

## Supporting Information

Quantitative NMR of quadrupolar nucleus as a novel analytical method

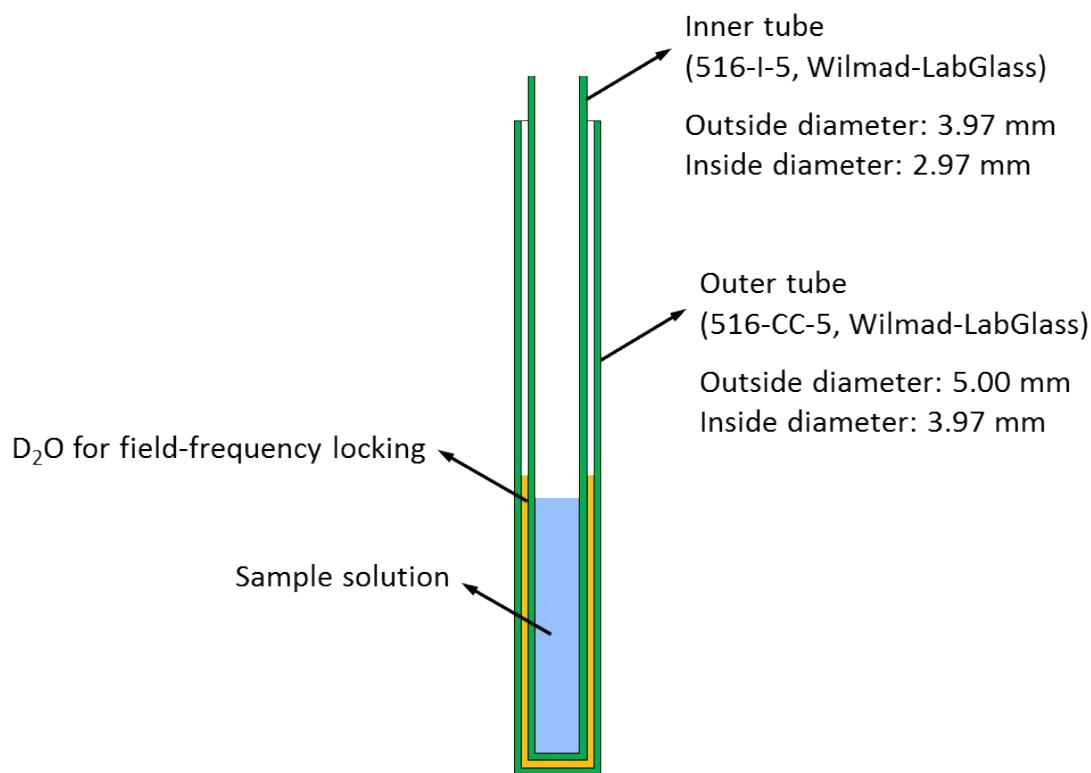
: Hydrolysis behavior analysis of aluminum ion

Hideshi Maki<sup>a,b\*</sup>, Genki Sakata<sup>b</sup>, Minoru Mizuhata<sup>b</sup>

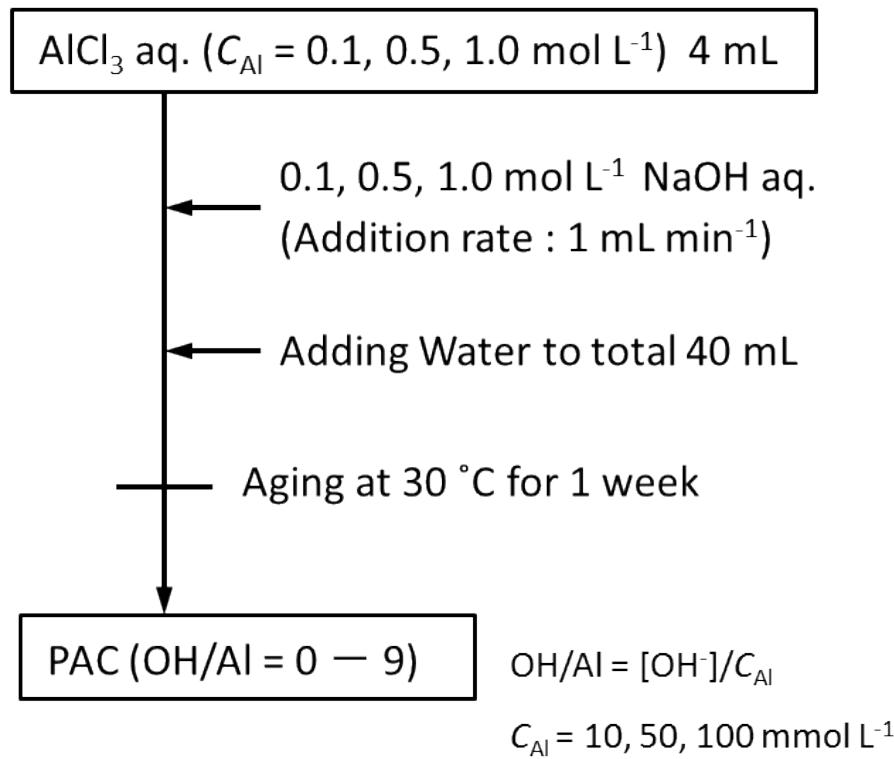
<sup>a</sup>Center for Environmental Management, Kobe University, 1-1 Rokkodai-cho, Nada-ku,  
Kobe 657-8501, Japan

