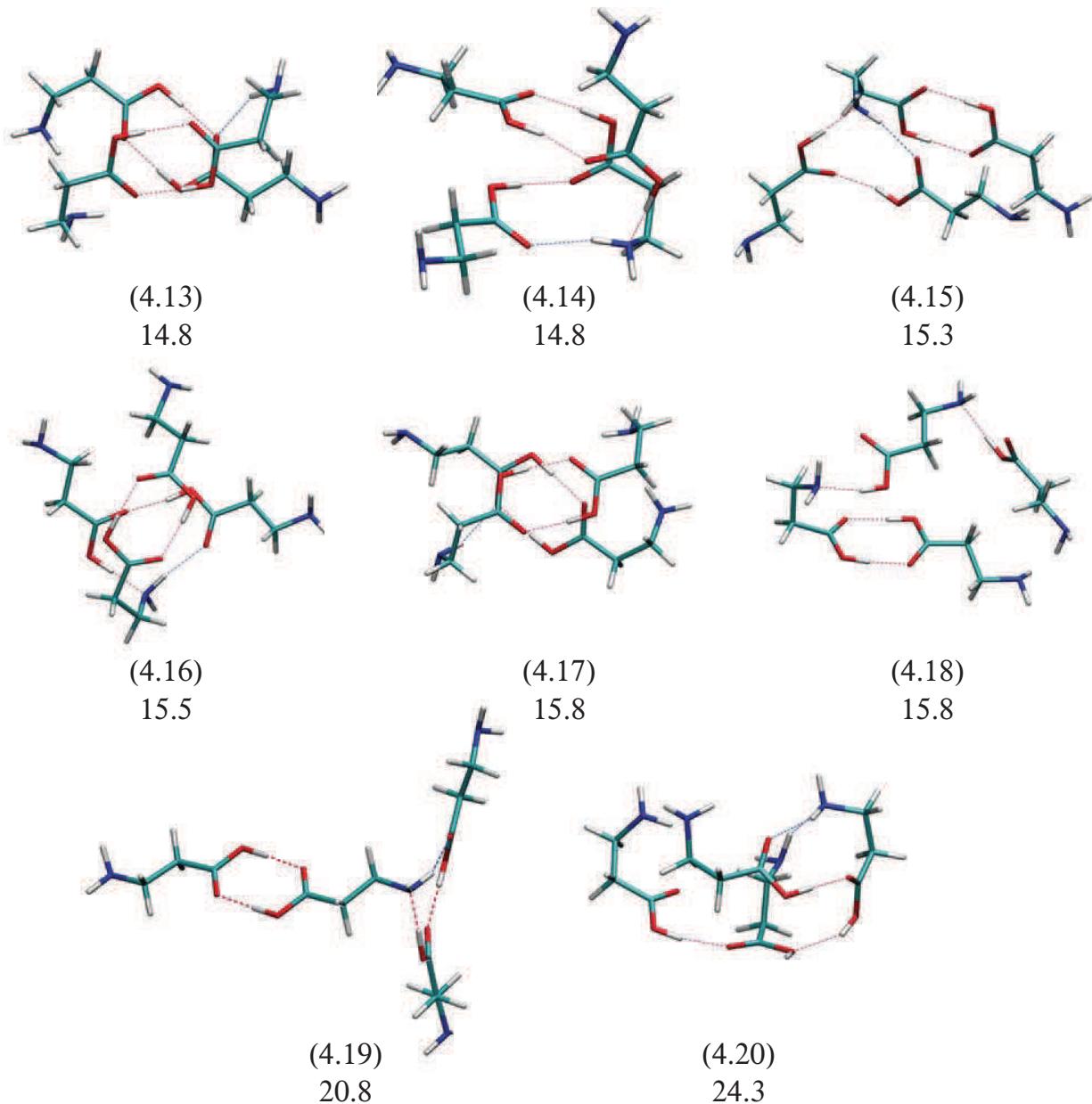


Figure 7: Optimized geometries of neutral tetramers (4.13-4.20) of β -alanine at the DFT-M06-2X/6-311++G(d,p) level of theory. Relative energies with respect to the most stable neutral tetramer (4.1) in kcal mol⁻¹. Dashed lines shows hydrogen (H) bonds with donor (D)-acceptor (A) atoms with the cut-off distance ≤ 3.2 Å and D-H-A angle ≤ 50 degree.¹³ The colors of hydrogen bond: red, blue and turquoise underline the donor atom: oxygen, nitrogen and carbon, respectively.

