

ELECTRONIC SUPPORTING INFORMATION

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Predicting bond dissociation energy and bond length for bimetallic diatomic molecules: A challenge for electronic structure theory

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This supporting information contains full versions of Tables 4-9.

Table S1. The signed errors and mean unsigned errors (MUEs) for the calculated equilibrium bond length (r_e in the units of Å) for various XC functionals, using the ECP protocol.

Functional	Cr_2	V_2	Mo_2	VCr	VNb	ScCo	YCo	NbCr	MUE
BLYP	-0.083	-0.040	-0.007	-0.055	-0.019	-0.028	-0.001	0.003	0.029
MN12-L	-0.100	-0.019	-0.021	0.064	-0.008	-0.011	-0.002	0.048	0.034
MGGA-MS1	-0.106	-0.031	-0.031	0.003	-0.034	-0.045	-0.026	0.012	0.036
RPBE	-0.092	-0.048	-0.021	-0.004	-0.031	-0.037	-0.012	-0.049	0.037
SOGGA11	-0.100	-0.053	-0.041	-0.015	-0.042	-0.035	-0.006	-0.004	0.037
revPBE	-0.093	-0.050	-0.022	-0.006	-0.032	-0.039	-0.015	-0.049	0.038
MGGA-MS2	-0.103	-0.037	-0.026	-0.043	-0.030	-0.044	-0.021	0.012	0.039
PBE	-0.096	-0.054	-0.025	-0.068	-0.037	-0.046	-0.024	-0.004	0.044
MOHLYP	-0.101	-0.057	-0.035	0.011	-0.042	-0.041	-0.013	-0.058	0.045
MGGA-MS0	-0.107	-0.106	-0.031	0.012	-0.032	-0.045	-0.026	0.017	0.047
OreLYP	-0.108	-0.066	-0.040	-0.013	-0.051	-0.060	-0.037	-0.005	0.048
M06-L	-0.106	-0.061	-0.046	0.005	-0.044	-0.054	-0.039	0.027	0.048
OLYP	-0.109	-0.067	-0.041	-0.019	-0.053	-0.059	-0.037	-0.005	0.049
MGGA-MS2h	-0.117	-0.119	-0.041	0.012	-0.032	-0.056	-0.037	0.011	0.053
PBEsol	-0.105	-0.064	-0.034	-0.044	-0.049	-0.064	-0.045	-0.029	0.054
SOGGA	-0.107	-0.066	-0.037	-0.043	-0.051	-0.066	-0.048	-0.027	0.056
τ -HCTH	-0.117	-0.076	-0.046	-0.029	-0.062	-0.072	-0.049	-0.013	0.058
N12	-0.106	-0.132	-0.037	-0.043	-0.053	-0.062	-0.043	-0.059	0.067
N12-SX	-0.119	-0.077	-0.049	-0.041	-0.064	-0.063	-0.053	-0.067	0.067
B1LYP	-0.127	-0.135	-0.050	0.030	-0.077	-0.065	-0.048	-0.015	0.068
M11-L	-0.125	-0.099	-0.048	-0.097	-0.048	-0.076	-0.042	-0.061	0.075
O3LYP	-0.127	-0.083	-0.057	-0.054	-0.069	-0.076	-0.057	-0.085	0.076
MN15-L	-0.130	-0.080	-0.065	0.062	-0.068	-0.070	-0.062	0.076	0.077
B97-3	-0.140	-0.093	-0.065	-0.019	-0.076	-0.078	-0.062	-0.083	0.077
B3LYP	-0.121	-0.132	-0.044	-0.078	-0.065	-0.063	-0.044	-0.067	0.077
B97-1	-0.127	-0.082	-0.051	-0.098	-0.065	-0.067	-0.049	-0.083	0.078
τ -HCTHhyb	-0.122	-0.132	-0.047	-0.080	-0.062	-0.068	-0.050	-0.073	0.079
MPW3LYP	-0.124	-0.134	-0.047	-0.094	-0.059	-0.065	-0.048	-0.068	0.080
M05	-0.141	-0.150	-0.080	0.026	-0.132	-0.075	-0.051	-0.012	0.083
M06	-0.135	-0.145	-0.064	-0.057	-0.133	-0.078	-0.058	0.003	0.084
SOGGA11-X	-0.159	-0.015	-0.084	-0.077	-0.047	-0.092	-0.082	-0.118	0.084
MN12-SX	-0.120	-0.118	-0.041	0.276	-0.039	-0.038	-0.028	-0.067	0.091
TPSSh	-0.112	-0.126	-0.040	0.282	-0.046	-0.057	-0.038	-0.060	0.095
ω B97X-D	-0.144	-0.100	-0.077	-0.102	-0.086	-0.081	-0.067	-0.186	0.106
MPW1K	-0.165	-0.172	-0.089	-0.093	0.053	-0.097	-0.087	-0.123	0.110
M08-SO	-0.167	-0.180	-0.084	0.021	-0.186	-0.079	-0.060	-0.126	0.113
M11	-0.162	-0.182	-0.093	-0.122	-0.115	-0.077	-0.060	-0.119	0.116
MN15	-0.149	-0.166	-0.069	-0.183	-0.168	-0.094	-0.069	-0.035	0.116
ω B97X	-0.154	-0.160	-0.091	-0.122	-0.098	-0.088	-0.072	-0.196	0.123
HSE06	-0.136	-0.148	-0.062	0.011	-0.101	-0.077	-0.063	0.479	0.135