<sup>b</sup>Department of Chemical Science and Engineering, Graduate School of Engineering,  
Kobe University, 1-1 Rokkodai-cho, Nada-ku, Kobe 657-8501, Japan

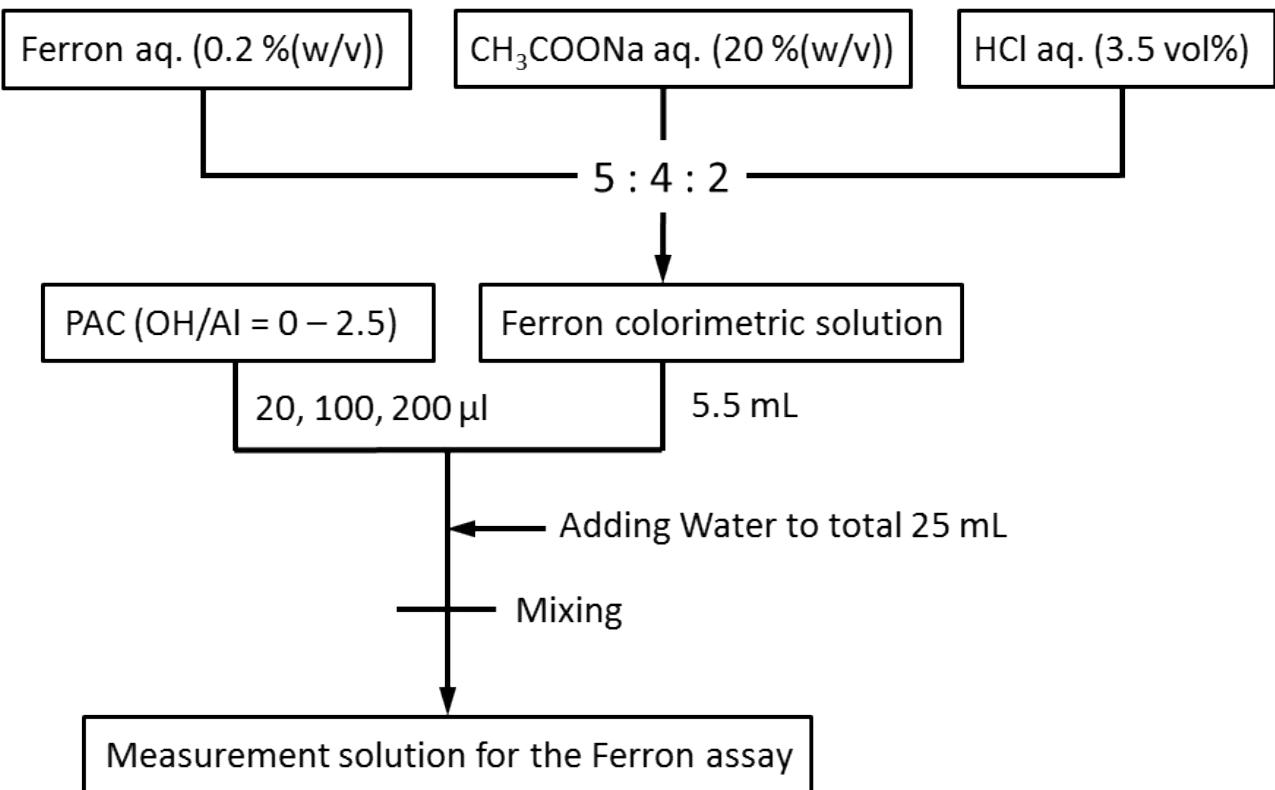
\*Corresponding author: maki@kobe-u.ac.jp



