

Supplementary Information for
**Emergence of Topological Nodal Loops in Alkaline-Earth
Hexaborides XB_6 ($X=Ca, Sr, Ba$) under Pressure**

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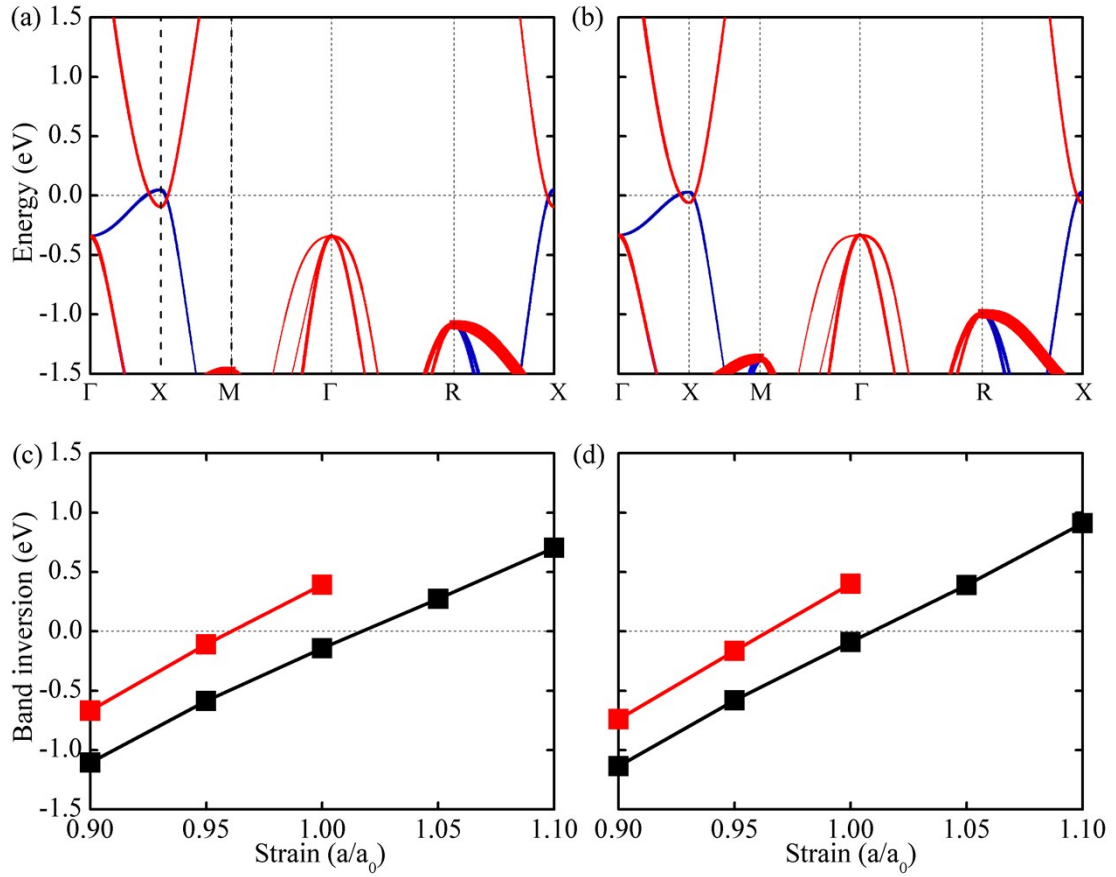


FIG. S1. (Color online) Projected band structures of (a) CaB₆ and (b) SrB₆ from GGA-PBE without SOC. The blue and red color show B p_x (p_z) and p_y orbitals, respectively. Evolution of the band inversion between the bonding and anti-bonding bands at X point of (c) CaB₆ and (d) SrB₆. Negative values indicate the existence of band inversion. Black: GGA-PBE. Red: HSE06.

