

# Combining random walk and regression models to understand solvation in multi-component solvent systems (Electronic Supplementary Information)

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## S1 Supplementary Information

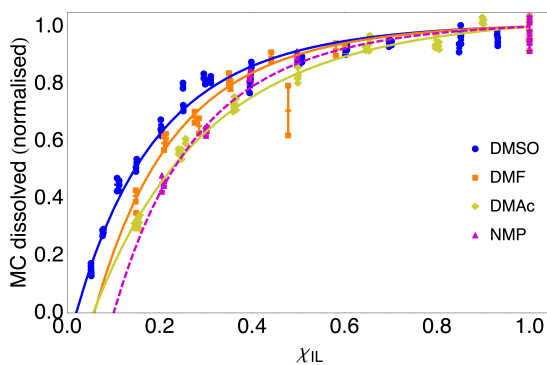


Figure S1: Typical dissolution profiles for selected organic electrolyte solutions (OES)s. Points are experimental data measured in pairs of over- and under-estimates of the maximum cellulose dissolvable, the lines are the 1-D random walk fits.

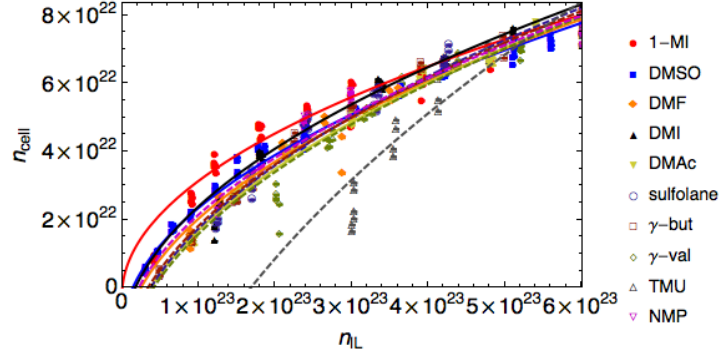


Figure S2: Number of cellobiose residues of cellulose,  $n_{cell}$  molecules (taken from molar fraction data) in a mole of mixture against the number of IL pairs. The fit is  $n_{cell} = d + \sqrt{m n_{IL}}$ . Points are experimental data measured in pairs of over- and under-estimates of the maximum cellulose dissolvable, the lines are the 1-D random walk fits.

Table S1: Coefficients for the  $n_{cell} vs n_{IL}$  fits. The equation used was:  $n_{cell} = d + m\sqrt{n_{IL}}$ . The norm of the residuals is given by  $R^2$ .

Dataset	d	m	$R^2$
1-MI	$-2.27001 \times 10^{21}$	$1.06328 \times 10^{11}$	0.994499
DMSO	$-1.40183 \times 10^{22}$	$1.18428 \times 10^{11}$	0.997986
DMF	$-2.01097 \times 10^{22}$	$1.27692 \times 10^{11}$	0.997576
DMI	$-1.70546 \times 10^{22}$	$1.29415 \times 10^{11}$	0.998327
DMAc	$-2.65143 \times 10^{22}$	$1.37092 \times 10^{11}$	0.998610
sulfolane	$-2.73645 \times 10^{22}$	$1.41466 \times 10^{11}$	0.996042
$\gamma$ -but	$-2.53112 \times 10^{22}$	$1.37517 \times 10^{11}$	0.996956
$\gamma$ -val	$-2.82255 \times 10^{22}$	$1.39164 \times 10^{11}$	0.998441
TMU	$-9.44975 \times 10^{22}$	$2.30376 \times 10^{11}$	0.985068
NMP	$-1.88558 \times 10^{22}$	$1.27419 \times 10^{11}$	0.995587

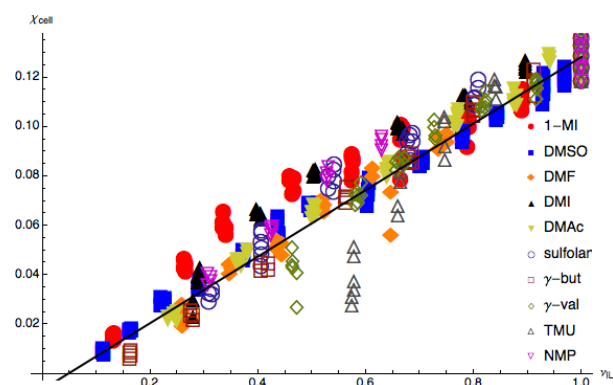


Figure S3: Molar fraction of cellobiose residues in dissolved cellulose versus volume fraction of ionic liquid (as calculated from molar volumes and molar fractions). The amount of cellulose dissolvable in a solution mixture is only related to the volume of IL available suggesting that a space-filling model of dissolution works. Fitted line equation given in Table 2 of the paper.

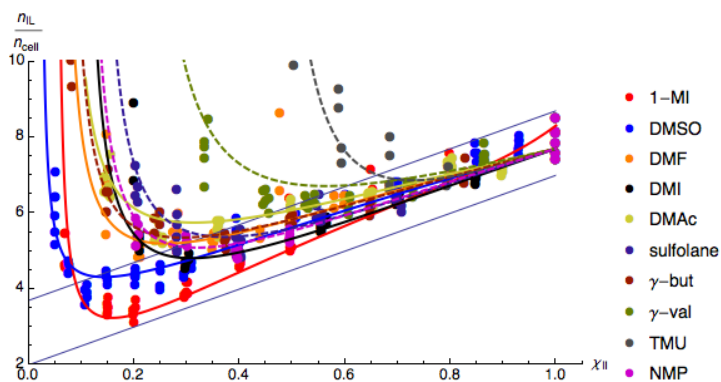


Figure S4: The number of ionic liquid pairs per cellobiose residue. Upper and lower boundaries (blue lines) are drawn at  $n_{IL}/n_{cell} = 1.8 + 1.5\chi_{IL}$  and  $n_{IL}/n_{cell} = 3.7 + 1.5\chi_{IL}$ .