	-0.062	-0.058	-0.063	0.695	-0.068	-0.150	-0.063	-0.039	0.150
GAM	-0.116	-0.073	-0.052	0.714	-0.055	-0.057	-0.032	0.114	0.152
MPW1B95	-0.146	-0.064	-0.071	0.728	-0.068	-0.093	-0.072	-0.043	0.161
PBE0	-0.139	-0.152	-0.065	0.761	-0.059	-0.082	-0.068	-0.084	0.176
MPWB1K	-0.070	-0.116	-0.089	0.838	-0.006	-0.148	-0.087	0.073	0.178
M06-2X	-0.174	-0.186	-0.091	0.834	-0.036	-0.111	-0.099	-0.134	0.208
M05-2X	-0.176	-0.180	-0.089	0.735	-0.183	-0.108	-0.091	-0.130	0.211
M08-HX	-0.172	-0.180	-0.087	0.812	0.334	-0.088	-0.077	-0.122	0.234
PWB6K	-0.167	-0.117	-0.090	0.848	0.014	-0.147	-0.086	0.677	0.268
M06-HF	-0.214	-0.160	-0.111	0.940	0.132	-0.102	-0.108	0.892	0.332
Exptl. r_e	1.681	1.770	1.938	1.724	1.943	1.809	1.980	1.892	-

Table S2. The signed errors and mean unsigned errors (MUEs) for the calculated equilibrium bond length (r_e in the units of Å) for various XC functionals, using the DKH protocol.

Functional	Cr ₂	V ₂	Mo ₂	VCr	VNb	ScCo	YCo	NbCr	MUE
BLYP	0.003	-0.018	-0.003	-0.015	-0.006	-0.005	0.007	0.000	0.007
RPBE	-0.085	-0.024	-0.020	0.006	-0.017	-0.011	-0.005	0.013	0.023
revPBE	-0.087	-0.026	-0.021	0.000	-0.019	-0.014	-0.008	0.012	0.024
SOGGA11	0.028	-0.021	-0.040	-0.039	-0.067	0.002	0.003	0.002	0.025
PBE	-0.092	-0.033	-0.024	-0.023	-0.025	-0.025	-0.018	-0.005	0.031
MOHLYP	-0.095	-0.032	-0.035	0.062	-0.028	-0.010	-0.006	-0.036	0.038
OLYP	0.096	-0.048	-0.043	-0.012	-0.042	-0.037	-0.032	-0.001	0.039
OreLYP	0.120	-0.048	-0.042	-0.009	-0.041	-0.038	-0.033	-0.004	0.042
PBESol	-0.105	-0.049	-0.036	-0.053	-0.040	-0.048	-0.042	-0.008	0.048
MGGA-MS0	-0.106	-0.109	-0.039	0.009	-0.035	-0.035	-0.040	0.018	0.049
SOGGA	-0.107	-0.051	-0.040	-0.052	-0.043	-0.050	-0.045	-0.032	0.053
τ -HCTH	-0.122	-0.066	-0.050	-0.024	-0.056	-0.057	-0.047	-0.009	0.054
N12-SX	-0.038	-0.067	-0.040	-0.030	-0.124	-0.052	-0.044	-0.054	0.056
M11-L	-0.004	-0.142	-0.065	-0.036	-0.040	-0.073	-0.050	-0.057	0.058
MN12-L	-0.015	-0.072	-0.049	-0.096	-0.058	-0.062	-0.053	-0.062	0.058
N12	-0.111	-0.059	-0.044	-0.080	-0.051	-0.054	-0.043	-0.069	0.064
MGGA-MS1	-0.105	-0.109	-0.038	0.158	-0.034	-0.033	-0.037	0.016	0.066
M06-L	-0.107	-0.044	-0.046	0.178	-0.034	-0.034	-0.030	0.060	0.067
B97-3	-0.142	-0.081	-0.065	-0.011	-0.067	-0.058	-0.056	-0.173	0.082
MN12-SX	-0.139	-0.020	-0.057	0.393	-0.097	-0.054	-0.052	0.006	0.102
PW6B95	-0.141	-0.043	-0.063	-0.008	-0.096	-0.061	-0.058	0.367	0.105
SOGGA11-X	-0.164	-0.104	-0.083	-0.128	-0.039	-0.075	-0.075	-0.189	0.107
M05	-0.141	-0.077	-0.078	-0.171	-0.091	-0.040	-0.039	0.263	0.112
MGGA-MS2	0.677	0.000	-0.035	-0.051	-0.031	-0.029	-0.033	-0.040	0.112
ω B97X-D	0.155	-0.091	-0.078	-0.182	-0.081	-0.065	-0.063	-0.181	0.112
M06	-0.136	-0.136	-0.056	-0.167	-0.081	-0.049	-0.041	0.316	0.123
PBE0	-0.142	-0.150	-0.065	-0.181	-0.147	-0.065	-0.063	-0.176	0.124
MGGA-MS2h	-0.118	-0.120	-0.049	0.008	-0.095	-0.043	-0.048	0.515	0.125
B3LYP	-0.123	-0.129	-0.042	-0.162	-0.125	-0.046	-0.038	0.413	0.135
τ -HCTHhyb	0.566	-0.068	-0.050	0.086	-0.096	-0.054	-0.050	-0.160	0.141
TPSSh	0.739	-0.124	-0.042	-0.072	-0.040	-0.041	-0.038	-0.058	0.144
GAM	-0.118	-0.057	-0.058	0.818	-0.045	-0.035	-0.025	-0.044	0.150
O3LYP	-0.129	-0.070	-0.058	0.670	-0.116	-0.057	-0.053	-0.169	0.165
ω B97X	0.749	-0.102	-0.048	-0.039	-0.137	-0.071	-0.068	-0.145	0.170
B1LYP	0.831	-0.026	-0.047	-0.166	-0.048	-0.048	-0.041	-0.159	0.171
MN15-L	0.754	-0.080	-0.078	-0.104	-0.074	-0.070	-0.076	0.211	0.181
B97-1	0.709	-0.043	-0.053	-0.168	-0.133	-0.050	-0.048	0.315	0.190
M08-SO	-0.167	-0.165	-0.082	0.788	-0.040	-0.043	-0.045	-0.190	0.190
M05-2X	-0.174	-0.114	-0.086	0.699	-0.096	-0.081	-0.079	-0.196	0.191
HSE06	0.887	-0.146	-0.061	-0.177	-0.063	-0.061	-0.057	-0.172	0.203