Scheme S1. Coaxial NMR tube system to avoid the contamination of  $D_2O$  for field-frequency locking into the sample solutions.



Scheme S2. Preparation of PAC sample solutions.



Scheme S3. Preparation of measurement solution for the Ferron assay.

Table S1. All raw data for the relationships between the integrated intensities per FID scan ( $I_{\text{freeAl}}$ ) of  $^{27}\text{Al}$  NMR signals due to  $[\text{Al}(\text{H}_2\text{O})_6]^{3+}$  ion in  $x \text{ molL}^{-1} \text{ Al}(\text{NO}_3)_3 + 0.1 \text{ molL}^{-1} \text{ HNO}_3$  aq. ( $x = \text{ca. } 0.1 - 1 \text{ mol L}^{-1}$ ) at  $30^\circ\text{C}$  and the  $[\text{Al}(\text{H}_2\text{O})_6]^{3+}$  concentrations ( $C_{\text{freeAl}}$ ) as shown in Figs. 1(a) and 1(b). The  $I_{\text{freeAl}}$  values are converted into the values before the input into the RF amplifier in an NMR spectrometer (i.e., corresponding to the receiver gain of 0 dB).

$C_{\text{freeAl}}$ (mmolL $^{-1}$ )	$\log(C_{\text{freeAl}})$ (mmolL $^{-1}$ )	$I_{\text{freeAl}}$	$\log(I_{\text{freeAl}})$
0.1173	-0.931	$1.512 \times 10^2$	2.18
0.212	-0.673	$4.49 \times 10^2$	2.65
0.446	-0.351	$8.16 \times 10^2$	2.91
0.594	-0.226	$1.015 \times 10^3$	3.01
0.959	-0.01800	$1.571 \times 10^3$	3.20
2.19	0.340	$3.60 \times 10^3$	3.56
3.51	0.546	$6.17 \times 10^3$	3.79
5.55	0.744	$9.53 \times 10^3$	3.98
7.20	0.858	$1.236 \times 10^4$	4.09
8.85	0.947	$1.475 \times 10^4$	4.17
20.0	1.301	$3.01 \times 10^4$	4.48
40.0	1.602	$6.38 \times 10^4$	4.80
60.0	1.778	$8.99 \times 10^4$	4.95
80.0	1.903	$1.232 \times 10^5$	5.09
100.0	2.00	$1.656 \times 10^5$	5.22
197.7	2.30	$3.26 \times 10^5$	5.51
368	2.57	$6.05 \times 10^5$	5.78
568	2.75	$9.30 \times 10^5$	5.97
752	2.88	$1.265 \times 10^6$	6.10
935	2.97	$1.602 \times 10^6$	6.20

Table S2. All raw data for the NMR measurement parameter dependences of the integrated intensities of  $^{27}\text{Al}$  NMR signal ( $I_{\text{freeAl}}$ ) due to  $[\text{Al}(\text{H}_2\text{O})_6]^{3+}$  ion in 0.1 mol L<sup>-1</sup>  $\text{Al}(\text{NO}_3)_3 + 0.1 \text{ mol L}^{-1} \text{ HNO}_3$  aq. at 30 °C as shown in Figs. 2(a) and 2(b). The  $I_{\text{freeAl}}$  values for Fig. 2(a) are converted into the values before the input into the RF amplifier in an NMR spectrometer (i.e., corresponding to the receiver gain of 0 dB). The integrated intensities for Fig. 2(b) are the values per FID scan.