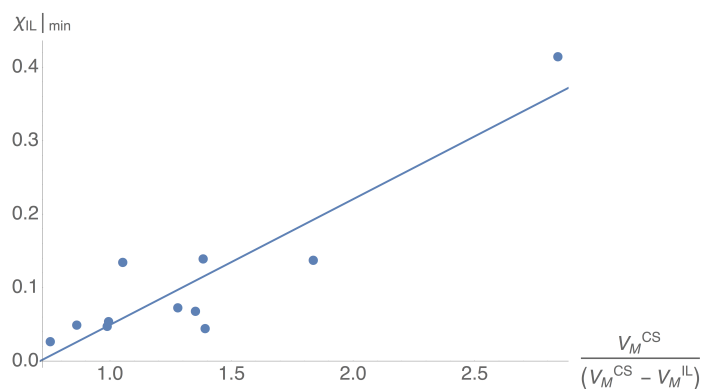


Figure S5: Linear fit of minimum  $\chi_{IL}$  to linearized CS molar volume.

Table S2: Molar volumes of tested co-solvents and ionic liquid.

Name	Key	Molar volume $\text{cm}^3\text{mol}^{-1}$
1-methylimidazole	1-MI	82.4
dimethylsulfoxide	DMSO	71.3
n,n-dimethylformamide	DMF	82.628
1,3-dimethylimidazolidin-2-one	DMI	107.3
n,n-dimethylacetamide	DMAc	93.02
sulfolane	Sulfolane	95.27
gamma-B542a-butyrolactone	$\gamma$ -But	76.8
gamma-valerolactone	$\gamma$ -Val	96.2
1,1,3,3-tetramethylurea	TMU	122.6
n-methylpyrrolidine-2-one	NMP	96.44
1-Ethyl-3-methylimidazolium acetate	[EMim][OAc]	165.735

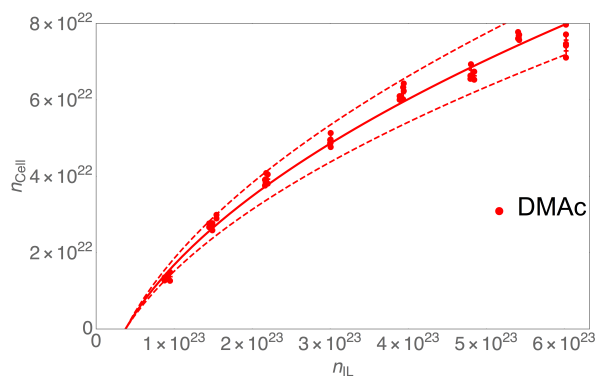


Figure S6: Sensitivity of the random walk model parameters. An example fitted model for DMAc is plotted with equations containing  $\pm 10\%$  of the fitted values. A small change in model parameters causes a small change in the model predictions

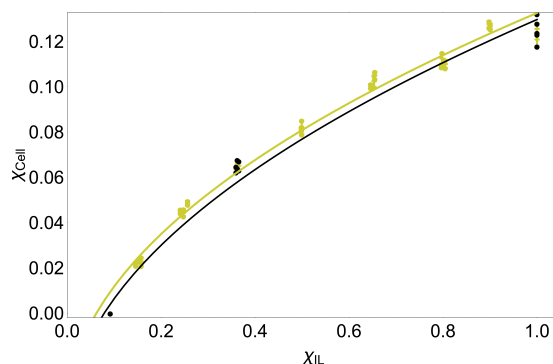


Figure S7: Using the random walk model for prediction of DMAc OES data. Yellow: fit (line) to all measured data (dots). Black: fit (line) to subset points (black dots). Only the measurement at around  $\chi_{IL} = 0.35$  needs to be measured, the point at  $\chi_{IL} = 1$  is known and the point at  $\chi_{cell} = 0$  can be estimated from equation 8. The single measurement fit differs from the actual data by only 7.1% on average.

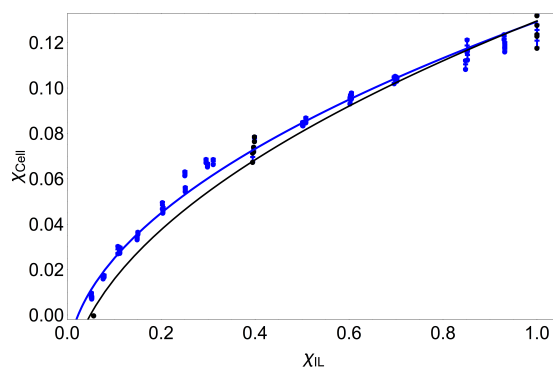


Figure S8: Using the random walk model for prediction of DMSO OES data. Blue: data (dotss) and fit (line) to all measured data. Black: fit (line) to measured or estimated points (dots). Only the measurement at around  $\chi_{IL} = 0.4$  needs to be measured, the point at  $\chi_{IL} = 1$  is known and the point at  $\chi_{cell} = 0$  can be estimated from equation 8. The single measurement fit differs from the actual data by only 9.4% on average.