Electronic supplementary information

Contents

Figure S1 Excitation schemes of IR-UV and UV-IR-UV spectroscopies.

Table S1 Comparison of bond lengths, binding energies of benzene (Bz) and the benzene dimer (Bz₂) obtained by (TD-)M06-2X/cc-pVDZ and (TD-)CAM-B3LYP/aug-cc-pVTZ with GD3BJ empirical dispersion correction levels of theory.

Table S2 Theoretical vibrational frequencies and assignments of Bz and Bz₂ in the S_0 and S_1 states calculated by the (TD-)M06-2X/cc-pVDZ level of theory.

Table S3 Comparison between the theoretical average frequencies of the S_0 and S_1 states of Bz and the EXC state of Bz₂ evaluated from values in Table S1.

Table S4 Theoretical vibrational frequencies and assignments of Bz and Bz₂ in the S_0 and S_1 states calculated by the (TD-)CAM-B3LYP/aug-cc-pVTZ level of theory with GD3BJ empirical dispersion correction.

Table S5 Comparison between the theoretical average frequencies of the S_0 and S_1 states of Bz and the EXC state of Bz₂ evaluated from values in Table S3.

Table S6 Comparison between the average frequencies of S_0 and S_1 states (v_{ave}) and EXC state (v_{EXC}) obtained by the (TD-)CAM-B3LYP/aug-cc-pVTZ level of theory with GD3BJ empirical dispersion correction. This is a table corresponding to Table 2 in the main text but with the CAM-B3LYP functional.

Figure S2 Comparison of vibration frequencies of (a) Bz in S_0 , (b) Bz in S_1 and (c) Bz₂ in S_1 states (SW structure) obtained by CAM-B3LYP/aug-cc-pVTZ and TD-CAM-B3LYP/aug-cc-pVTZ levels of theory with the GD3BJ empirical dispersion correction, and the experimental spectrum (d). This is a figure corresponding to Figure 5 in the main text but with the CAM-B3LYP functional.

Full expression of the excimer state vibrational energy, $E_{v_{\pm}}^{+/-'}$, derived from the secular determinant given by equation (34) in *Appendix*.



Figure S1 Excitation schemes of (a) IR-UV spectroscopy for a S₀ state and (b) UV-IR-UV spectroscopy for a S₁ state. In this work, v_{IR} was fired 50 ns prior to the two UV pulses ($\Delta t = 50$ ns) for the IR-UV spectroscopy, while v_{IR} was irradiated 15 ns after v_{exc} , and v_{ion} was fired 15 ns after v_{IR} ($\Delta t_1 = \Delta t_2 = 15$ ns) for the UV-IR-UV spectroscopy according to the lifetime of the S₁ state of Bz₂ (~40 ns).⁶⁴ v_{ion} was set to 270 nm for Bz and 285 nm for Bz₂, respectively.

Table S1 Comparison of C–C bond lengths in Bz (r_{C-C}), distances between centers of each Bz ring (r_{Bz-Bz}), binding energies of EXC (D_0) of benzene (Bz) and benzene dimer (Bz₂) obtained by (TD-)M06-2X/cc-pVDZ and (TD-)CAM-B3LYP/aug-cc-pVTZ with GD3BJ empirical dispersion correction levels of theory. Upper and lower rows of each parameter show results by M06-2X and CAM-B3LYP functionals, respectively. r_{Bz-Bz} means distance between centers of each Bz ring.

	Bz (S ₀)	Bz (S ₁)	Bz_2 (EXC, SW, D_{6h})	$Bz_2 (S_1(stem^*), T, C_{2v})$
	139.5	142.5	140.8	142.5 (stem); 139.5 (top)
<i>r</i> _{C–C} / pm	138.5	141.5	139.8	141.4 (stem); 138.5 (top)
			299.8	488.2
r _{Bz-Bz} ∕ pm			304.7	496.4
D / am^{-1}			4428	641
D_0 / cm			4113	845

Table S2 Theoretical (v_{calc}) vibrational frequencies and the assignments of Bz and Bz₂ in the S₀ and S₁ states calculated by normal mode analyses on the optimized structures obtained by M06-2X/cc-pVDZ and TD-M06-2X/cc-pVDZ level of theory, respectively.