(a) Number of FID scans dependence

Number of FID scans	$I_{\text{freeAl}}$
8	$1.335 \times 10^6$
32	$5.31 \times 10^6$
128	$2.13 \times 10^7$
512	$8.54 \times 10^7$
2048	$3.41 \times 10^8$
8192	$1.361 \times 10^9$

(b) Receiver gain dependence

Receiver gain (dB)	$I_{\text{freeAl}}$
6	$3.42 \times 10^5$
10	$5.46 \times 10^5$
16	$1.084 \times 10^6$
20	$1.763 \times 10^6$
26	$3.35 \times 10^6$
30	$5.32 \times 10^6$
36	$1.111 \times 10^7$
40	$1.671 \times 10^7$
46	$3.41 \times 10^7$
50	$5.48 \times 10^7$
56	$1.041 \times 10^8$
60	$1.660 \times 10^8$

Table S3. All raw data for the effect of the sample solution temperature on the relationships between the integrated intensities per FID scan of  $^{27}\text{Al}$  NMR signals due to  $[\text{Al}(\text{H}_2\text{O})_6]^{3+}$  ion in  $x$  mol L $^{-1}$   $\text{Al}(\text{NO}_3)_3 + 0.1$  mol L $^{-1}$   $\text{HNO}_3$  aq. ( $x = \text{ca. } 1 - 1000$  mmol L $^{-1}$ ) and the  $[\text{Al}(\text{H}_2\text{O})_6]^{3+}$  ion concentrations as shown in Figs. 3(a), 3(b), and 3(c). The  $I_{\text{freeAl}}$  values are converted into the values before the input into the RF amplifier in an NMR spectrometer (i.e., corresponding to the receiver gain of 0 dB).

(a) 21.4 °C (i.e., room temperature)

$C_{\text{reeAl}}$ (mmol L $^{-1}$ )	$\log (C_{\text{reeAl}})$ (mmol L $^{-1}$ )	$I_{\text{freeAl}}$	$\log (I_{\text{freeAl}})$
1.020	0.00860	$1.675 \times 10^3$	3.224
2.55	0.4065	$4.26 \times 10^3$	3.629
5.10	0.7076	$8.56 \times 10^3$	3.932
8.16	0.9117	$1.340 \times 10^4$	4.127
10.20	1.0086	$1.752 \times 10^4$	4.244
25.5	1.4065	$4.36 \times 10^4$	4.640
51.0	1.7076	$8.73 \times 10^4$	4.941
81.6	1.912	$1.376 \times 10^5$	5.139
102.0	2.009	$1.847 \times 10^5$	5.267
204	2.310	$3.42 \times 10^5$	5.534
408	2.611	$6.95 \times 10^5$	5.842
612	2.787	$1.023 \times 10^6$	6.010
816	2.912	$1.409 \times 10^6$	6.149
1020	3.009	$1.829 \times 10^6$	6.262

(b) 30 °C

$C_{\text{reeAl}}$ (mmol L <sup>-1</sup> )	$\log (C_{\text{reeAl}})$ (mmol L <sup>-1</sup> )	$I_{\text{freeAl}}$	$\log (I_{\text{freeAl}})$
1.020	0.00860	$1.751 \times 10^3$	3.243
2.55	0.4065	$4.00 \times 10^3$	3.602
5.10	0.7076	$8.51 \times 10^3$	3.930
8.16	0.9117	$1.337 \times 10^4$	4.126
10.20	1.0086	$1.697 \times 10^4$	4.230
25.5	1.4065	$4.29 \times 10^4$	4.632
51.0	1.7076	$8.28 \times 10^4$	4.918
81.6	1.912	$1.350 \times 10^5$	5.130
102.0	2.009	$1.819 \times 10^5$	5.260
204	2.310	$3.30 \times 10^5$	5.518
408	2.611	$6.84 \times 10^5$	5.835
612	2.787	$1.008 \times 10^6$	6.004
816	2.912	$1.397 \times 10^6$	6.145
1020	3.009	$1.718 \times 10^6$	6.235