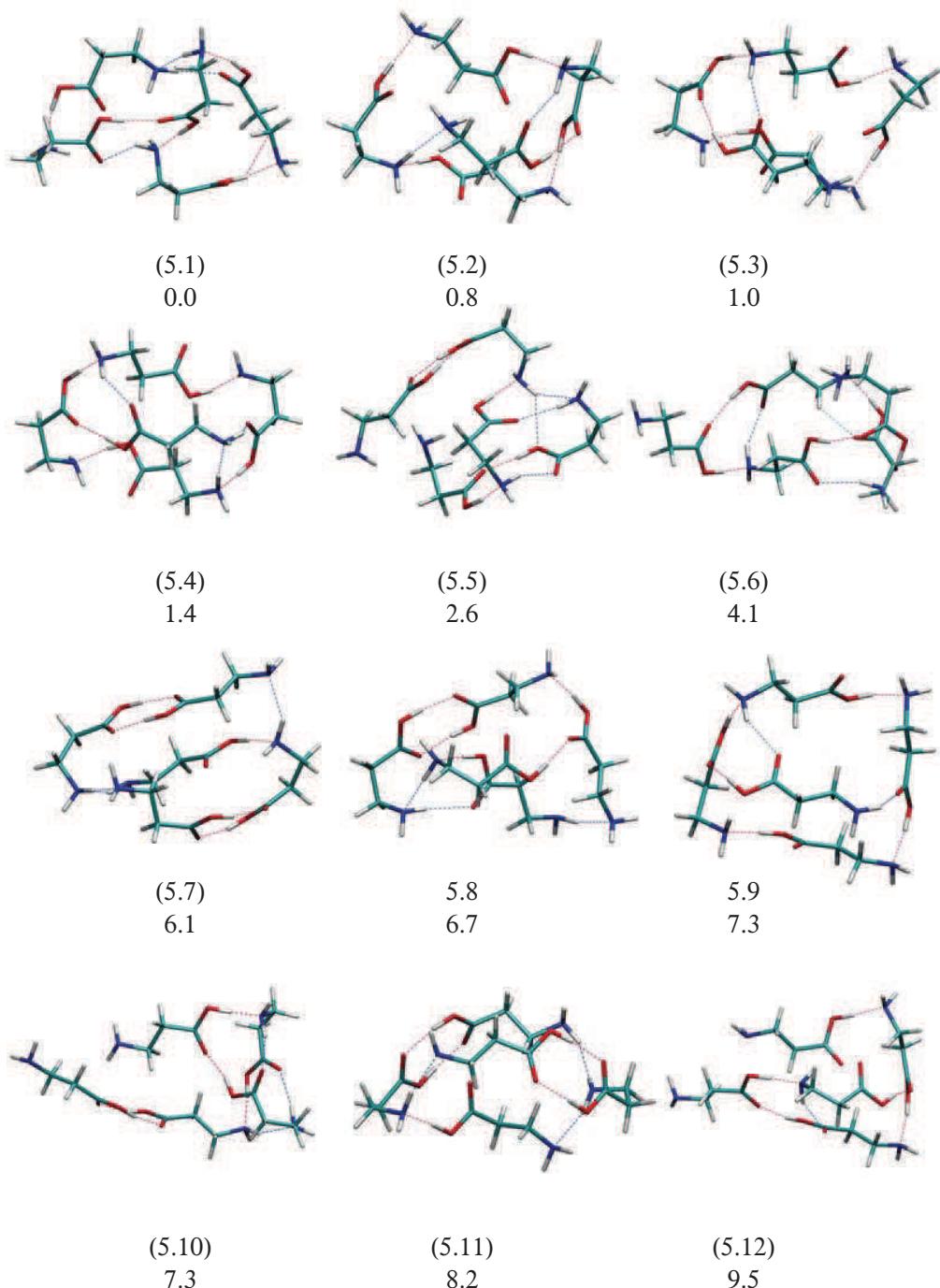


Figure 8: Optimized geometries of neutral pentamers (5.1-5.12) of β -alanine at the DFT-M06-2X/6-311++G(d,p) level of theory. Relative energies with respect to the most stable neutral tetramer (5.1) in kcal mol⁻¹. Dashed lines shows hydrogen (H) bonds with donor (D)-acceptor (A) atoms with the cut-off distance ≤ 3.2 and D-H-A angle ≤ 50 degree.¹³ The colors of hydrogen bond: **red**, **blue** and **turquoise** underline the donor atom: **oxygen**, **nitrogen** and **carbon**, respectively.

