## The investigation of Na-related defects in Cu<sub>2</sub>ZnSnSe<sub>4</sub> Miaomiao Han,<sup>1, 2</sup> Xiaoli Zhang<sup>1</sup> and Zhi Zeng<sup>1, 2, \*</sup>

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Table S1 Convergence test of cut-off energy (take full relaxation of Na<sub>Zn</sub> as an example).

E <sub>cutoff</sub> (eV)	E <sub>tot</sub> (eV)	Lattice constant (Å)		Average bond length (Å)		
		а	С	Cu-Se	Sn-Se	Zn-Se
370	-238.835	5.775	11.591	2.435	2.625	2.500
390	-283.826	5.775	11.593	2.435	2.625	2.500
410	-283.820	5.777	11.597	2.436	2.626	2.501

Fig. S2. Migration path of Na in Cu<sub>2</sub>ZnSnSe<sub>4</sub>1) Na<sub>i</sub>-->Na<sub>i</sub>2)Na<sub>i</sub>-->V<sub>Cu</sub>3) Na<sub>Cu</sub>-->V<sub>Cu</sub>4)Na<sub>Zn</sub>-->V<sub>Cu</sub>.



Fig. S1. The local density of states (LDOS) of NaCu, NaZn corresponding to the four nearest neighbor atoms around the substitutional Na with all the possible charge states in a 64-atom supercell using HSE06 functional. The energy is given referenced to the Fermi level.

