# Electronic Supplementary Information (ESI) 

for

# Muffin-like lanthanide complexes with an $\mathrm{N}_{5} \mathrm{O}_{2}$-donor macrocyclic ligand showing field-induced single-molecule magnet behaviour 

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Figure S1. A comparison of the X-ray powder diffraction patterns of compounds $\mathbf{2}$ (blue) and $\mathbf{3}$ (red).


Figure S2. (A) Molecular structure of the $\left[\mathrm{Dy}(\mathrm{L})\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{NO}_{3}\right)\right]^{2+}$ complex cation in 2. Thermal ellipsoids are drawn with $50 \%$ probability level. The hydrogen atoms are omitted for clarity. (B) The coordination geometry of the [ $\mathrm{DyN}_{5} \mathrm{O}_{4}$ ] core in 2.


Figure S3. Photoluminescence spectra of 1 (red line) and Tb"II complex of the parent $15-\mathrm{N}_{3} \mathrm{O}_{2}$ macrocyclic ligand without 2-pyridylmethyl pendant arms (dark blue) measured in acetonitrile/methanol solution ( $c=1 \times 10^{-3} \mathrm{~mol}$ $\mathrm{dm}^{-3}$ ) at room temperature. The $\mathrm{Tb}^{\text {III }}$ complex of $15-\mathrm{N}_{3} \mathrm{O}_{2}$ was prepared in situ by mixing of equimolar amounts of $\mathrm{Tb}\left(\mathrm{NO}_{3}\right)_{3} \cdot 5 \mathrm{H}_{2} \mathrm{O}$ and $15-\mathrm{N}_{3} \mathrm{O}_{2}$.


Figure S4. The analysis of the molar susceptibilities for 1-3 with Curie-Weiss law in the temperature range of 25-300 K. Empty circles - experimental data, full lines - calculated data.


Figure S5. The in-phase $\chi_{\text {real }}$ and out-of-phase $\chi_{\text {imag }}$ molar susceptibilities for $\mathbf{1 - 3}$ at zero static magnetic field (left) and in non-zero static magnetic field $B=0.1 \mathrm{~T}$ (right).


Figure S6. Top: frequency dependence of in-phase $\chi_{\text {real }}$ and out-of-phase $\chi_{\text {imag }}$ molar susceptibilities for $\mathbf{2}$ at $B_{\mathrm{DC}}$ $=0.1 \mathrm{~T}$. Full points - experimental data, full lines - fitted data using eq. 6. Bottom: Argand (Cole-Cole) plot and fit of resulting relaxation times according to Arrhenius law (red line), where only data having maxima in the Argand diagram were used.

1


2


3


Figure S7. Analysis of in-phase $\chi_{\text {real }}$ and out-of-phase $\chi_{\text {imag }}$ molar susceptibilities for $\mathbf{1 - 3}$ measured at the applied external field $B_{\mathrm{DC}}=0.1 \mathrm{~T}$ according to eq. 2 . Full points - experimental data, full lines - calculated data.

2


3


Figure S8. Representations of the geometries of $\left[\mathrm{Dy}(\mathrm{L})\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{NO}_{3}\right)\right]\left(\mathrm{NO}_{3}\right)_{2}(\mathbf{2}$, top $)$ and $\left[\mathrm{Er}(\mathrm{L})\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{NO}_{3}\right)\right]\left(\mathrm{NO}_{3}\right)_{2}$ ( $\mathbf{3}$, bottom) which were used in CASSCF calculations and easy axes of the ground state (KD1) and first excited (KD2) Kramer doublets. Dotted lines represent the O-H…O hydrogen bonds.

Table S1. Results of continuous shape calculations using program Shape 2.1 for complexes $\mathbf{1}$ and 2. ${ }^{\text {a }}$

|  | Tb(III) | Dy(III) |
| :--- | :---: | :---: |
| CN $=9^{\text {b }}$ |  |  |
| EP-9 | 34.013 | 34.075 |
| OPY-9 | 20.955 | 20.930 |
| HBPY-9 | 16.739 | 16.822 |
| JTC-9 | 14.546 | 14.581 |
| JCCU-9 | 9.017 | 9.046 |
| CCU-9 | 7.831 | 7.883 |
| JCSAPR-9 | 2.748 | 2.698 |
| CSAPR-9 | 1.785 | 1.748 |
| JTCTPR-9 | 4.116 | 4.043 |
| TCTPR-9 | 1.764 | 1.722 |
| JTDIC-9 | 11.193 | 11.214 |
| HH-9 | 10.386 | 10.420 |
| MFF-9 | 1.045 | 1.042 |

${ }^{a}$ the listed values correspond to the deviation between the ideal and real coordination polyhedra, the lowest values are given in red colour.
${ }^{\text {b }}$ EP-9 = enneagon, OPY-9 = octagonal pyramid, HBPY-9 = heptagonal bipyramid, JTC-9 = Johnson triangular cupola J3, JCCU-9 = capped cube J8, CCU-9 = spherical-relaxed capped cube, JCSAPR-9 = capped square antiprism, CSAPR-9 $=$ spherical capped square antiprism, JTCTPR-9 $=$ tricapped trigonal prism J51, TCTPR-9 = spherical tricapped trigonal prism, JTDIC-9 = tridiminished icosahedron, HH-9 = hula-hoop, MFF-9 = muffin.