(c) 40 °C

$C_{\text{reeAl}}$ (mmol L <sup>-1</sup> )	$\log (C_{\text{reeAl}})$ (mmol L <sup>-1</sup> )	$I_{\text{freeAl}}$	$\log (I_{\text{freeAl}})$
1.020	0.00860	$1.728 \times 10^3$	3.237
2.55	0.4065	$4.05 \times 10^3$	3.608
5.10	0.7076	$8.01 \times 10^3$	3.903
8.16	0.9117	$1.244 \times 10^4$	4.095
10.20	1.0086	$1.587 \times 10^4$	4.201
25.5	1.4065	$4.03 \times 10^4$	4.606
51.0	1.7076	$7.93 \times 10^4$	4.899
81.6	1.912	$1.277 \times 10^5$	5.106
102.0	2.009	$1.676 \times 10^5$	5.224
204	2.310	$3.15 \times 10^5$	5.498
408	2.611	$6.31 \times 10^5$	5.800
612	2.787	$9.61 \times 10^5$	5.983
816	2.912	$1.319 \times 10^6$	6.120
1020	3.009	$1.649 \times 10^6$	6.217

Table S4.  $^{27}\text{Al}$  spin-lattice and spin-spin relaxation times, i.e.,  $T_1$  and  $T_2$ , of all aluminum species were determined by the inversion recovery<sup>40,41</sup> and the CPMG procedure<sup>42-44</sup>. Total concentration of aluminum ( $C_{\text{Al}}$ ) is 100 mmol L<sup>-1</sup>.

Chemical shift	0 ppm	4.0 ppm	62.5 ppm	80 ppm
Species	$[\text{Al}(\text{H}_2\text{O})_6]^{3+}$	$\text{Al}_3$	$\text{K-Al}_{13}$	$\text{Al}(\text{OH})_4^-$
$T_1$ (s)	0.035*	0.0014*	0.040*	0.013**
$T_2$ (s)	0.028*	0.0015*	0.034*	0.011**

\*Determined from the sample solution of OH/Al = 1.25

\*\* Determined from the sample solution of OH/Al = 4.0

Table S5. Fitting parameters and reaction rate constant,  $k$ , which were derived from a nonlinear least squares curve fitting method by the Ferron assay of PAC aqueous solutions after aging for 1 week at 30 °C.

(a)  $C_{\text{Al}} = 10 \text{ mmol L}^{-1}$

OH/Al	$A_0$	$A_\infty$	$A_1$	$A_2 (A_\infty - A_0)$	$k_{\text{b1}}$	$k_{\text{b2}}$	$R$
0	0.6195	0.6195	0.10407	0.08706	0.06992	0.0003217	0.94493
0.25	0.6038	0.6038	0.12627	0.14479	0.08261	0.0006955	0.98416
0.50	0.4211	0.6049	0.09437	0.18386	0.06458	0.0007862	0.99732
0.75	0.3575	0.6035	0.09765	0.2460	0.06689	0.0007310	0.99855
1.00	0.3369	0.6060	0.05104	0.2691	0.03981	0.0008570	0.99915
1.25	0.2672	0.5941	0.06389	0.3269	0.004192	0.0006971	0.99846
1.50	0.2174	0.5913	0.02435	0.3740	0.02190	0.0009467	0.99955
1.75	0.16400	0.5888	0.015752	0.4248	0.015287	0.0007925	0.99987
2.00	0.08985	0.5530	0.008229	0.4632	0.005048	0.0008749	0.99972
2.25	0.05528	0.5120	0.010663	0.4567	0.005728	0.0008047	0.99982
2.50	0.02796	0.2437	0.007243	0.2158	0.003333	0.0007019	0.99968

(b)  $C_{\text{Al}} = 50 \text{ mmol L}^{-1}$

OH/Al	$A_0$	$A_\infty$	$A_1$	$A_2 (A_\infty - A_0)$	$k_{\text{b1}}$	$k_{\text{b2}}$	$R$
0	0.5307	0.6362	0.14077	0.10554	0.08851	0.0003644	0.88508
0.25	0.4467	0.6248	0.19666	0.17808	0.11930	0.0006671	0.95170
0.50	0.4375	0.6215	0.11327	0.18405	0.07564	0.0007569	0.99327
0.75	0.3926	0.6010	0.06683	0.2084	0.05035	0.0008850	0.99754
1.00	0.3853	0.6089	0.017868	0.2235	0.007634	0.0008993	0.99874
1.25	0.2785	0.5983	0.05081	0.3198	0.03886	0.0009583	0.99879
1.50	0.2358	0.5878	0.018443	0.3520	0.016507	0.0009977	0.99950
1.75	0.17947	0.5915	0.014217	0.4121	0.011904	0.0010337	0.99952
2.00	0.11594	0.5759	0.012572	0.4600	0.007566	0.0010691	0.99958
2.25	0.05709	0.5842	0.0144	0.5271	0.004990	0.0010608	0.99996
2.50	0.02796	0.2437	0.007243	0.2158	0.003333	0.0007019	0.99968