MPWB1K	-0.171	-0.112	-0.090	0.856	-0.125	-0.081	-0.082	0.175	0.211
M06-2X	-0.171	-0.112	-0.088	0.851	-0.133	-0.075	-0.079	-0.198	0.213
M08-HX	-0.170	-0.164	-0.086	0.536	0.065	-0.058	-0.057	0.603	0.217
MPW1B95	0.875	-0.155	-0.071	-0.099	-0.073	-0.069	-0.073	0.447	0.233
MPW1K	1.002	-0.173	-0.089	-0.204	-0.040	-0.081	-0.082	-0.199	0.234
MN15	-0.153	-0.156	-0.081	0.781	-0.159	-0.077	-0.082	0.416	0.238
MPW3LYP	0.782	-0.035	-0.045	0.669	-0.124	-0.049	-0.041	0.413	0.270
M11	1.009	-0.166	-0.085	0.772	-0.135	-0.039	-0.033	-0.194	0.304
M06-HF	1.046	-0.147	-0.113	0.885	0.067	-0.051	-0.081	-0.235	0.328
PWB6K	0.940	-0.171	-0.091	0.870	-0.033	-0.079	-0.080	0.665	0.366
Exptl. r_e	1.681	1.770	1.938	1.724	1.943	1.809	1.980	1.892	-

Table S3. The signed errors and mean unsigned errors (MUEs) for the calculated equilibrium bond dissociation energy ($D_e^{\text{SP-ECP}}$ in the units of kcal/mol) for various XC functionals, using the def2-QZVP basis combined with SDD ECP.