^{a)} These are scaled values by 0.98 for skeletal vibrations and 0.95 for CH stretching vibrations, respectively. Values in parentheses are transition intensities in km/mol.

Bz (S ₀)		Bz (S ₁)		$Bz_2 (S_1, SW, D_{6h})$		$Bz_2 (S_1, T, C_{2v})$	
$v_{\rm calc}$ / cm ^{-1 a)}	assignments ^{b)}	$v_{\rm calc}$ / cm ^{-1 a)}	assignments	$v_{\rm calc}$ / cm ^{-1 a)}	assignments ^{b)}	$v_{\rm calc}$ / cm ^{-1 a)}	assignments
				66 (0)	\mathbf{R}_{z}	-26 (0)	\mathbf{R}_{y}
				104 (0)	$\beta_{(x, y)}$	-9 (0)	\mathbf{R}_{x}
				104 (0)	$\beta_{(x, y)}$	13 (0)	R _z
				118 (0.14)	$\mathbf{R}_{(x, y)}$	70 (0)	σ_z
				118 (0.14)	$\mathbf{R}(x, y)$	88 (0)	β _x
				152 (0)	σ_z	90 (0)	β_y
404 (0)	16 (e _{2u})	244 (0)	16	348 (0)	$16^{-}(e_{2g})$	241 (0)	16a (stem)
				366 (0)	$16^{+}(e_{2u})$	251 (0)	16b (stem)
		253 (0)	4			262 (0)	4 (stem)
						402 (0)	16b (top)
602 (0)	6 (e _{2g})			512 (0)	$6^{+}(e_{2g})$	403 (0)	16a (top)
		508 (0)	6	576 (0)	$6^{-}(e_{2u})$	505 (0)	6b (stem)
						514 (0)	6a (stem)
						549 (93)	11 (stem)
712 (0)	4 (b _{2g})			577 (0)	$4^{-}(b_{1u})$	561 (0)	10a (stem)
				596 (0)	$4^{+}(b_{2g})$	585 (0)	10b (stem)
678 (92)	11 (a _{2u})	553 (119)	11	625 (83)	$11^{+}(a_{2u})$	601 (0)	6a (top)
				643 (0)	$11^{-}(a_{1g})$	601 (0)	6b (top)
858 (0)	10 (e _{1g})	576 (0)	10	749 (0)	$10^{+} (e_{1g})$	681 (108)	11 (top)
				751 (7.2)	$10^{-}(e_{1u})$	708 (0)	4 (top)
						752 (0)	17a (stem)
						777 (0)	17b (stem)
981 (0)	17 (e _{2u})	765 (0)	17	875 (0)	$17^{-}(e_{2g})$	809 (0)	5 (stem)
				881 (0)	$17^{+}(e_{2u})$	859 (0)	10a (top)
						863 (0)	10b (top)
						964 (1)	1 (stem)
1012 (0)	5 (b _{2g})	807 (0)	5	900 (0)	$5^{-}(b_{1u})$	969 (1)	12 (stem)
				914 (0)	$5^{+}(b_{2g})$	974 (1)	18a (stem)
1018 (0)	1 (a _{1g})	963 (0)	1	914 (38)	$1^{-}(a_{2u})$	977 (3)	18b (stem)
987 (0)	12 (b _{1u})	963 (0)	12	978 (0)	$12^{-}(b_{2g})$	982 (0)	17a (top)

^{b)} +/- on the shoulder means the signs of the linear combinations, see text. Symmetry species in the D_{6h} point group are denoted in parentheses.

