

Supplementary Table Captions STable 1. Atomic coordinates (x,y,z), isotropic displacement parameters and site occupancy factors and their estimated standard deviations found with the Rietveld refinement results from bulk samples of  $\text{Ba}_x\text{Cr}_5\text{Se}_8$

STable 2. Main distances extracted from Rietveld refinement on bulk samples of  $\text{Ba}_x\text{Cr}_5\text{Se}_8$

Supplementary Figure Caption:

SFigure 1. Temperature dependence of the magnetic susceptibility for  $\text{Ba}_x\text{Cr}_5\text{Se}_8$  measured under a magnetic field of 0.1 T for  $x = 0.5, 0.55$  and  $0.6$ . An antiferromagnetic transition is observed at 58 K, where the derivative of the curve is maximum. Only the 0.6 content sample shows a ferrimagnetic transition, with a transition temperature tending to the one of  $\text{Ba}_{1-p}\text{Cr}_2\text{Se}_4$ .

**STable 1. Atomic coordinates (x,y,z), isotropic displacement parameters and site occupancy factors and their estimated standard deviations found with the Rietveld refinement results from bulk samples of Ba<sub>x</sub>Cr<sub>5</sub>Se<sub>8</sub>**

Atoms	x = 0.5					x = 0.51					x = 0.52					x = 0.55				
	s.o.f	x	y	z	U <sub>iso</sub>	s.o.f	x	y	z	U <sub>iso</sub>	s.o.f	x	y	z	U <sub>iso</sub>	s.o.f	x	y	z	U <sub>iso</sub>
Ba(1)	0.874(7)	0	0	0	0.020(4)	0.906(7)	0	0	0	0.019(3)	0.904(7)	0	0	0	0.031(3)	0.861(8)	0	0	0	0.043(3)
Ba(2)	0.126(7)	0	0.5	0	0.025(4)	0.114(7)	0	0.5	0	0.019(3)	0.136(7)	0	0.5	0	0.031(3)	0.239(8)	0	0.5	0	0.043(3)
Cr(1)	1	0.996(2)	0.749(3)	0.510(2)	0.004(4)	1	0.999(2)	0.752(3)	0.506(3)	-0.001(4)	1	1.000(2)	0.746(3)	0.506(2)	0.004(3)	1	0.998(3)	0.745(3)	0.509(2)	0.006(3)
Cr(2)	1	0.5894(18)	0.397(5)	0.1543(17)	0.011(2)	1	0.5903(19)	0.399(5)	0.1559(17)	0.0059(17)	1	0.5909(19)	0.399(5)	0.1621(16)	0.0103(16)	1	0.590(2)	0.397(4)	0.1595(16)	0.0098(15)
Cr(3)	1	0.685(2)	-0.082(6)	0.5285(19)	0.014(3)	1	0.6862(19)	-0.080(5)	0.5286(17)	0.008(3)	1	0.688(2)	-0.076(6)	0.5210(16)	0.012(2)	1	0.686(2)	-0.083(4)	0.5230(17)	0.013(2)
Cr(4)	1	0.407(2)	0.096(5)	-0.1761(18)	0.011(2)	1	0.411(2)	0.101(5)	-0.1705(18)	0.0059(17)	1	0.411(2)	0.095(5)	-0.1692(16)	0.0103(16)	1	0.407(2)	0.091(4)	-0.1705(17)	0.0098(15)
Cr(5)	1	0.686(2)	0.419(6)	0.515(2)	0.014(3)	1	0.688(2)	0.423(5)	0.5129(18)	0.008(3)	1	0.684(2)	0.417(6)	0.5200(16)	0.012(2)	1	0.683(2)	0.412(4)	0.5197(17)	0.013(2)
Se(1)	1	0.8527(15)	0.969(4)	0.3330(13)	0.006(2)	1	0.8511(15)	0.966(3)	0.3388(13)	0.0026(18)	1	0.8526(14)	0.965(4)	0.3352(12)	0.0037(16)	1	0.8545(15)	0.968(3)	0.3341(13)	0.0024(16)
Se(2)	1	0.4832(14)	0.375(4)	0.6548(13)	0.0047(19)	1	0.4835(13)	0.375(3)	0.6576(13)	-0.0006(17)	1	0.4770(12)	0.372(4)	0.6627(11)	0.0043(16)	1	0.4777(13)	0.371(3)	0.6631(12)	0.0029(16)
Se(3)	1	0.6639(13)	0.169(4)	-0.0009(14)	0.0091(17)	1	0.6669(14)	0.166(4)	0.0045(15)	0.0050(15)	1	0.6639(13)	0.163(4)	0.0113(12)	0.0046(14)	1	0.6643(13)	0.160(3)	0.0124(12)	0.0035(13)
Se(4)	1	0.8290(15)	0.711(3)	0.6797(14)	0.0072(19)	1	0.8319(14)	0.708(3)	0.6812(13)	0.0032(18)	1	0.8309(13)	0.708(3)	0.6780(12)	0.0048(16)	1	0.8319(14)	0.712(3)	0.6768(13)	0.0044(15)
Se(5)	1	0.8532(15)	0.464(4)	0.3467(13)	0.006(2)	1	0.8560(15)	0.469(3)	0.3392(12)	0.0026(18)	1	0.8523(14)	0.467(4)	0.3419(11)	0.0037(16)	1	0.8502(14)	0.470(3)	0.3433(12)	0.0024(16)
Se(6)	1	0.4771(14)	-0.129(4)	0.6584(12)	0.0041(19)	1	0.4785(13)	-0.130(3)	0.6572(12)	-0.0006(17)	1	0.4823(12)	-0.132(4)	0.6494(11)	0.0043(16)	1	0.4824(13)	-0.129(3)	0.6508(11)	0.0029(16)
Se(7)	1	0.3318(13)	0.327(4)	-0.0111(12)	0.0091(17)	1	0.3327(14)	0.326(4)	-0.0046(14)	0.0050(15)	1	0.3315(13)	0.326(4)	0.0003(11)	0.0046(14)	1	0.3330(14)	0.324(3)	0.0023(12)	0.0035(13)
Se(8)	1	0.8320(15)	0.202(3)	0.6835(13)	0.0075(19)	1	0.8290(14)	0.204(3)	0.6825(13)	0.0032(18)	1	0.8294(13)	0.205(3)	0.6849(12)	0.0048(16)	1	0.8277(14)	0.206(3)	0.6852(13)	0.0044(15)