Functional	Cr ₂	V ₂	Mo ₂	Rh ₂	VNb	ScCo	YCo	NbCr	MUE
τ-HCTHhyb	2.1	0.1	8.4	5.0	-0.2	7.9	-11.0	-6.2	5.1
M05	-5.7	9.1	9.0	1.5	7.8	12.1	-12.5	-1.7	7.4
MN15	-9.0	13.0	-11.4	2.8	-2.0	12.6	-9.9	-13.6	9.3
M06-L	14.0	22.9	-6.9	9.3	10.5	23.6	-3.9	-4.8	12.0
BLYP	9.2	25.1	4.5	11.0	8.8	30.8	6.5	-2.3	12.3
N12-SX	-0.6	-24.3	3.3	-3.1	-14.5	-19.0	-32.8	-2.0	12.4
M06	-10.1	15.7	2.2	10.1	11.0	10.3	-14.4	-29.3	12.9
OreLYP	2.3	26.6	-1.4	10.3	10.3	39.0	12.7	-12.3	14.4
MN15-L	-14.0	1.8	-33.0	5.0	-14.1	20.6	-2.7	-24.4	14.5
RPBE	-6.4	31.7	-19.7	4.8	3.9	30.9	5.8	-15.3	14.8
OLYP	-2.0	28.2	-10.6	5.8	5.7	37.3	10.9	-18.8	14.9
O3LYP	-23.9	-0.8	-27.6	-10.1	-16.5	11.2	-11.2	-29.2	16.3
GAM	-4.9	18.1	-4.3	15.5	6.2	41.8	15.6	-25.2	16.4
revPBE	-7.2	33.8	-20.6	5.8	4.4	32.4	7.3	-21.9	16.7
B97-1	-15.6	-20.4	-8.0	-9.3	-18.0	-12.8	-28.2	-23.1	17.0
MOHLYP	-20.0	6.7	-33.6	-15.1	-15.5	13.8	-11.2	-38.5	19.3
TPSSh	-29.0	19.8	-34.5	-12.7	-10.0	4.6	-15.7	-33.1	19.9
N12	4.1	37.3	19.9	35.6	20.6	34.7	12.7	3.7	21.1
MPW3LYP	-30.0	-11.3	-29.0	-8.0	-23.2	-7.9	-25.3	-45.4	22.5
PBE	1.1	66.5	-9.8	15.4	25.6	43.0	17.3	-12.5	23.9
SOGGA11	-6.1	43.7	14.5	12.6	26.7	59.6	37.1	-7.6	26.0
M11-L	-9.5	-35.6	-15.3	-9.4	-31.5	-36.2	-59.5	-20.2	27.2
MGGA-MS2	-18.5	-38.0	-37.3	-15.9	-36.2	-13.6	-31.1	-28.7	27.4
B3LYP	-30.6	-22.6	-30.1	-18.4	-29.7	-13.7	-31.2	-45.7	27.7
PBEsol	11.8	61.6	1.4	27.8	28.1	61.0	33.5	2.3	28.4
SOGGA	9.2	63.1	-1.3	28.7	28.0	62.4	34.7	0.0	28.4
MGGA-MS0	-28.7	-7.0	-42.5	-22.3	-32.7	-27.1	-42.8	-32.4	29.5
MGGA-MS1	-26.9	-22.5	-42.3	-21.2	-39.2	-19.2	-36.1	-34.3	30.2
MN12-SX	14.6	-62.5	31.4	3.8	-18.8	-40.5	-53.1	17.6	30.3
B97-3	-32.2	-34.5	-25.2	-21.5	-32.3	-25.3	-40.5	-32.5	30.5
PW6B95	-42.1	-20.7	-39.3	-20.4	-32.9	-16.3	-31.7	-44.2	31.0
ωB97X	-25.8	-43.7	-21.6	-17.2	-36.0	-30.1	-43.9	-45.0	32.9
MPW1B95	-46.3	-22.1	-43.9	-21.8	-36.4	-19.7	-34.7	-48.8	34.2
ωB97X-D	-36.3	-38.0	-30.4	-18.5	-36.5	-24.7	-39.2	-55.5	34.9
M08-SO	-45.5	-22.0	-40.9	-13.0	-33.4	-32.8	-48.8	-47.9	35.5
HSE06	-47.2	-17.2	-49.8	-22.1	-37.2	-18.6	-35.5	-66.7	36.8
PBE0	-47.0	-17.3	-50.7	-22.9	-37.7	-18.8	-35.9	-67.2	37.2
B1LYP	-39.6	-40.5	-38.7	-26.0	-42.5	-29.9	-45.1	-43.0	38.2
MGGA-MS2h	-39.2	-34.8	-48.6	-23.3	-48.9	-30.0	-43.1	-44.7	39.1
M05-2X	-34.2	-51.3	-20.0	-19.7	-39.8	-51.7	-59.0	-58.9	41.8
M06-2X	-39.9	-57.7	-20.9	-32.6	-49.4	-45.6	-60.2	-40.4	43.3
MN12-L	23.5	-68.5	-12.1	-20.5	-46.7	-80.9	-90.4	7.8	43.8
MPWB1K	-61.5	-43.2	-61.0	-32.6	-55.0	-49.2	-59.4	-64.4	53.3
SOGGA11-X	-52.6	-64.1	-52.3	-27.1	-58.5	-59.1	-69.8	-55.4	54.9
M11	-72.9	-37.2	-64.6	-35.3	-52.3	-40.0	-48.9	-101.8	56.6
M08-HX	-58.8	-56.7	-47.0	-28.6	-56.5	-58.4	-68.5	-82.0	57.1
PWB6K	-63.3	-49.5	-63.1	-34.3	-59.0	-56.1	-65.0	-66.1	57.1
τ-HCTH	38.8	45.2	41.5	110.8	40.0	102.1	72.5	34.8	60.7
M06-HF	-55.3	-129.4	-18.7	-48.3	-73.8	-48.9	-52.9	-86.0	64.2
MPW1K	-69.5	-47.6	-75.9	-39.8	-70.4	-53.6	-64.3	-98.5	65.0
Exptl. D_e	36.0	64.2	103.9	55.9	88.1	56.8	60.0	70.3	-

Table S4. The signed errors and mean unsigned errors (MUEs) for the calculated equilibrium bond dissociation energy ($D_e^{\text{SP-DKH}}$ in the units of kcal/mol) for various XC functionals, using aug-cc-pwCVTZ-DK all-electron basis and DKH2.

