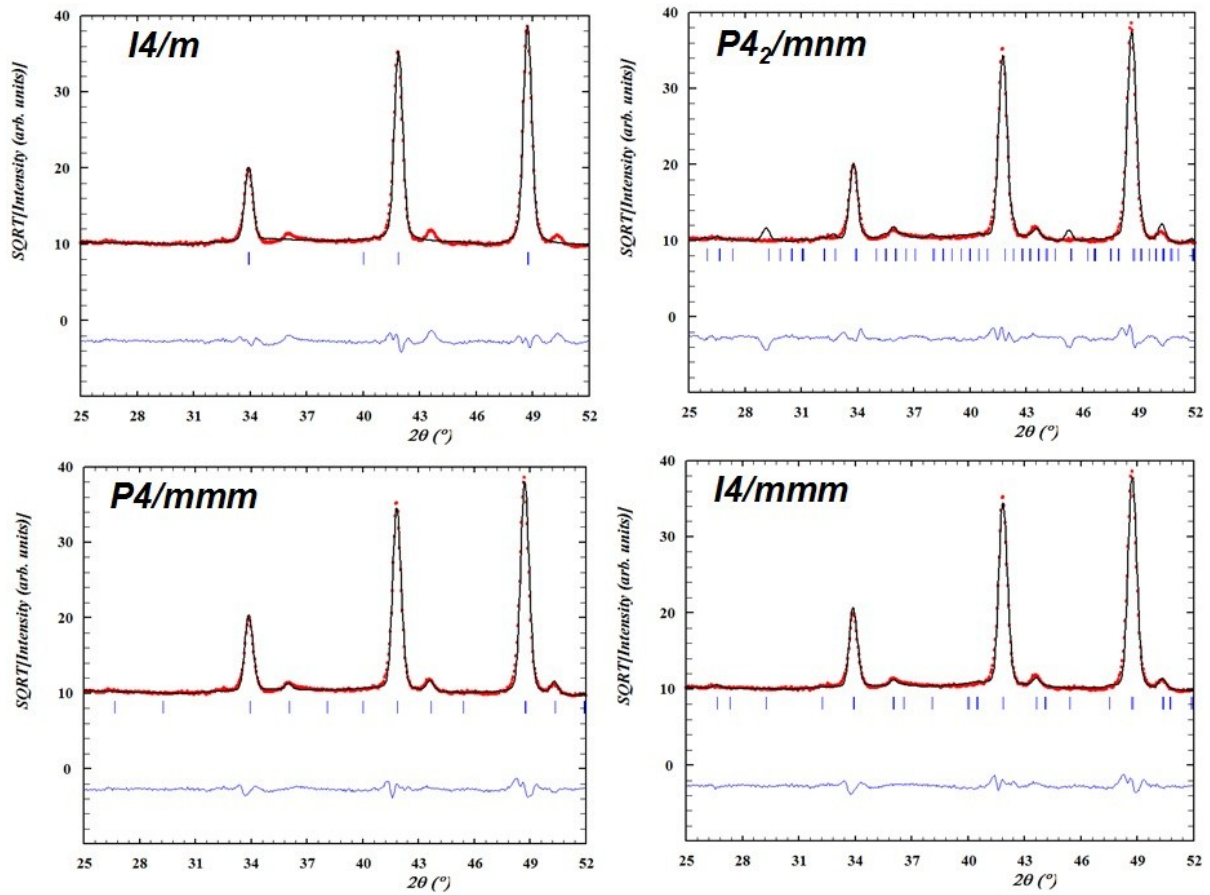


Atom	Wickoff position	x	y	z	Biso(Å <sup>2</sup> )	Occ.
Sr	1a	0.00	0.00	0.00	0.63(4)	1
Co/Fe	1b	0.50	0.50	0.50	0.69(6)	1
O	3c	0.50	0.00	0.50	0.5	2.63

**Table S1.** Structural parameters obtained by the Rietveld's refinement of the x-ray powder diffraction data using the cubic *Pm-3m* space group. Occupation factors were fixed to the structural formula values. Fe and Co cations could not be distinguished because of their similar scattering factors.



