## Supplementary Information for:

## New Family of Room Temperature Quantum Spin Hall Insulators in Two-Dimensional Germanene films

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Fig. S1. Orbital-resolved band structures with SOC of (a) $\mathrm{GeC}_{2} \mathrm{~F}$ and (b) $\mathrm{GeC}_{2} \mathrm{Cl}$ under the value of strain $\varepsilon=0.0 \%, 2.0 \%, 4.0 \%$ respectively. (c) $\mathrm{GeC}_{2} \mathrm{Br}$ presents orbital-resolved band structures with SOC under the value of strain $\varepsilon=-4.0 \%,-2.0 \%$, $0.0 \%$ respectively. The red dots represent the contributions from the $s$ atomic orbital of Ge atom and the blue dots represent contributions from the $p_{\mathrm{x}}$ and $p_{\mathrm{y}}$ atomic orbitals of Ge atom.


Fig. S2 The calculated energy gaps at $\Gamma$ point $\left(E_{\Gamma}\right)$ and the global energy gap $\left(E_{\mathrm{g}}\right)$ of $\mathrm{GeC}_{2} \mathrm{~F}$ (a), $\mathrm{GeC}_{2} \mathrm{Cl}$ (b) and $\mathrm{GeC}_{2} \mathrm{Br}$ (c) with SOC as a function of external strain by GGA method. The energy gaps at $\Gamma$ point $\left(E_{\Gamma}\right)$ and the global energy gap $\left(E_{\mathrm{g}}\right)$ of $\mathrm{GeC}_{2} \mathrm{~F}(\mathrm{~d}), \mathrm{GeC}_{2} \mathrm{Cl}$ (e) and $\mathrm{GeC}_{2} \mathrm{Br}$ (f) with SOC as a function of external strain by HSE method. Insets in panel show the trend of band gaps of TI phase as a function of external strain.


Fig. S3 Total (left panel) and spin (right panel) edge density of states for (a) $\mathrm{GeC}_{2} \mathrm{~F}$, (b) $\mathrm{GeC}_{2} \mathrm{Cl}$ and (c) $\mathrm{GeC}_{2} \mathrm{Br}$. In the spin edge plot, red/blue lines denote the spin up/down polarization.


Fig. S4 Calculated electronic band structures of the zigzag-type nanoribbons of (a) $\mathrm{GeC}_{2} \mathrm{~F}(\varepsilon=8.0 \%) ;(\mathrm{b}) \mathrm{GeC}_{2} \mathrm{Cl}(\varepsilon=8.0 \%)$; and (d) $\mathrm{GeC}_{2} \mathrm{Br}(\varepsilon=0 \%)$ with SOC.


Fig. S5 The orbital-resolved band structures with SOC for (a) $\mathrm{GeC}_{2} \mathrm{~F} @ \mathrm{BN}$, (b) $\mathrm{GeC}_{2} \mathrm{Cl} @ \mathrm{BN}$ and (c) $\mathrm{GeC}_{2} \mathrm{I} @ \mathrm{BN}$, respectively.


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