Functional	Cr ₂	V ₂	Mo ₂	Rh ₂	VNb	ScCo	YCo	NbCr	MUE
τ-HCTHhyb	0.2	-4.9	4.0	10.8	-0.3	4.6	-5.0	1.6	3.9
M06-L	-3.3	-8.0	-16.9	-7.2	-8.8	9.9	-4.6	-5.6	8.0
N12-SX	11.8	-14.1	5.7	-0.9	-6.1	-11.3	-17.8	-2.1	8.7
OreLYP	0.3	16.3	-1.7	10.5	7.3	24.8	13.0	-1.1	9.4
GAM	-7.6	4.6	-19.4	12.5	-4.4	20.6	6.3	-10.8	10.8
OLYP	-5.6	17.1	-11.3	6.4	2.3	23.9	11.6	-16.1	11.8
MN12-L	21.6	-16.7	-6.8	-16.9	-17.8	-4.2	-13.3	1.7	12.4
RPBE	-6.4	23.5	-21.5	5.9	1.7	22.7	10.7	-17.3	13.7
M05	-16.7	-19.5	-10.7	-6.3	-12.8	-11.0	-23.1	-11.9	14.0
BLYP	14.4	25.1	5.5	13.1	11.4	26.9	13.0	7.1	14.6
revPBE	-7.4	26.1	-22.1	6.9	2.6	24.8	12.6	-18.1	15.1
TPSSh	-25.5	-5.0	-32.0	-9.1	-17.9	-1.8	-10.3	-26.3	16.0
O3LYP	-29.3	-12.3	-28.6	-9.1	-20.1	-1.5	-10.9	-28.7	17.6
M06	-26.3	-23.5	-9.3	-10.6	-13.4	-14.0	-25.6	-18.8	17.7
PBE	2.7	37.3	-10.7	16.5	13.2	35.4	22.4	-3.6	17.7
B97-1	-18.8	-27.0	-10.1	-4.5	-18.5	-22.1	-27.8	-14.7	17.9
MGGA-MS2	-19.9	-18.3	-26.7	-12.0	-25.5	-6.4	-12.9	-21.3	17.9
MOHLYP	-26.4	-6.7	-36.1	-14.0	-20.6	0.9	-10.2	-29.6	18.1
M11-L	7.3	-20.9	-23.0	-31.5	-21.8	-27.1	-41.0	-1.7	21.8
MN15-L	-27.2	-24.1	-38.4	-9.2	-27.7	-5.5	-13.7	-30.0	22.0
MGGA-MS1	-27.9	-22.3	-32.2	-15.0	-29.4	-11.9	-17.9	-28.4	23.1
MN12-SX	20.0	-44.0	13.2	-13.4	-15.2	-31.7	-36.5	17.9	24.0
MGGA-MS0	-27.6	-26.5	-31.1	-15.8	-31.3	-16.3	-21.7	-26.2	24.6
SOGGA11	10.0	59.2	17.6	-7.8	38.5	32.4	28.3	15.0	26.1
MN15	-29.8	-28.7	-34.7	-14.8	-32.2	-13.1	-18.6	-38.4	26.3
SOGGA	9.0	53.8	-0.8	29.1	25.8	51.2	37.6	3.3	26.3
PBEsol	11.9	53.1	1.9	28.5	26.4	50.8	36.8	5.7	26.9
B3LYP	-32.9	-29.6	-30.4	-16.8	-30.4	-23.0	-30.8	-31.7	28.2
MPW3LYP	-32.6	-34.0	-29.3	-17.1	-31.8	-14.2	-21.4	-47.2	28.4
N12	12.2	52.0	16.7	25.6	28.0	50.4	35.3	9.9	28.8
B97-3	-35.7	-47.1	-24.5	-20.4	-35.4	-43.7	-47.3	-30.1	35.5
PW6B95	-46.5	-38.2	-41.3	-18.5	-37.8	-27.4	-31.8	-42.3	35.5
ωB97X	-26.8	-50.7	-28.0	-18.1	-39.6	-38.8	-44.9	-40.6	35.9
B97X-D	-39.8	-43.7	-33.3	-18.5	-38.3	-36.6	-42.2	-36.1	36.1
τ-HCTH	40.8	31.4	37.2	33.2	33.5	45.9	30.3	37.2	36.2
HSE06	-51.6	-33.3	-52.3	-21.3	-41.3	-26.0	-31.9	-49.4	38.4
PBE0	-52.6	-34.4	-52.5	-21.6	-42.1	-26.8	-32.3	-50.1	39.0
MGGA-MS2h	-37.4	-53.7	-40.2	-24.9	-40.8	-29.4	-33.9	-55.3	39.4
B1LYP	-42.8	-48.3	-39.1	-25.0	-43.7	-42.6	-48.5	-40.8	41.3
MPW1B95	-52.5	-43.0	-45.9	-20.2	-42.4	-31.8	-35.4	-64.0	41.9
M05-2X	-37.9	-81.9	-25.1	-13.1	-53.8	-71.9	-68.1	-51.0	50.4
M11	-70.3	-37.5	-71.5	-17.8	-49.1	-50.0	-49.4	-86.2	54.0
SOGGA11-X	-56.0	-78.7	-52.7	-27.0	-62.6	-55.1	-56.9	-52.6	55.2
M06-2X	-45.7	-87.7	-29.6	-34.1	-59.3	-102.1	-100.3	-58.3	64.6
PWB6K	-71.3	-76.3	-65.5	3.1	-71.0	-83.3	-82.1	-66.1	64.8
MPWB1K	-69.9	-70.5	-63.3	-32.2	-66.9	-75.7	-75.2	-87.4	67.6
M08-HX	-70.2	-82.7	-67.2	-26.7	-69.0	-72.6	-75.6	-89.3	69.2
MPW1K	-78.6	-70.3	-77.6	-39.6	-76.6	-82.1	-76.4	-54.4	69.5
M08-SO	-70.1	-77.8	-71.3	-26.4	-71.2	-77.7	-76.1	-91.2	70.2
M06-HF	-52.2	-113.1	-31.7	-44.8	-81.4	-104.2	-82.2	-57.6	70.9
Exptl. D_e	36.0	64.2	103.9	55.9	88.1	56.8	60.0	70.3	-