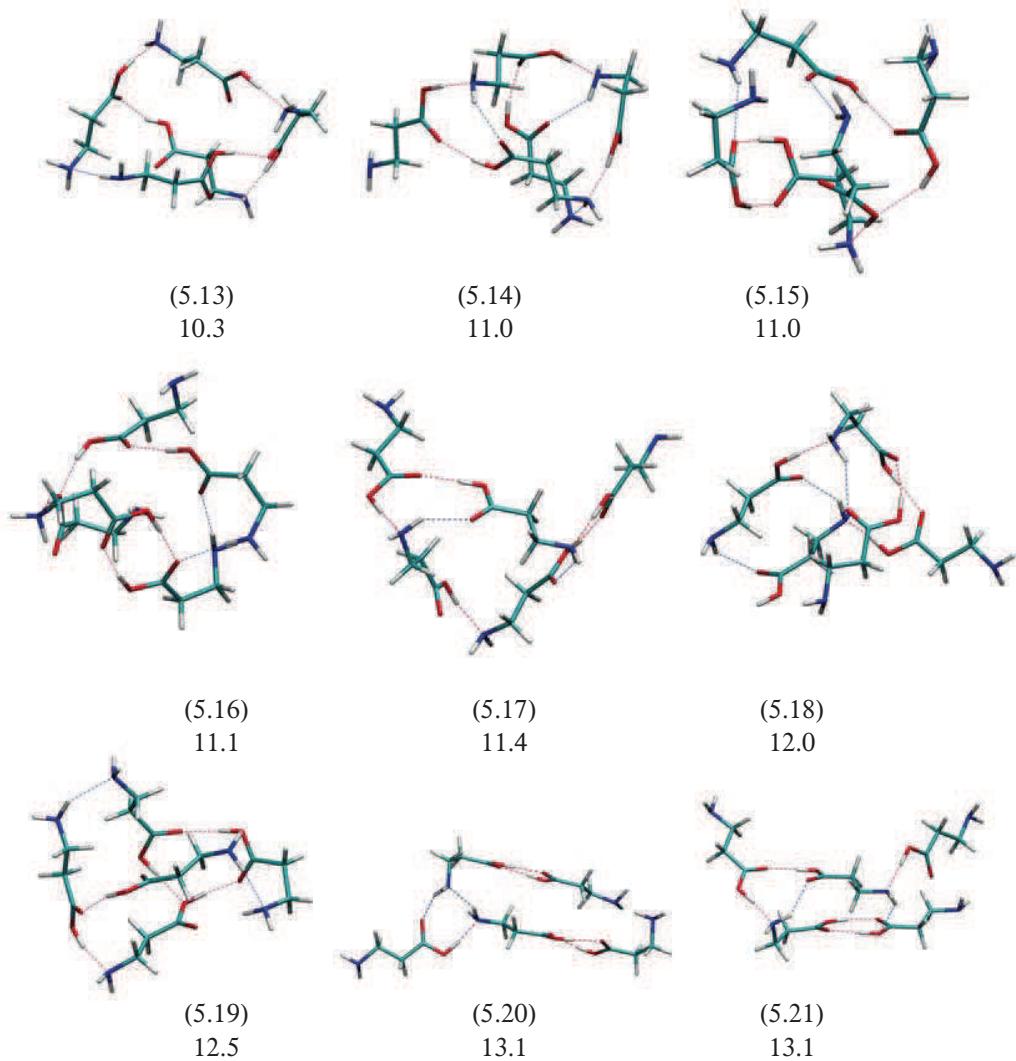


Figure 9: Optimized geometries of neutral pentamers (5.13-5.21) of β -alanine at the DFT-M06-2X/6-311++G(d,p) level of theory. Relative energies with respect to the most stable neutral tetramer (5.1) in kcal mol^{-1} . Dashed lines shows hydrogen (H) bonds with donor (D)-acceptor (A) atoms with the cut-off distance ≤ 3.2 and D-H-A angle ≤ 50 degree.¹³ The colors of hydrogen bond: red, blue and turquoise underline the donor atom: oxygen, nitrogen and carbon, respectively.