				979 (0)	$12^{+}(b_{1u})$	985 (0)	17b (top)
				993 (0)	$1^{+}(a_{1g})$	987 (0)	12 (top)
1048 (10)	18 (e _{1u})	976 (6)	18	1014 (8.6)	$18^{+}(e_{1u})$	1012 (0)	5 (top)
				1017 (0)	$18^{-}(e_{1g})$	1015 (0)	1 (top)
						1047 (4)	18a (top)
						1048 (5)	18b (top)
1129 (0)	15 (b _{2u})	1132 (0)	15	1132 (0)	$15^{-}(b_{1g})$	1128 (1)	15 (stem)
				1135 (0)	$15^{+}(b_{2u})$	1131 (0)	15 (top)
1162 (0)	9 (e _{2g})	1146 (0)	9	1135 (0)	$9^{-}(e_{2u})$	1139 (1)	9a (stem)
				1155 (0)	$9^{+}(e_{2g})$	1147 (2)	9b (stem)
						1161 (0)	9a (top)
						1164 (0)	9b (top)
1330 (0)	3 (a _{2g})	1315 (0)	3	1321 (0)	$3^{-}(a_{1u})$	1312 (0)	3 (stem)
				1321 (0)	$3^{+}(a_{2g})$	1327 (0)	14 (top)
1326 (0)	14 (b _{2u})	1573 (0)	14	1435 (0)	$14^{+}(b_{2u})$	1331 (0)	3 (top)
1486 (18)	19 (e _{1u})	1420 (14)	19	1449 (44)	$19^{+}(e_{1u})$	1415 (12)	19a (stem)
				1453 (0)	$19^{-}(e_{1g})$	1420 (5)	19b (stem)
						1484 (10)	19a (top)
						1486 (9)	19b (top)
				1454 (0)	$14^{-}(b_{1g})$	1572 (1)	14 (stem)
1649 (0)	8 (e _{2g})	1583 (0)	8	1541 (0)	$8^{-}(e_{2u})$	1582 (0)	8b (stem)
				1615 (0)	$8^{+}(e_{2g})$	1582 (0)	8a (stem)
						1644 (0)	8b (top)
						1645 (0)	8a (top)
3039 (0)	13 (b _{1u})	3064 (0)	13	3047 (0)	$13^{-}(b_{2g})$	3042 (0)	13 (top)
				3048 (0)	$13^{+}(b_{1u})$	3050 (0)	7b (top)
3048 (0)	7 (e _{2g})	3068 (0)	7	3052 (0)	$7^{+}(e_{2g})$	3053 (0)	7a (top)
				3055 (0)	$7^{-}(e_{2u})$	3061 (0)	13 (stem)
						3063 (0)	7b (stem)
						3064 (18)	20b (top)
3063 (52)	20 (e _{1u})	3084 (34)	20	3070 (0)	$20^{-}(e_{1g})$	3067 (18)	20a (top)
				3071 (68)	$20^{+}(e_{1u})$	3070 (13)	7a (stem)
						3075 (0)	2 (top)
						3079 (18)	20b (stem)
3072 (0)	2 (a _{1g})	3094 (0)	2	3076 (32)	$2^{-}(a_{2u})$	3087 (5)	20a (stem)
				3082 (0)	$2^{+}(a_{1g})$	3115 (3)	2 (stem)

Table S3 Comparison between the theoretical average frequencies of the S₀ and S₁ states (v_{ave}) and the EXC state (v_{EXC}) calculated at M06-2X/cc-pVDZ and TD-M06-2X/cc-pVDZ level of theory with GD3BJ empirical dispersion correction, respectively. The second column lists frequencies in the EXC state, v_{EXC} , and absolute values of splitting of the modes, $|\Delta v_{EXC}(+/-)| = |v_{EXC}(+) - v_{EXC}(-)|$, and percentage of the splitting to the average frequencies $\langle v_{EXC} \rangle = (v_{EXC}(+) + v_{EXC}(-))/2$. The third column shows deviations from the average values ($\Delta v = v_{EXC} - v_{ave}$) and percentages of difference to the average values.