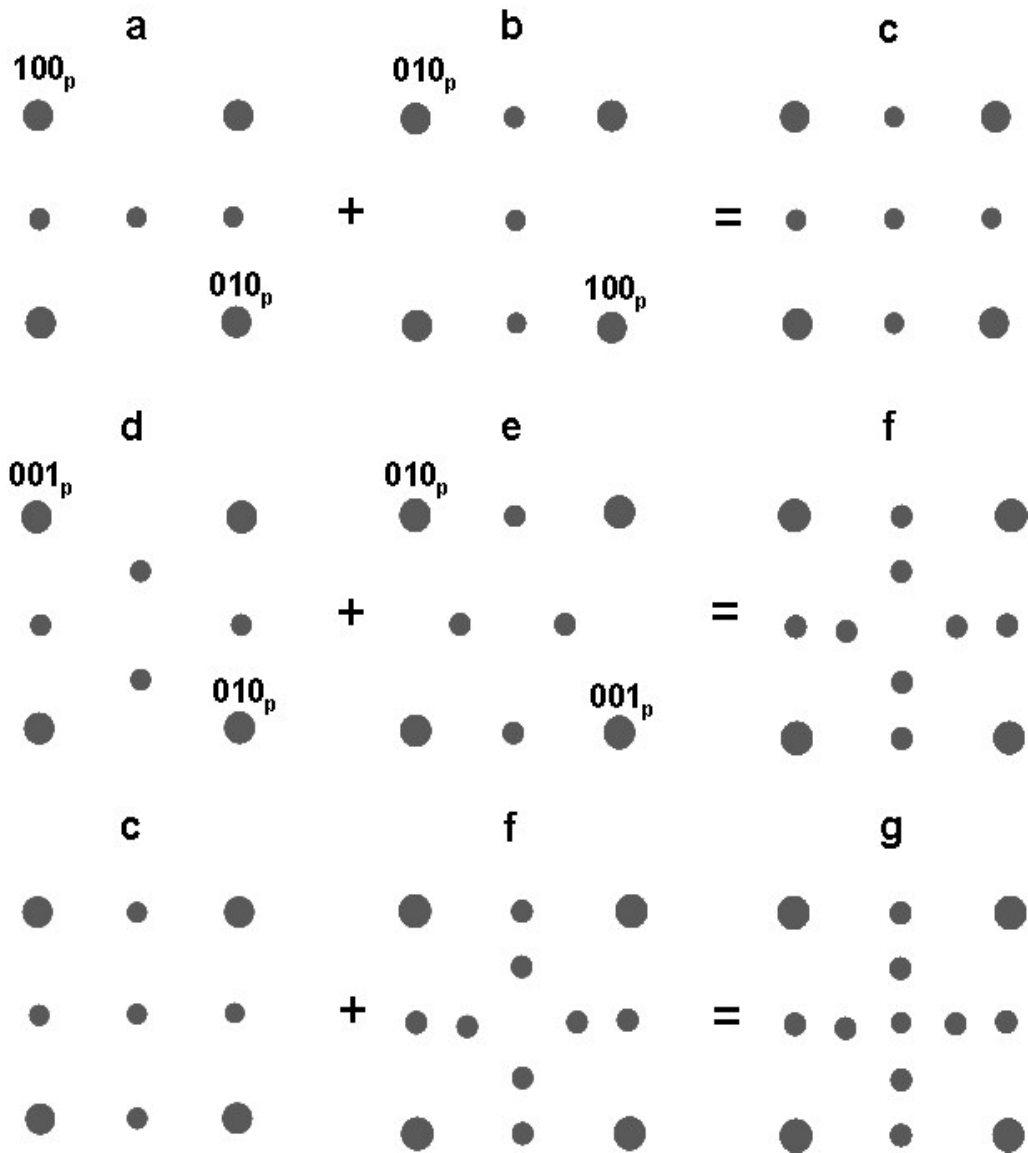
**Figure S-1.** Experimental (red dot) and calculated (thin solid line) neutron diffraction patterns at RT (D2B, ILL  $\lambda=1.594\text{\AA}$ ) for  $\text{SrFe}_{0.25}\text{Co}_{0.75}\text{O}_{2.63}$  material on a particular angular window. The vertical bars indicate calculated Bragg peak positions for nuclear structures for