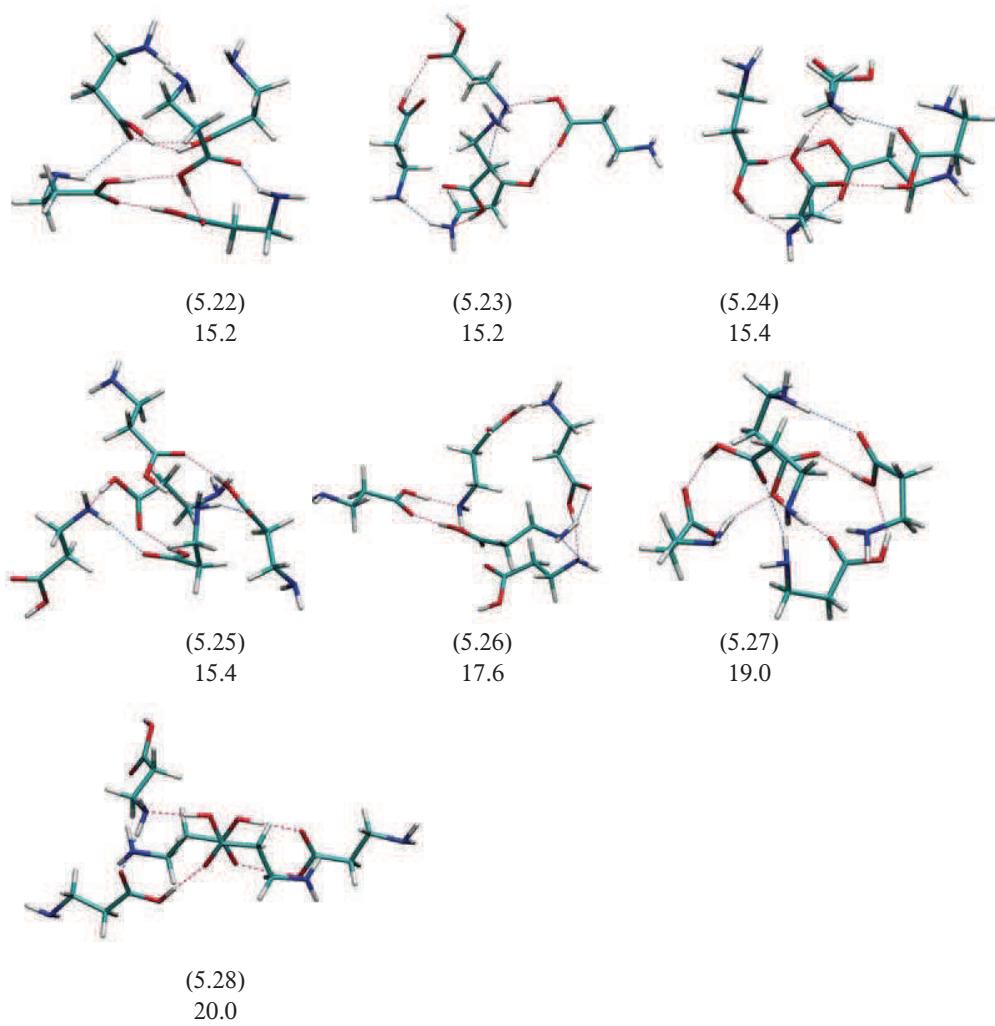


Figure 10: Optimized geometries of neutral pentamers (5.22-5.28) of β -alanine at the DFT-M06-2X/6-311++G(d,p) level of theory. Relative energies with respect to the most stable neutral tetramer (5.1) in kcal mol⁻¹. Dashed lines shows hydrogen (H) bonds with donor (D)-acceptor (A) atoms with the cut-off distance ≤ 3.2 and D-H-A angle ≤ 50 degree.¹³ The colors of hydrogen bond: red, blue and turquoise underline the donor atom: oxygen, nitrogen and carbon, respectively.

Finally, we present a thorough study based on wave function analysis techniques for the most stable conformer of each cluster size. We focused on the estimated stabilization energies for all evaluated hydrogen bonds including a detailed analysis of the type of the donor hydrogen atom, acceptor hydrogen atom, acceptor and donor orbital energy differences and Fock-diagonal NBO Fock matrix elements.

Table 11: Estimated stabilization energy ($\Delta E_{ij}^{(2)}$) (in kcal mol⁻¹) of all the interaction between atoms involved in the hydrogen bonds (HBs) for the most stable dimer. Acceptor and donor orbital energy differences ($\epsilon_j^{(NL)} - \epsilon_i^{(L)}$) in a.u. and off-diagonal NBO Fock matrix elements (F_{ij}) in a.u. are also presented.