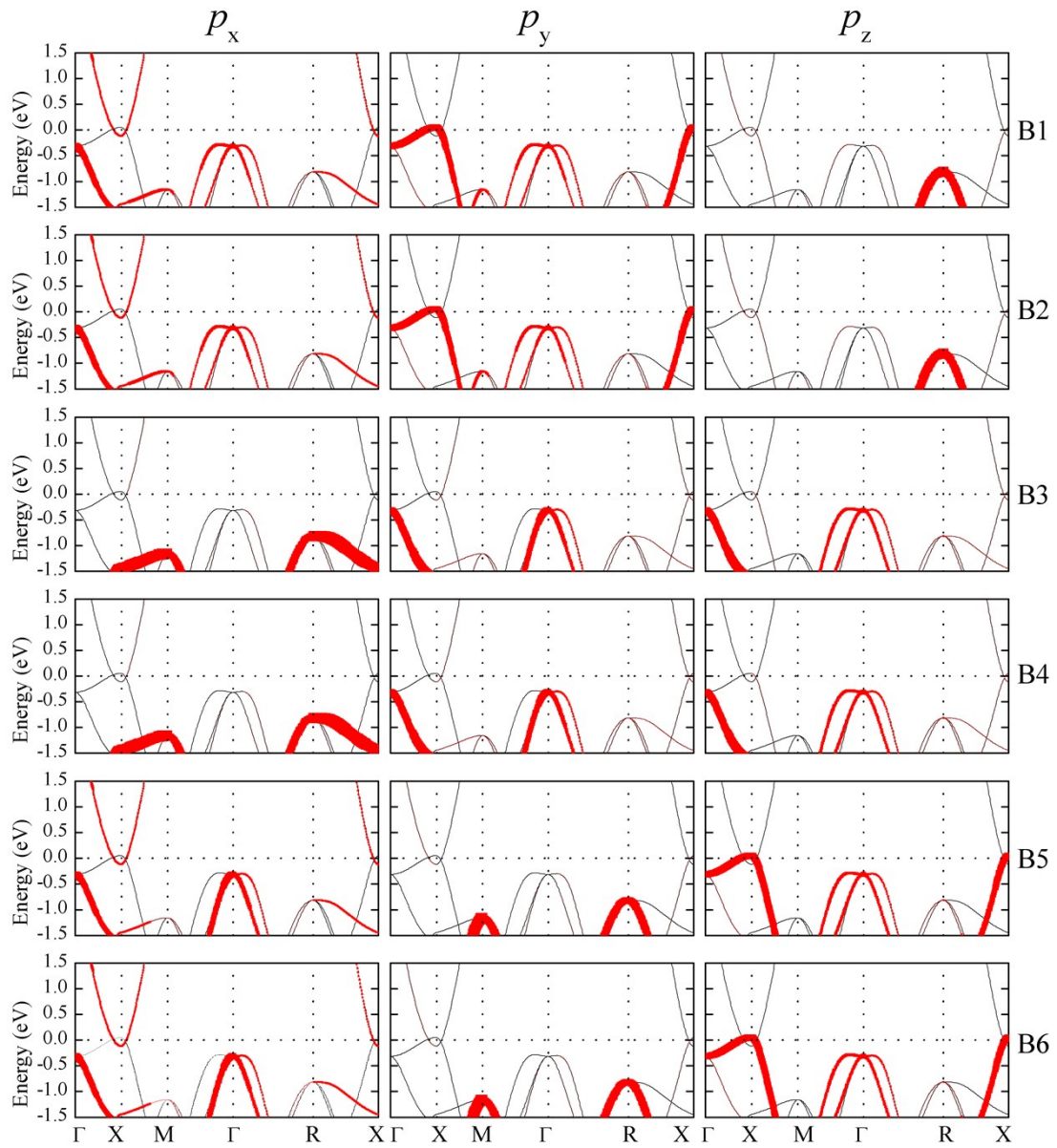


FIG. S2. (Color online) Projected band structures of B p orbitals.