Table S5. The signed errors and mean unsigned errors (MUEs) for the calculated equilibrium bond dissociation energy ($D_e^{\text{opt-ECP}}$ in the units of kcal/mol) for various XC functionals, using the def2-QZVP basis combined with SDD ECP.

Functional	Cr ₂	V ₂	Mo ₂	Rh ₂	VNb	ScCo	YCo	NbCr	MUE
τ-HCTHhyb	-11.1	-7.7	7.0	5.1	0.5	9.5	-10.3	-1.9	6.7
M05	-20.4	12.6	8.6	2.9	10.6	14.0	-11.9	-1.7	10.3
M06-L	6.4	25.0	-7.8	9.3	11.3	24.6	-3.6	5.9	11.7
BLYP	5.1	25.9	4.5	11.0	9.0	31.0	6.5	1.1	11.8
MN15	-20.0	21.0	-14.6	1.7	-0.2	16.2	-8.6	-13.2	11.9
M06	-25.6	18.6	1.7	10.8	12.2	12.4	-13.5	-8.5	12.9
N12-SX	-13.7	-24.8	1.5	-3.0	-14.7	-17.4	-32.0	-4.2	13.9
OreLYP	-5.0	29.0	-1.9	10.3	11.4	40.2	13.0	-3.5	14.3
OLYP	-8.6	30.7	-11.4	5.9	6.9	38.4	11.3	-10.2	15.4
RPBE	-12.0	33.0	-20.3	4.8	4.3	31.3	5.8	-16.2	16.0
GAM	-18.4	21.0	-6.6	15.6	7.3	42.8	15.8	-6.0	16.7
revPBE	-12.8	35.1	-21.2	5.8	4.9	32.9	7.3	-17.1	17.1
MN15-L	-30.0	5.8	-37.4	5.5	-12.0	22.3	-1.7	-23.5	17.3
B97-1	-32.2	-20.2	-10.0	-9.8	-17.9	-11.2	-27.6	-20.0	18.6
O3LYP	-38.4	2.7	-29.9	-10.2	-14.4	13.3	-10.4	-32.9	19.0
MOHLYP	-27.8	8.4	-35.1	-14.9	-14.7	14.4	-11.1	-30.4	19.6
N12	1.7	39.9	20.7	35.7	21.7	36.1	13.2	4.9	21.8
TPSSh	-43.9	21.5	-36.8	-12.8	-9.5	5.7	-15.3	-36.5	22.8
PBE	-3.8	68.1	-10.1	15.4	26.2	43.7	17.5	-7.3	24.0
MPW3LYP	-48.9	-21.2	-31.4	-8.3	-22.9	-6.3	-24.7	-37.3	25.1
MGGA-MS2	-23.7	-18.5	-38.7	-17.0	-36.6	-13.0	-31.0	-28.7	25.9
SOGGA11	-11.2	45.1	14.5	12.1	27.5	60.0	37.1	0.9	26.1
SOGGA	5.1	65.6	-1.3	29.1	29.1	64.0	35.3	0.2	28.7
PBEsol	8.0	64.0	1.5	28.1	29.2	62.4	34.0	2.6	28.7
MN12-SX	-5.3	-69.2	29.7	1.8	-19.5	-40.1	-52.9	13.4	29.0
B3LYP	-48.1	-25.5	-32.0	-18.6	-29.5	-12.3	-30.7	-38.0	29.4
MGGA-MS0	-28.7	-9.9	-44.6	-19.3	-33.3	-26.4	-42.7	-32.3	29.7