DIMER (β -ala) ₂												
HBs index	Donor NBO (i)				Acceptor NBO (j)				$\Delta E_{ij}^{(2)}$	$\epsilon_j^{(NL)} - \epsilon_i^{(L)}$	F_{ij}	
1	BD C 2	N 3	BD*	O 18	H 22	0.28	1.25	0.017				
	BD N 3	H 7	BD*	O 18	H 22	0.28	1.15	0.016				
	BD N 3	H 8	BD*	O 18	H 22	1.62	1.15	0.039				
	CR N 3	-	BD*	O 18	H 22	0.38	15.02	0.069				
	LP N 3	-	BD*	O 18	H 22	34.94	0.86	0.155				
	BD O 18	H 22	RY*	N 3	-	0.07	1.56	0.01				
	BD O 18	H 22	BD*	C 2	N 3	0.07	1.22	0.008				
	BD O 18	H 22	BD*	N 3	H 7	0.15	1.32	0.013				
	BD O 18	H 22	BD*	N 3	H 8	0.06	1.33	0.008				
2	BD O 5	H 9	RY*	N 16	-	0.07	1.56	0.01				
	BD O 5	H 9	BD*	C 15	N 16	0.07	1.22	0.008				
	BD O 5	H 9	BD*	N 16	H 20	0.15	1.32	0.013				
	BD O 5	H 9	BD*	N 16	H 21	0.06	1.33	0.008				
	BD C 15	N 16	BD*	O 5	H 9	0.27	1.25	0.017				
	BD N 16	H 20	BD*	O 5	H 9	0.28	1.15	0.016				
	BD N 16	H 21	BD*	O 5	H 9	1.62	1.15	0.039				
	CR N 16	-	BD*	O 5	H 9	0.38	15.02	0.069				
	LP N 16	-	BD*	O 5	H 9	34.94	0.86	0.155				

Table 12: See caption of 11.

TRIMER (β -ala) ₃											
HBs index	Donor NBO (i)				Acceptor NBO (j)				$\Delta E_{ij}^{(2)}$	$\epsilon_j^{(NL)} - \epsilon_i^{(L)}$	F_{ij}
1	BD O 3 H 4	RY*	N 37	-	-	0.08	1.61	0.010			
	BD O 3 H 4	RY*	N 37	-	-	0.07	1.86	0.011			
	BD O 3 H 4	RY*	N 37	-	-	0.06	2.35	0.011			
	BD O 3 H 4	BD*	C 34	N 37	0.08	1.18	0.009				
	BD O 3 H 4	BD*	N 37	H 39	0.07	1.30	0.009				
	BD* O 3 H 4	RY*	N 37	-	-	1.07	0.02	0.014			
	BD* O 3 H 4	RY*	N 37	-	-	0.17	0.35	0.025			
	BD C 34 N 37	BD*	O 3	H 4	1.66	1.19	0.041				
	BD N 37 H 38	BD*	O 3	H 4	1.97	1.10	0.043				
	BD N 37 H 39	BD*	O 3	H 4	1.88	1.10	0.042				
	CR N 37 - -	BD*	O 3	H 4	1.55	14.97	0.141				
	LP N 37 - -	BD*	O 3	H 4	80.1	0.79	0.226				
2	BD C 15 O 18	BD*	N 37	H 39	0.31	0.96	0.015				
	LP O 18 - -	BD*	N 37	H 39	2.53	1.31	0.051				
	LP O 18 - -	BD*	N 37	H 39	1.48	0.85	0.033				
	BD* C 15 O 18	BD*	N 37	H 39	0.11	0.45	0.018				
	BD N 37 H 39	BD*	C 15	O 18	0.07	0.77	0.007				
3	BD C 21 N 24	BD*	O 29	H 30	0.15	1.26	0.012				
	BD N 24 H 25	BD*	O 29	H 30	0.14	1.16	0.012				
	BD N 24 H 26	BD*	O 29	H 30	1.45	1.15	0.037				
	CR N 24 - -	BD*	O 29	H 30	0.23	15.02	0.054				
	LP N 24 - -	BD*	O 29	H 30	26.84	0.86	0.136				
	BD O 29 H 30	RY*	N 24	-	0.07	1.78	0.010				
	BD O 29 H 30	BD*	C 21	N 24	0.07	1.23	0.008				
	BD O 29 H 30	BD*	N 24	H 25	0.18	1.33	0.014				
	BD O 29 H 30	BD*	N 24	H 26	0.1	1.33	0.010				
4	BD C 2 O 5	BD*	O 16	H 17	0.27	1.65	0.019				
	BD C 2 O 5	BD*	O 16	H 17	1.50	0.95	0.034				
	CR O 5 - -	BD*	O 16	H 17	0.19	19.85	0.056				
	LP O 5 - -	BD*	O 16	H 17	15.13	1.28	0.124				
	LP O 5 - -	BD*	O 16	H 17	3.67	0.85	0.051				
	BD* C 2 O 5	BD*	O 16	H 17	0.66	0.43	0.038				
	BD O 16 H 17	RY*	O 5	-	0.12	1.63	0.013				
	BD O 16 H 17	RY*	O 5	-	0.36	2.54	0.027				
	BD O 16 H 17	BD*	C 2	O 5	0.34	1.51	0.020				
	BD O 16 H 17	BD*	C 2	O 5	0.25	0.9	0.014				