\* U<sub>iso</sub> fixed for Ba(1)-Ba(2), Cr(2)-Cr(4), Cr(3)-Cr(5), Se(1)-Se(5), Se(2)-Se(6), Se(3)-Se(7) and Se(4)-Se(8) as explicated in the main paper.

**STable 2. Main distances extracted from Rietveld refinement on bulk samples of  $\text{Ba}_x\text{Cr}_5\text{Se}_8$**

	at 1	at	x = 0.5 [12]	x = 0.51 [This work]	x = 0.52 [This work]	x = 0.55 [This work]
tunneled Ba-Se	Ba(1)	Se(4)	3.402(15)	3.402(14)	3.422(15)	3.414(13)
		Se(8)	3.359(16)	3.387(15)	3.374(15)	3.381(14)
	Ba(2)	Se(4)	3.429(16)	3.399(15)	3.425(15)	3.442(14)
		Se(8)	3.409(15)	3.411(14)	3.391(14)	3.388(13)
lowest and largest In-plane and in- chain Cr-Se	Cr(1)	Se(1)		2.45(3)		
		Se(4)	2.43(3)		2.46(3)	2.41(3)
		Se(8)	2.64(3)	2.60(3)	2.62(3)	2.66(3)
	Cr(2)	Se(3)		2.47(4)	2.47(4)	2.46(3)
		Se(7)	2.46(4)			
		Se(6)	2.64(4)	2.65(3)	2.66(3)	2.67(3)
		Se(4)	2.40(4)			2.41(3)
	Cr(3)	Se(8)		2.44(3)	2.46(4)	
		Se(2)	2.66(4)	2.70(3)	2.68(4)	2.64(3)
		Cr(1)	3.60(3)	3.56(3)	3.55(3)	3.54(3)
lowest In-plane and in-chain Cr- Cr	Cr(1)	Cr(3)	3.44(4)	3.47(4)	3.48(4)	3.45(4)
		Cr(5)	3.42(4)	3.44(3)	3.49(3)	3.49(3)
		Cr(2)	3.36(3)	3.38(3)	3.46(3)	3.44(3)
	Cr(2)	Cr(2)	3.36(3)	3.38(3)	3.46(3)	3.44(3)

		Cr(4)	3.53(3)	3.49(3)	3.55(6)	3.54(3)	
	Cr(3)	Cr(3)	3.83(4)	3.84(3)	3.86(4)	3.87(4)	
		Cr(5)	3.59(6)	3.59(5)	3.55(6)	3.57(5)	
		Cr(4)	Cr(4)	3.61(3)	3.55(3)	3.49(3)	3.51(3)
bridging		Cr(2)	Cr(5)	3.12(2)	3.09(2)	3.10(2)	3.12(2)
connection Cr-Cr		Cr(3)	Cr(4)	3.05(2)	3.10(2)	3.045(19)	3.05(2)