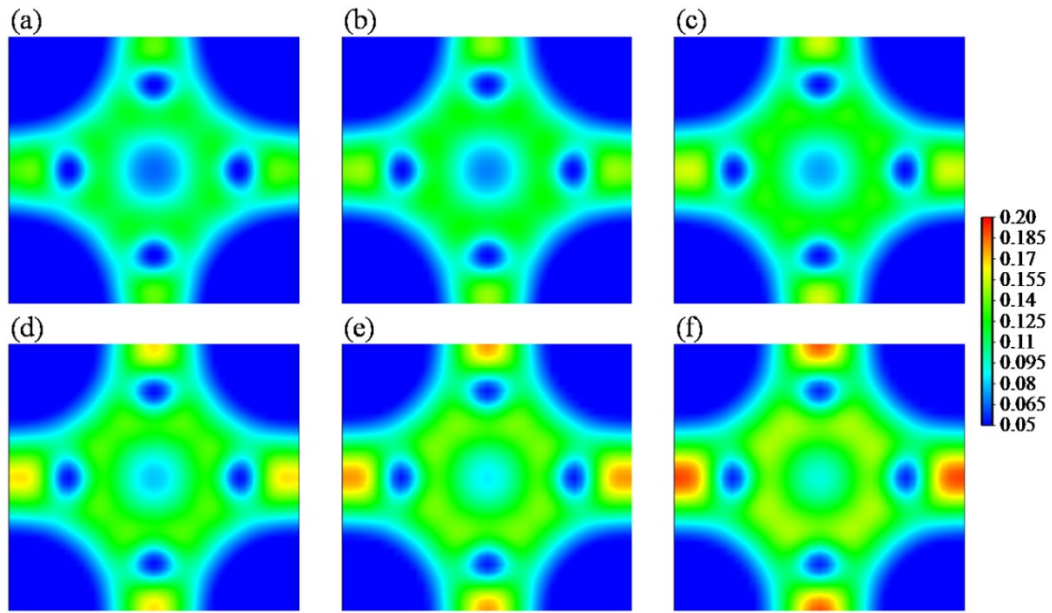


FIG. S3. (Color online) Charge density contours of the (001) plane formed by B3-B6 atoms as shown in Fig. 1a: (a) unstrained; (b)-(f) strained systems at a strain of 0.98, 0.96, 0.94, 0.92, and 0.90, respectively.

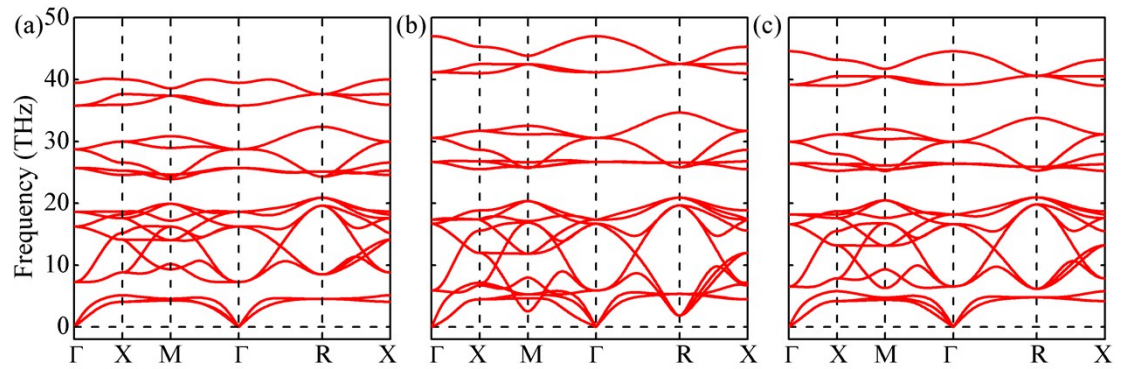


FIG. S4. (Color online) Phonon band dispersions of (a) BaB_6 , (b) CaB_6 , and (c) SrB_6 at the strain of 0.95.