Table 13: See caption of 11.

 TETRAMER (β -ala)₄

HBs index	Donor NBO (i)				Acceptor NBO (j)				$\Delta E_{ij}^{(2)}$	$\epsilon_j^{(\text{NL})} - \epsilon_i^{(\text{L})}$	F_{ij}	
1	BD	O	3	H	4	RY*	N	37	-	0.10	2.56	0.014
	BD	O	3	H	4	BD*	C	34	N	37	0.09	1.19
	BD	O	3	H	4	BD*	N	37	H	38	0.08	1.27
	BD*	O	3	H	4	RY*	N	37	-	-	0.09	0.40
	BD	C	34	N	37	BD*	O	3	H	4	1.22	1.20
	BD	N	37	H	38	BD*	O	3	H	4	1.53	1.10
	BD	N	37	H	39	BD*	O	3	H	4	2.06	1.10
	CR	N	37	-	-	BD*	O	3	H	4	1.33	14.97
	LP	N	37	-	-	BD*	O	3	H	4	71.11	0.80
2	BD	C	2	O	5	BD*	O	16	H	17	0.44	1.64
	BD	C	2	O	5	BD*	O	16	H	17	2.28	0.95
	CR	O	5	-	-	BD*	O	16	H	17	0.26	19.84
	LP	O	5	-	-	BD*	O	16	H	17	13.83	1.26
	LP	O	5	-	-	BD*	O	16	H	17	9.78	0.85
	BD*	C	2	O	5	BD*	O	16	H	17	1.06	0.42
	BD	O	16	H	17	RY*	O	5	-	-	0.05	2.58
	BD	O	16	H	17	BD*	C	2	O	5	0.19	1.50
	BD	O	16	H	17	BD*	C	2	O	5	0.44	0.91
3	BD	N	11	H	13	RY*	O	18	-	-	0.10	1.98
	BD	N	11	H	13	BD*	C	15	O	18	0.13	0.79
	BD	C	15	O	18	BD*	N	11	H	13	0.47	1.00
	LP	O	18	-	-	BD*	N	11	H	13	2.46	1.31
	LP	O	18	-	-	BD*	N	11	H	13	2.60	0.86
	BD*	C	15	O	18	BD*	N	11	H	13	0.20	0.44
4	BD	N	24	H	26	RY*	O	44	-	-	0.10	1.35
	BD	N	24	H	26	RY*	O	44	-	-	0.08	1.64
	BD	N	24	H	26	BD*	C	41	O	44	0.10	0.74
	BD	C	41	O	44	BD*	N	24	H	26	0.96	0.96
	LP	O	44	-	-	BD*	N	24	H	26	0.39	1.31
	LP	O	44	-	-	BD*	N	24	H	26	0.32	0.85
	BD*	C	41	O	44	BD*	N	24	H	26	0.11	0.45
5	BD	N	24	H	25	RY*	O	31	-	-	0.06	1.74
	BD	N	24	H	25	RY*	O	31	-	-	0.15	2.10
	BD	N	24	H	25	BD*	C	28	O	31	0.05	1.37
	BD	N	24	H	25	BD*	C	28	O	31	0.19	0.75
	BD	C	28	O	31	BD*	N	24	H	25	0.38	0.98
	LP	O	31	-	-	BD*	N	24	H	25	2.15	1.32
	LP	O	31	-	-	BD*	N	24	H	25	0.89	0.87
	BD*	C	28	O	31	BD*	N	24	H	25	0.16	0.46
6	BD	N	24	H	25	BD*	N	50	H	52	0.43	1.19
	BD	N	24	H	26	BD*	N	50	H	52	0.35	1.19
	LP	N	24	-	-	BD*	N	50	H	52	11.15	0.89
	BD	N	50	H	-	RY*	N	24	-	-	0.07	1.53
	BD	N	50	H	52	RY*	N	24	-	-	0.18	1.95
	BD	N	50	H	52	BD*	C	21	N	24	0.29	1.15

Table 13: See caption of 11.