MGGA-MS1	-32.4	-22.3	-44.3	-19.1	-39.7	-18.4	-35.9	-34.2	30.8
M11-L	-26.8	-36.3	-16.4	-9.6	-31.6	-45.0	-62.7	-18.5	30.9
PW6B95	-50.6	-20.2	-42.6	-21.0	-32.1	-16.5	-30.7	-46.3	32.5
B97-3	-55.4	-33.8	-28.7	-19.1	-31.8	-23.1	-39.5	-37.8	33.7
ωB97X	-51.5	-46.9	-26.0	-13.3	-35.2	-27.2	-42.5	-48.2	36.4
ωB97X-D	-59.6	-37.1	-33.3	-16.3	-35.7	-22.2	-38.0	-55.8	37.3
HSE06	-71.4	-20.8	-54.0	-21.8	-37.3	-16.4	-34.5	-43.3	37.4
MPW1B95	-73.5	-21.6	-47.8	-22.5	-35.3	-16.7	-33.3	-51.3	37.8
PBE0	-71.7	-20.6	-55.2	-23.7	-36.7	-16.3	-34.6	-56.9	39.5
M08-SO	-74.2	-23.8	-46.4	-14.6	-34.5	-31.0	-47.8	-54.9	40.9
MGGA-MS2h	-48.6	-38.1	-51.5	-25.6	-49.2	-28.9	-44.9	-44.7	41.4
B1LYP	-61.8	-44.0	-41.7	-26.7	-43.2	-28.4	-44.5	-43.8	41.8
MN12-L	16.4	-66.1	-13.6	-23.0	-47.0	-80.9	-90.4	8.6	43.2
M05-2X	-80.5	-62.9	-27.5	-25.5	-49.5	-47.2	-56.8	-49.9	50.0
M06-2X	-86.5	-71.5	-28.5	-35.9	-48.7	-46.1	-61.7	-56.1	54.4
MPWB1K	-75.4	-55.2	-67.9	-37.1	-55.0	-46.8	-57.3	-66.7	57.7
SOGGA11-X	-90.8	-58.0	-58.2	-20.5	-57.8	-56.0	-68.0	-68.2	59.7
τ-HCTH	31.1	48.4	40.4	111.0	41.7	101.6	70.8	34.8	60.0
PWB6K	-107.5	-56.0	-70.5	-25.9	-59.0	-53.7	-63.0	-46.7	60.3
M11	-110.6	-56.7	-72.6	-41.7	-54.5	-37.8	-48.0	-80.6	62.8
M08-HX	-104.3	-73.6	-54.0	-24.1	-63.2	-55.7	-65.7	-72.7	64.2
MPW1K	-113.6	-62.4	-84.9	-45.4	-63.7	-50.1	-62.2	-89.9	71.5
M06-HF	-145.8	-132.4	-31.9	-69.6	-71.8	-64.5	-69.3	-19.6	75.6
Exptl. D_e	36.0	64.2	103.9	55.9	88.1	56.8	60.0	70.3	-

Table S6. The signed errors and mean unsigned errors (MUEs) for the calculated equilibrium bond dissociation energy ($D_e^{\text{opt-DKH}}$ in the units of kcal/mol) for various XC functionals, using aug-cc-pwCVTZ-DK all-electron basis and DKH2.