Table S2. Selected hydrogen bonds and other non-covalent contacts in the crystal structures of $\mathbf{1}$ and $\mathbf{2}$.

| $\mathrm{D}-\mathrm{H} \cdots \mathrm{A}^{a}$ | $d(\mathrm{D} \cdots \mathrm{H})[\AA]$ | $d(\mathrm{H} \cdots \mathrm{A})[\AA \AA]$ | $d(\mathrm{D} \cdots \mathrm{A})[\AA]$ | $\vartheta(\mathrm{D} \cdots \mathrm{H})\left[{ }^{\circ}\right]$ |
| :--- | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ |  |  |  |  |
| $\mathrm{O}(3)-\mathrm{H}(3 \mathrm{~V}) \cdots \mathrm{O}(12)$ | 0.82 | 2.05 | 2.746 | 142.7 |
| $\mathrm{O}(3)-\mathrm{H}(3 \mathrm{~W}) \cdots \mathrm{O}(8)$ | 0.83 | 1.87 | 2.660 | 158.4 |
| $\mathrm{C}(11)-\mathrm{H}(11 \mathrm{~A}) \cdots \mathrm{O}(11)^{b}$ | 0.95 | 2.51 | 3.150 | 124.7 |
| $\mathrm{C}(13)-\mathrm{H}(13 \mathrm{~A}) \cdots \mathrm{O}(5)$ | 0.95 | 2.54 | 3.315 | 139.0 |
| $\mathrm{C}(17)-\mathrm{H}(17 \mathrm{~A}) \cdots \mathrm{O}(5)^{c}$ | 0.95 | 2.51 | 3.339 | 146.1 |
| $\mathrm{C}(24)-\mathrm{H}(24 \mathrm{~A}) \cdots \mathrm{O}(12)^{d}$ | 0.95 | 2.50 | 3.382 | 154.4 |
| $\mathrm{C}(19)-\mathrm{H}(19 \mathrm{~A}) \cdots \mathrm{N}(5)$ | 0.95 | 2.54 | 3.156 | 122.5 |
| $\mathrm{C}(3 \mathrm{~A})-\mathrm{H}(3 \mathrm{~A}) \cdots \mathrm{N}(8)^{e}$ | 0.99 | 2.45 | 3.325 | 147.6 |
| $\mathbf{2}$ |  |  |  |  |
| $\mathrm{O}(3)-\mathrm{H}(3 \mathrm{~V}) \cdots \mathrm{O}(11)$ | 0.82 | 2.03 | 2.750 | 145.1 |
| $\mathrm{O}(3)-\mathrm{H}(3 \mathrm{~W}) \cdots \mathrm{O}(8)$ | 0.83 | 1.90 | 2.662 | 151.9 |
| $\mathrm{C}(11)-\mathrm{H}(11 \mathrm{~A}) \cdots \mathrm{O}(5)$ | 0.95 | 2.54 | 3.316 | 138.8 |
| $\mathrm{C}(13)-\mathrm{H}(13 \mathrm{~A}) \cdots \mathrm{O}(10)^{f}$ | 0.95 | 2.50 | 3.143 | 125.1 |
| $\mathrm{C}(17)-\mathrm{H}(17 \mathrm{~A}) \cdots \mathrm{O}(11)^{g}$ | 0.95 | 2.51 | 3.391 | 153.9 |
| $\mathrm{C}(18)-\mathrm{H}(18 \mathrm{~A}) \cdots \mathrm{O}(8)^{h}$ | 0.95 | 2.67 | 3.356 | 130.0 |
| $\mathrm{C}(25)-\mathrm{H}(25 \mathrm{~A}) \cdots \mathrm{N}(4)$ | 0.95 | 2.54 | 3.148 | 122.3 |
| $\mathrm{C}(8 \mathrm{~A})-\mathrm{H}(8 \mathrm{~A}) \cdots \mathrm{N}(8)^{e}$ | 0.99 | 2.45 | 3.326 | 147.4 |

${ }^{a}$ Symmetry transformations used to generate equivalent atoms: ${ }^{b} x,-y+1, z+1 / 4 .{ }^{c} x,-y, z+1 / 4 .{ }^{d}-x, y-1, z-1 / 4 .{ }^{e}$ $x+1,-y+1, z+1 / 4 .{ }^{f} x,-y+2, z+1 / 4 .{ }^{g}-x+1, y+1, z-1 / 4 .{ }^{h} x-1,-y+1, z+1 / 4$.