 TETRAMER (β -ala)₄

HBs index	Donor NBO (i)				Acceptor NBO (j)				$\Delta E_{ij}^{(2)}$	$\epsilon_j^{(NL)} - \epsilon_i^{(L)}$	F_{ij}
7	BD O 29 H 30	RY*	N 50	-	-	0.06	1.71	0.009			
	BD O 29 H 30	RY*	N 50	-	-	0.08	2.63	0.013			
	BD O 29 H 30	BD*	C 47	N 50	0.06	1.21	0.008				
	BD O 29 H 30	BD*	N 50	H 51	0.08	1.29	0.009				
	BD* O 29 H 30	RY*	N 50	-	-	0.07	0.46	0.022			
	BD* O 29 H 30	RY*	N 50	-	-	0.07	0.33	0.018			
	BD* O 29 H 30	RY*	N 50	-	-	0.09	0.26	0.018			
	BD* O 29 H 30	BD*	N 50	H 51	0.09	0.05	0.008				
	BD C 47 N 50	BD*	O 29	H 30	0.75	1.23	0.028				
	BD N 50 H 51	BD*	O 29	H 30	0.85	1.12	0.028				
	BD N 50 H 52	BD*	O 29	H 30	1.92	1.13	0.043				
	CR N 50 - -	BD*	O 29	H 30	0.83	14.99	0.102				
	LP N 50 - -	BD*	O 29	H 30	53.91	0.82	0.189				
8	BD C 8 N 11	BD*	O 42	H 43	0.90	1.21	0.030				
	BD N 11 H 12	BD*	O 42	H 43	1.26	1.11	0.034				
	BD N 11 H 13	BD*	O 42	H 43	1.96	1.11	0.043				
	CR N 11 - -	BD*	O 42	H 43	1.07	14.98	0.117				
	LP N 11 - -	BD*	O 42	H 43	64.44	0.81	0.205				
	BD O 42 H 43	RY*	N 11	-	-	0.11	1.77	0.013			
	BD O 42 H 43	RY*	N 11	-	-	0.09	2.57	0.013			
	BD O 42 H 43	BD*	C 8	N 11	0.12	1.21	0.011				
	BD* O 42 H 43	RY*	N 11	-	-	0.06	0.17	0.011			
	BD* O 42 H 43	RY*	N 11	-	-	0.47	0.13	0.027			
	BD* O 42 H 43	BD*	N 11	H 12	0.06	0.07	0.007				

Table 14: See caption of 11.

 PENTAMER (β -ala)₅

HBs index	Donor NBO (i)				Acceptor NBO (j)				$\Delta E_{ij}^{(2)}$	$\epsilon_j^{(NL)} - \epsilon_i^{(L)}$	F_{ij}
1	BD O 16 H 17	RY*	N 50	-	-	0.05	1.72	0.008			
	BD O 16 H 17	RY*	N 50	-	-	0.08	2.31	0.012			
	BD O 16 H 17	BD*	N 50	H 51	0.09	1.30	0.010				
	BD* O 16 H 17	RY*	N 50	-	-	0.14	0.38	0.029			
	BD* O 16 H 17	RY*	N 50	-	-	0.07	0.24	0.016			
	BD* O 16 H 17	BD*	N 50	H 51	0.08	0.05	0.008				
	BD C 47 N 50	BD*	O 16	H 17	0.54	1.24	0.024				
	BD N 50 H 51	BD*	O 16	H 17	0.59	1.13	0.024				
	BD N 50 H 52	BD*	O 16	H 17	1.38	1.14	0.036				
	CR N 50 - -	BD*	O 16	H 17	0.59	15.00	0.086				
	LP N 50 - -	BD*	O 16	H 17	44.90	0.84	0.174				
2	BD N 50 H 52	RY*	N 63	-	-	0.11	1.72	0.012			
	BD N 50 H 52	RY*	N 63	-	-	0.10	2.44	0.014			
	BD N 50 H 52	BD*	C 60	N 63	0.11	1.13	0.010				
	BD N 63 H 64	BD*	N 50	H 52	0.61	1.18	0.024				
	LP N 63 - -	BD*	N 50	H 52	10.35	0.89	0.086				

Table 14: See caption of 11.