- (a) Model based on  $I4/m$ ,  $a = b = a_p \sqrt{2}$  and  $c = 2 a_p$
- (b) Model based on  $P4_2/mnm$ ,  $a = b = 2 a_p \sqrt{2}$  and  $c = 4 a_p$
- (c) Model based on  $P4/mmm$ ,  $a = b = a_p$  and  $c = 2 a_p$
- (d) Model based on  $I4/mmm$ ,  $a = b = 2a_p$  and  $c = 4 a_p$

**Table S2.** The  $P4/mmm$  tetragonal SG is characteristic of the “ $\text{Sr}_2\text{B}_2\text{O}_{5.5}$ ” oxygen-vacancy ordering model.

Unit cell with lattice parameters  $a=3.86034(2) \text{ \AA} \approx a_p$ ,  $c=7.7318(1)\text{\AA} \approx 2a_p$  ( $a_p$ : lattice parameter of the cubic perovskite subcell). The agreement factors are  $\chi^2=3.36$ ,  $R_{wp}(\%)=7.01$ ,  $R_p(\%)=5.43$ ,  $R_{bragg}(\%)=11.7$  and  $R_f(\%)=12.5$ . Atomic positions, thermal factors and occupancies obtained by Rietveld refinement of the neutron powder diffractogram using the tetragonal  $P4/mmm$  space group and referring to the  $\text{Sr}_2\text{B}_2\text{O}_{5.5}$  model.

Atom	Wickoff position	x	y	z	Biso ( $\text{\AA}^2$ )	Occ.
Sr1	2g	0.0000	0.0000	0.2610(3)	1.00(3)	1.00
Co1/Fe1	1c	0.5	0.5	0.0000	0.6(1)	0.740(5)/0.260(5)
Co2/Fe2	1d	0.5	0.5	0.5	0.7(1)	0.760(5)/0.240(5)
O1	2h	0.5	0.5	0.2352(6)	2.6(1)	0.90(1)
O2	2f	0.0000	0.5	0.0000	2.3(3)	0.72(1)
O3	2e	0.5	0.0000	0.5	0.81(4)	1.0



**Figure S-2.** displays schematic representations of planes of the reciprocal lattice along different zone axis and different orientations of a crystal with a  $2\sqrt{2}a_p \times 2\sqrt{2}a_p \times 4a_p$  unit cell.

The pattern represented in Fig. S2c (similar to the SAED pattern in Fig. 3a) is a combination of the patterns represented in Fig. S2a and S2b. The pattern in Fig. S2f is a combination of the patterns in Fig. S2d and S2e. The pattern represented in Fig. S2g (similar to the SAED pattern in Fig. 3b) is a combination of the patterns represented in Fig. 2c and f. According to these representations, the FFT in Fig. 3 (similar to the SAED pattern in Fig. 2b) corresponds to Fig. S2g, which indicates that the crystal is formed by four different domains with  $2\sqrt{2}a_p \times 2\sqrt{2}a_p \times 4a_p$  unit cell perpendicularly oriented. Fig. 4 shows a single domain of a crystal along the  $[100]_p$  zone axis and the FFT corresponds to Fig. S2d and the FFT in Fig. 5 (similar to the SAED pattern in Fig. 2a) correspond to the representation in Fig. S2c.