(c)  $C_{\text{Al}} = 100 \text{ mmol L}^{-1}$

OH/Al	$A_0$	$A_\infty$	$A_1$	$A_2 (A_\infty - A_0)$	$k_{\text{b1}}$	$k_{\text{b2}}$	$R$
0	0.5527	0.6409	0.10405	0.08824	0.07064	0.0004093	0.95192
0.25	0.5535	0.6284	0.06248	0.07483	0.04912	0.0004495	0.99029
0.50	0.4999	0.6307	0.06622	0.13078	0.04930	0.0007246	0.99605
0.75	0.4226	0.6104	0.06912	0.18782	0.05072	0.0008799	0.99638
1.00	0.3808	0.6170	0.05163	0.2362	0.03986	0.0009378	0.99704
1.25	0.3036	0.6182	0.06082	0.3147	0.04484	0.00092114	0.99846
1.50	0.2615	0.6212	0.02837	0.3598	0.02505	0.00099744	0.99924
1.75	0.19763	0.5985	0.016816	0.4009	0.014226	0.0010621	0.99935
2.00	0.13216	0.6018	0.019884	0.4696	0.013553	0.0010489	0.99925
2.25	0.07495	0.5951	0.01534	0.5202	0.006760	0.0010835	0.99951
2.50	0.06341	0.3969	0.03926	0.3335	0.02276	0.0008521	0.99620