 PENTAMER (β -ala)₅

HBs index	Donor NBO (i)				Acceptor NBO (j)				$\Delta E_{ij}^{(2)}$	$\epsilon_j^{(NL)} - \epsilon_i^{(L)}$	F_{ij}
3	BD C 15	O 18	BD* N 63	H 64	1.55	0.99	0.035				
	LP O 18	-	BD* N 63	H 64	2.65	1.32	0.053				
	LP O 18	-	BD* N 63	H 64	0.64	0.87	0.022				
	BD* C 15	O 18	BD* N 63	H 64	0.45	0.46	0.037				
	BD N 63	H 64	BD* C 15	O 18	0.30	0.76	0.014				
4	BD O 3	H 4	RY* O 44	-	0.14	1.95	0.015				
	BD O 3	H 4	RY* O 44	-	0.28	2.52	0.024				
	BD O 3	H 4	BD* C 41	O 44	0.45	1.51	0.023				
	BD O 3	H 4	BD* C 41	O 44	0.26	0.92	0.015				
	BD C 41	O 44	BD* O 3	H 4	0.42	1.64	0.024				
	BD C 41	O 44	BD* O 3	H 4	0.60	0.96	0.022				
	CR O 44	-	BD* O 3	H 4	0.27	19.85	0.066				
	LP O 44	-	BD* O 3	H 4	20.42	1.27	0.144				
	LP O 44	-	BD* O 3	H 4	2.09	0.84	0.038				
	BD* C 41	O 44	BD* O 3	H 4	0.70	0.42	0.039				
5	BD C 8	N 11	BD* O 55	H 56	0.41	1.25	0.021				
	BD N 11	H 12	BD* O 55	H 56	0.41	1.16	0.020				
	BD N 11	H 13	BD* O 55	H 56	1.84	1.15	0.042				
	CR N 11	-	BD* O 55	H 56	0.53	15.02	0.081				
	LP N 11	-	BD* O 55	H 56	41.64	0.86	0.169				
	BD O 55	H 56	RY* N 11	-	0.05	1.66	0.008				
	BD O 55	H 56	RY* N 11	-	0.06	1.50	0.009				
	BD O 55	H 56	BD* C 8	N 11	0.07	1.22	0.008				
	BD O 55	H 56	BD* N 11	H 12	0.13	1.32	0.012				
	BD C 2	O 5	BD* N 37	H 38	0.91	0.98	0.027				
6	LP O 5	-	BD* N 37	H 38	1.63	1.30	0.041				
	LP O 5	-	BD* N 37	H 38	2.29	0.85	0.041				
	BD* C 2	O 5	BD* N 37	H 38	0.21	0.43	0.024				
	BD N 37	H 38	BD* C 2	O 5	0.11	0.77	0.009				
	BD C 34	N 37	BD* O 42	H 43	1.84	1.15	0.043				
7	BD N 37	H 38	BD* O 42	H 43	4.48	1.06	0.064				
	BD N 37	H 39	BD* O 42	H 43	2.02	1.06	0.043				
	CR N 37	-	BD* O 42	H 43	2.16	14.93	0.168				
	LP N 37	-	BD* O 42	H 43	93.72	0.76	0.239				
	BD O 42	H 43	BD* C 34	N 37	0.16	1.19	0.012				
	BD O 42	H 43	BD* N 37	H 39	0.10	1.28	0.010				
	BD* O 42	H 43	RY* N 37	-	0.06	1.66	0.031				
	BD* O 42	H 43	BD* C 34	N 37	1.73	0.04	0.024				
	BD* O 42	H 43	BD* N 37	H 39	0.21	0.13	0.015				
	BD C 21	H 22	BD* O 29	H 30	0.08	1.02	0.008				
8	BD C 21	N 24	BD* O 29	H 30	0.99	1.25	0.032				
	BD C 21	N 24	BD* O 29	H 30	0.99	1.25	0.032				
	BD N 24	H 25	BD* O 29	H 30	1.28	1.16	0.035				
9	BD N 24	H 26	BD* O 29	H 30	0.27	1.16	0.016				
	CR N 24	-	BD* O 29	H 30	0.58	15.03	0.085				
	LP N 24	-	BD* O 29	H 30	42.86	0.86	0.172				
	BD O 29	H 30	RY* N 24	-	0.11	1.83	0.013				
	BD O 29	H 30	BD* N 24	H 26	0.22	1.31	0.015				

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