Functional	Cr ₂	V ₂	Mo ₂	Rh ₂	VNb	ScCo	YCo	NbCr	MUE
τ-HCTHhyb	10.4	-3.1	2.4	10.9	0.2	5.5	-4.4	-21.5	7.3
N12-SX	10.9	-14.4	4.2	-1.4	-9.5	-10.5	-17.3	2.3	8.8
M06-L	-14.3	-7.2	-18.9	-9.2	-8.4	10.3	-4.4	-4.1	9.6
OreLYP	1.4	17.3	-2.0	10.5	8.0	25.2	13.3	-1.1	9.8
OLYP	-4.8	18.1	-11.9	6.4	3.0	24.3	11.8	-16.1	12.0
MN12-L	21.7	-17.5	-8.8	-16.1	-22.2	-3.1	-12.6	3.2	13.2
RPBE	-10.3	23.8	-22.1	5.9	1.8	22.8	10.7	-17.8	14.4
BLYP	14.4	25.2	5.5	13.2	11.4	27.0	13.0	7.1	14.6
GAM	-20.5	5.9	-22.8	12.2	-3.7	20.9	6.5	-26.9	14.9
M05	-33.8	-16.8	-13.2	-6.3	-10.8	-10.6	-22.7	-11.2	15.7
revPBE	-11.1	26.4	-22.6	6.9	2.8	24.8	12.6	-18.6	15.7
B97-1	1.1	-26.4	-12.1	-4.7	-21.3	-21.3	-27.2	-16.7	16.4
MGGA-MS2	-10.2	-18.3	-27.8	-11.8	-27.0	-6.2	-12.6	-21.9	17.0
PBE	0.0	37.8	-11.0	16.5	13.4	35.6	22.5	-3.6	17.6
MN15-L	0.5	-21.1	-43.1	-9.3	-25.4	-4.1	-12.3	-27.6	17.9
TPSSh	-10.4	-10.7	-34.1	-9.3	-44.1	-1.3	-9.9	-28.9	18.6
MOHLYP	-33.5	-6.3	-37.6	-13.7	-20.3	0.9	-10.2	-37.6	20.0
M06	-44.5	-22.8	-11.2	-14.7	-12.1	-13.3	-25.2	-18.4	20.3
O3LYP	-42.1	-10.1	-31.0	-9.3	-20.2	-0.5	-10.2	-50.2	21.7
MN12-SX	4.0	-43.9	10.2	-16.1	-22.2	-30.8	-35.8	18.1	22.6
MPW3LYP	-8.0	-33.6	-31.6	-17.5	-35.0	-13.5	-20.9	-30.4	23.8
M11-L	7.3	-21.9	-28.6	-34.3	-29.1	-25.7	-39.9	-10.3	24.6
MGGA-MS0	-30.7	-32.1	-32.8	-16.9	-34.1	-16.0	-21.3	-26.2	26.3
MGGA-MS1	-34.1	-28.7	-33.9	-15.8	-31.1	-11.6	-17.5	-37.7	26.3
SOGGA	7.3	54.9	-0.7	29.5	26.6	52.0	38.1	3.6	26.6
PBEsol	10.5	54.1	2.1	28.8	27.1	51.5	37.2	5.8	27.1
MN15	-49.1	-25.1	-39.7	-15.9	-32.2	-11.2	-16.7	-30.0	27.5
SOGGA11	10.1	59.0	17.5	-35.5	38.0	32.4	28.3	15.0	29.5
N12	15.7	53.5	17.9	25.7	29.0	51.3	35.8	11.7	30.1
B3LYP	-47.4	-33.0	-32.4	-16.9	-33.6	-22.4	-30.4	-32.5	31.1
MPW1B95	-16.0	-48.1	-50.0	-20.9	-43.0	-30.3	-34.2	-41.3	35.5
ωB97X	0.4	-53.0	-29.7	-15.2	-42.8	-37.2	-43.7	-62.3	35.5
τ-HCTH	34.2	33.4	36.1	33.3	34.8	46.9	30.8	37.2	35.8
PW6B95	-67.3	-37.6	-44.8	-19.4	-38.7	-26.3	-30.9	-37.8	37.8
ωB97X-D	-29.0	-45.8	-36.6	-17.2	-39.2	-35.3	-41.1	-65.8	38.7
HSE06	-16.2	-37.5	-56.6	-21.6	-41.6	-24.9	-31.0	-84.5	39.2
B97-3	-56.3	-47.3	-27.9	-18.2	-36.5	-42.6	-46.4	-47.4	40.3
B1LYP	-11.2	-48.1	-42.0	-25.0	-45.3	-41.9	-48.0	-75.5	42.1
MGGA-MS2h	-49.2	-44.5	-42.8	-21.0	-45.6	-28.8	-33.3	-92.0	44.6
PBE0	-74.3	-38.7	-57.1	-22.7	-45.8	-25.5	-31.2	-69.5	45.6
M11	-21.1	-49.2	-79.6	-19.9	-56.7	-50.1	-49.0	-109.0	54.3
PWB6K	-17.4	-91.6	-73.2	-1.3	-81.0	-81.4	-80.4	-77.2	62.9
M05-2X	-81.2	-87.9	-32.7	-14.4	-60.2	-68.0	-62.6	-96.9	63.0
SOGGA11-X	-89.5	-86.6	-58.5	-21.0	-67.7	-53.4	-55.4	-77.2	63.7
M08-HX	-113.0	-95.4	-76.1	-28.5	-76.9	-79.5	-74.8	-38.0	72.8
MPWB1K	-108.2	-95.9	-70.5	-35.8	-72.9	-73.7	-73.4	-54.6	73.1
MPW1K	-20.2	-85.0	-86.8	-44.5	-77.3	-80.1	-80.6	-112.3	73.3
M06-2X	-88.5	-91.9	-38.0	-36.5	-67.0	-97.8	-94.6	-103.7	77.2
M08-SO	-114.1	-90.3	-79.5	-28.3	-74.4	-77.2	-78.5	-104.0	80.8
M06-HF	22.3	-140.1	-45.7	-53.4	-75.5	-112.4	-94.4	-138.0	85.2
Exptl. D_e	36.0	64.2	103.9	55.9	88.1	56.8	60.0	70.3	-