Table S3. Parameters of one-component Debye model for the Dy ${ }^{\text {III }}$ complex 2 derived according to eq. 1 in the main text.

| $T / K$ | $\chi_{\mathrm{S}} /\left(10^{-6} \mathrm{~m}^{3} \mathrm{~mol}^{-1}\right)$ | $\chi_{\mathrm{T}} /\left(10^{-6} \mathrm{~m}^{3} \mathrm{~mol}^{-1}\right)$ | $\alpha$ | $\tau /\left(10^{-4} \mathrm{~s}\right)$ |
| ---: | ---: | ---: | :---: | ---: |
| 1.9 | 2.148 | 63.462 | 0.378 | 46.817 |
| 2.2 | 4.743 | 53.209 | 0.316 | 17.579 |
| 2.5 | 0.002 | 47.464 | 0.358 | 4.242 |
| 2.8 | 3.734 | 41.807 | 0.255 | 1.648 |
| 3.1 | 21.593 | 39.314 | 0.258 | 1.984 |

Table S4 Energy levels ( $\mathrm{cm}^{-1}$ or K ) of the lowest ligand field multiplets in zero magnetic field derived from CASSCF/DKH2/SINGLE_ANISO calculations of $\left[\mathrm{Tb}(\mathrm{L})\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{NO}_{3}\right)\right]\left(\mathrm{NO}_{3}\right)_{2} \mathbf{1}$ with the respective $g$-factors derived for each Kramer's doublet with the effective spin $1 / 2$.

| Energy <br> $\left(\mathrm{cm}^{-1}\right)$ | Energy <br> $(\mathrm{K})$ | $g_{\mathrm{x}}$ | $g_{\mathrm{Y}}$ | $g_{\mathrm{z}}$ |
| :--- | :--- | :--- | :--- | :---: |
| 0.000 | 0.000 | 0.000000103 | 0.000000273 | 16.675081359 |
| 0.695 | 1.000 |  |  |  |
| 23.137 | 33.289 |  |  |  |
| 27.367 | 39.375 |  |  |  |
| 67.869 | 97.648 |  |  |  |
| 83.357 | 119.931 |  |  |  |
| 99.152 | 142.657 |  |  |  |
| 126.438 | 181.915 |  |  |  |
| 140.271 | 201.818 |  |  |  |
| 199.698 | 287.319 |  |  |  |
| 204.141 | 293.712 |  |  |  |
| 376.397 | 541.548 |  |  |  |
| 376.714 | 542.004 |  |  |  |

Table S5 Energy levels ( $\mathrm{cm}^{-1}$ or K ) of the lowest ligand field multiplets in zero magnetic field derived from CASSCF/DKH2/SINGLE_ANISO calculations of $\left[\mathrm{Dy}(\mathrm{L})\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{NO}_{3}\right)\right]\left(\mathrm{NO}_{3}\right)_{2} \mathbf{2}$ with the respective $g$-factors derived for each Kramer's doublet with the effective spin 1/2.

| Energy <br> $\left(\mathrm{cm}^{-1}\right)$ | Energy <br> $(\mathrm{K})$ | $g_{\mathrm{x}}$ | $g_{\curlyvee}$ | $g_{z}$ |
| :--- | :--- | :---: | :---: | :---: |
| 0 | 0.000 | 0.123208278 | 0.401662841 | 19.214014361 |
| 38.243 | 55.023 | 0.356141137 | 0.826105795 | 18.433216066 |
| 113.567 | 163.397 | 3.918803592 | 4.811990429 | 12.560372284 |
| 150.540 | 216.592 | 1.850824694 | 2.945792689 | 13.510993216 |
| 190.234 | 273.703 | 7.954737034 | 5.663277147 | 3.008111909 |
| 296.665 | 426.832 | 0.459719199 | 0.947727009 | 14.713092241 |
| 332.608 | 478.546 | 0.139527338 | 0.371625830 | 18.288261450 |
| 391.878 | 563.822 | 0.247472833 | 0.431595384 | 17.241550158 |

Table S6 Energy levels ( $\mathrm{cm}^{-1}$ or K ) of the lowest ligand field multiplets in zero magnetic field derived from CASSCF/DKH2/SINGLE_ANISO calculations of $\left[\mathrm{Er}(\mathrm{L})\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{NO}_{3}\right)\right]\left(\mathrm{NO}_{3}\right)_{2} 3$ with respective $g$-factors derived for each Kramer's doublet with the effective spin $1 / 2$.

| Energy <br> $\left(\mathrm{cm}^{-1}\right)$ | Energy <br> $(\mathrm{K})$ | $g_{\mathrm{x}}$ | $g_{\gamma}$ | $g_{\mathrm{z}}$ |
| :--- | :--- | :---: | :---: | :---: |
| 0.000 | 0.000 | 1.123801903 | 2.180915307 | 13.849557162 |
| 47.928 | 68.957 | 0.771485743 | 2.219025733 | 11.176748604 |
| 69.830 | 100.469 | 3.012527039 | 5.223582763 | 8.198121785 |
| 133.220 | 191.673 | 1.949056313 | 2.887259140 | 10.494647672 |
| 159.320 | 229.225 | 1.280224132 | 4.288008015 | 8.089948499 |
| 213.909 | 307.766 | 8.967453663 | 5.443248836 | 0.007673973 |
| 269.653 | 387.968 | 0.225782405 | 3.578347299 | 7.125835001 |
| 319.015 | 458.989 | 1.252656637 | 5.766399195 | 12.068693060 |