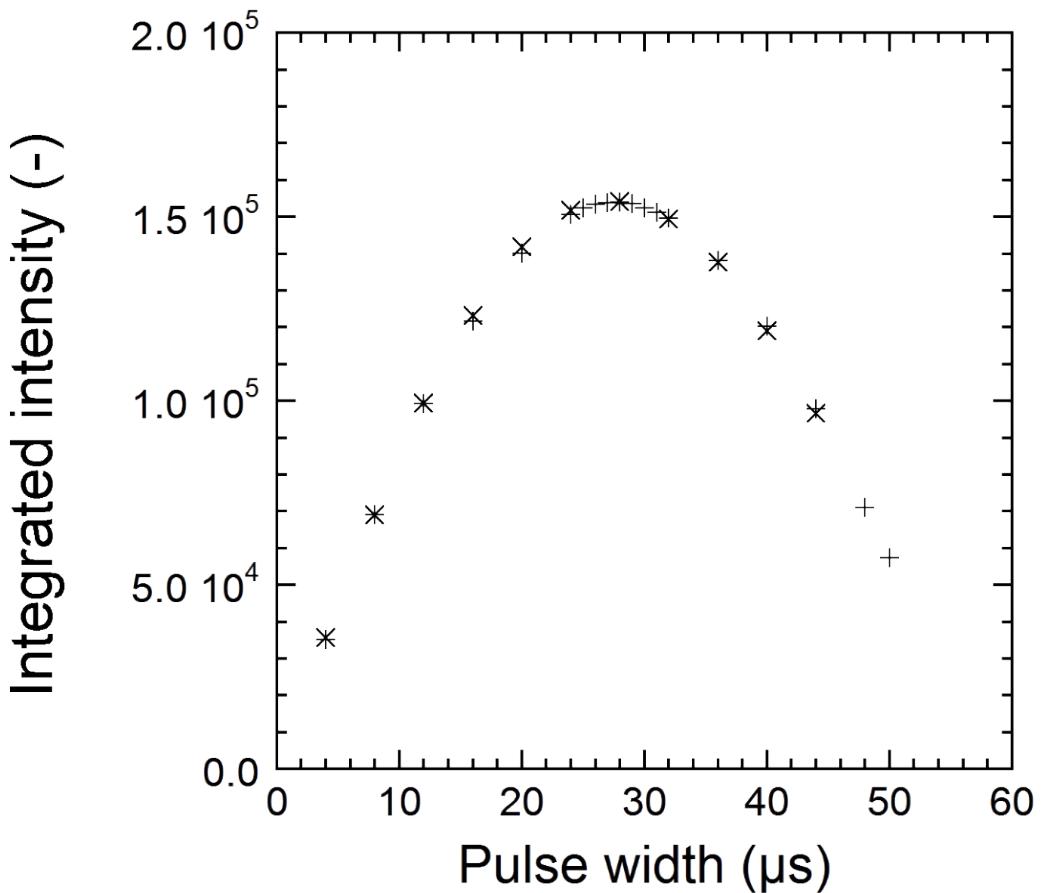
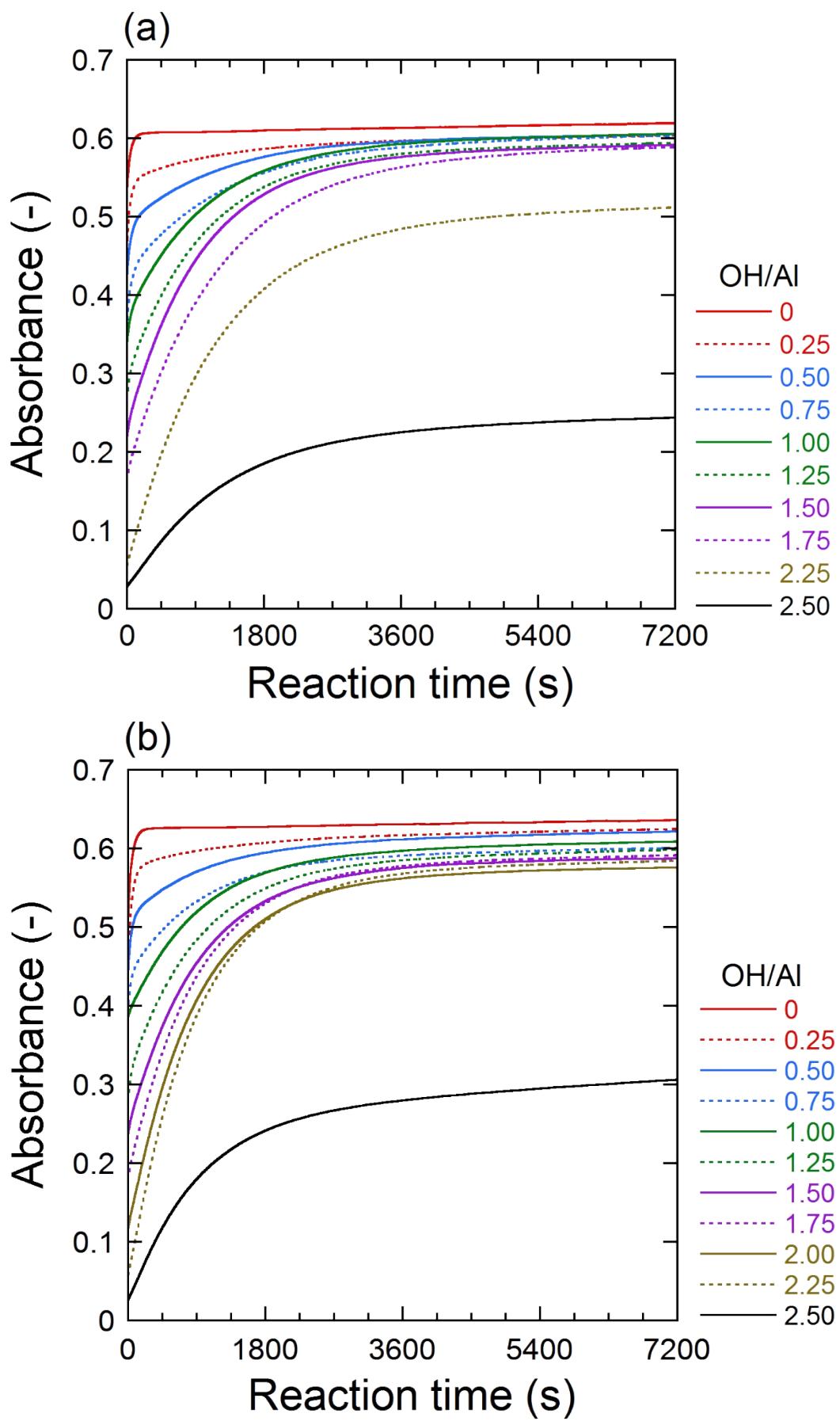


Fig. S1. Influence of anionic species on the pulse width dependence of the integrated intensities per FID scan ( $I_{\text{freeAl}}$ ) of  $^{27}\text{Al}$  NMR signals due to  $[\text{Al}(\text{H}_2\text{O})_6]^{3+}$  ion at 30 °C. The  $I_{\text{freeAl}}$  values are converted into the values before the input into the RF amplifier in an NMR spectrometer (i.e., corresponding to the receiver gain of 0 dB). Sample solution: (+) 0.1 mol L<sup>-1</sup>  $\text{Al}(\text{NO}_3)_3$  + 0.1 mol L<sup>-1</sup>  $\text{HNO}_3$ , (×) 0.1 mol L<sup>-1</sup>  $\text{AlCl}_3$  + 0.1 mol L<sup>-1</sup>  $\text{HCl}$ .



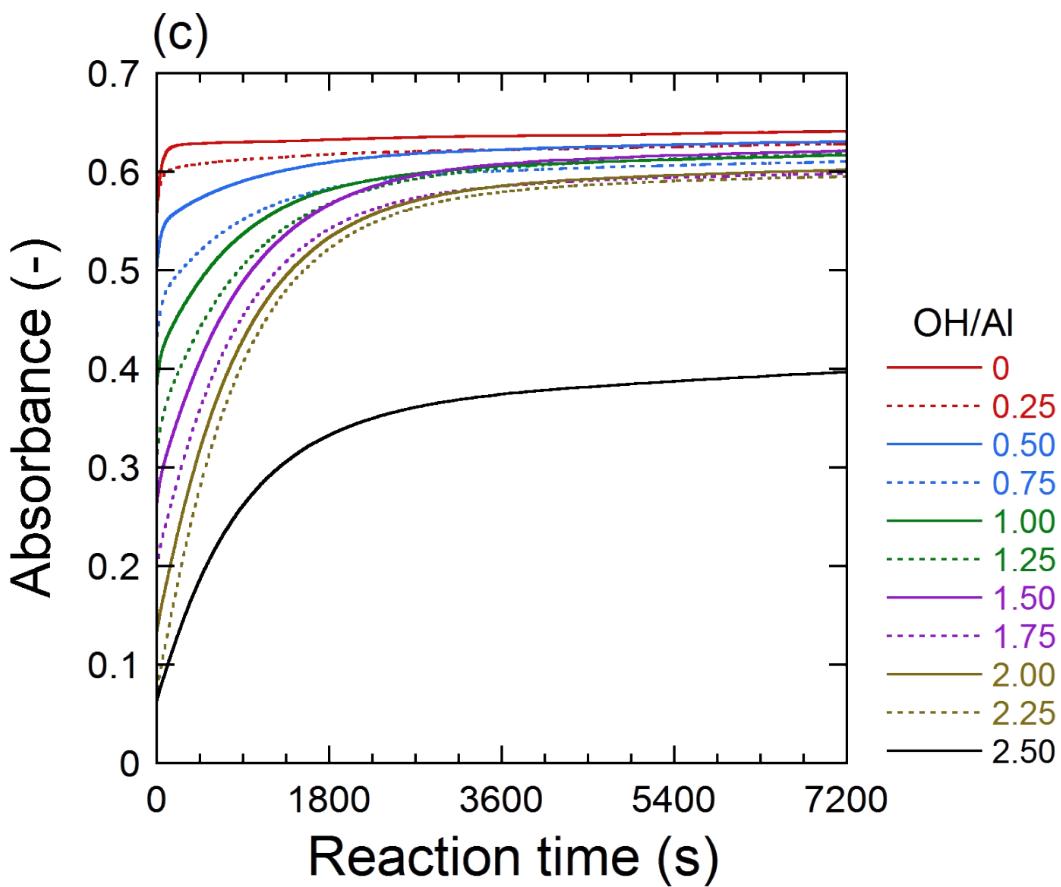


Fig. S2. Time course of absorbance for the Ferron assay of PAC aqueous solutions after aging for 1 week at 30 °C. Total concentration of aluminum: (a) 10 mmol L<sup>-1</sup>, (b) 50 mmol L<sup>-1</sup>, (c) 100 mmol L<sup>-1</sup>.