	···· 1		
Mode	$v_{\rm ave}$ / cm ⁻¹	$v_{\rm EXC}$ / cm ⁻¹	$\Delta v / \mathrm{cm}^{-1}$
Widde	$(v(S_0); v(S_1); \Delta v(S_1/S_0))$	$(\Delta v_{\text{EXC}}(+/-) ; \Delta v_{\text{EXC}}(+/-) /\langle v_{\text{EXC}}\rangle)$	$(\Delta v / v_{ave})$
v_{16}	324	241(-), 251(+)	-83, -73
(e _{2u} ; op)	(404; 244; -160)	(10; 4.1 %)	(-26 %, -23 %)
v_6	555	512(+), 576(-)	-43, -21
(e _{2g} ; ip)	(602; 508; -94)	(64; 12 %)	(-7.7 %, -3.8 %)
v_4	483	577(-), 596(+)	+94, +113
(b _{2g} ; op)	(712; 253; -459)	(19; 3.2 %)	(+19 %, +23 %)
<i>v</i> ₁₁	616	625(+), 643(-)	+9, +27
(a _{2u} ; op)	(678; 553; -135)	(18; 2.8 %)	(+1.5 %, +4.4 %)
<i>v</i> ₁₀	717	749(+), 751(-)	+32, +34
(e _{1g} ; op)	(858; 576; -282)	(2; 0.3 %)	(+4.5 %, +4.7 %)
<i>v</i> ₁₇	873	875(-), 881(+)	+2, +8
(e _{2u} ; op)	(981; 765; -216)	(6; 0.7 %)	(+0.2 %, +0.9 %)
<i>v</i> ₅	910	900(-), 914(+)	-10, +4
(b _{2g} ; op)	(1012; 807; -205)	(14; 1.5 %)	(-1.1 %, +0.4 %)
<i>v</i> ₁	991	914(-), 993(+)	-77, +2
(a _{1g} ; ip)	(1018; 963; -55)	(79; 8.3 %)	(-7.8 %, +0.2 %)
<i>v</i> ₁₂	975	978(-), 979(+)	+3, +4
(b _{1u} ; ip)	(987; 963; -24)	(1; 0.1 %)	(+0.3 %, +0.4 %)
<i>v</i> ₁₈	1012	1014(+), 1017(-)	+2, +5
(e _{1u} ; ip)	(1048; 976; -72)	(3; 0.3 %)	(+0.2 %, +0.5 %)
<i>v</i> ₁₅	1131	1132(-), 1135(+)	+1, +4
(b _{2u} ; ip)	(1129; 1132; +3)	(3; 0.3 %)	(+0.1 %, +0.4 %)
<i>v</i> ₉	1154	1135(-), 1155(+)	-7, +13
(e _{2g} ; ip)	(1162; 1146; -16)	(20; 1.7 %)	(-0.4 %, +0.7 %)
<i>v</i> ₃	1323	1321(-), 1321(+)	-2, -2
(a _{2g} ; ip)	(1330; 1315; -15)	(0; 0 %)	(-0.2 %, -0.2 %)
<i>v</i> ₁₄	1450	1435(+), 1454(-)	-15, +4
(b _{2u} ; ip)	(1326; 1573; +247)	(9; 0.6 %)	(-1.0 %, 0.3 %)
<i>v</i> ₁₉	1453	1449(+), 1453(-)	-4,0
(e _{1u} ; ip)	(1486; 1420; -66)	(4; 0.3 %)	(-0.3 %, 0 %)
v_8	1616	1541(-), 1615(+)	-76, -1

(e _{2g} ; ip)	(1649; 1583; -66)	(74; 4.7 %)	(-4.7 %, -0.1 %)
<i>v</i> ₁₃	3052	3047(-),3048(+)	-5, -4
(b _{2u} ; ip)	(3039; 3064; +25)	(1; 0.0 %)	(-0.2 %, -0.1 %)
v_7	3058	3052(+),3055(-)	-6, -3
(e _{2g} ; ip)	(3048; 3068; +20)	(3; 0.1 %)	(-0.2 %, -0.1 %)
<i>v</i> ₂₀	3074	3070(-),3071(+)	-4, -3
(e _{1u} ; ip)	(3063; 3084; +21)	(1; 0.0 %)	(-0.1 %, -0.1 %)
<i>v</i> ₂	3083	3076(-),3082(+)	-7, -1
(a _{1g} ; ip)	(3072; 3094; +22)	(6; 0.2 %)	(-0.2 %, -0.0 %)

Table S4 Theoretical (v_{calc}) vibrational frequencies and the assignments of Bz and Bz₂ in the S₀ and S₁ states calculated by normal mode analyses on the optimized structures obtained by CAM-B3LYP/aug-cc-pVTZ and TD-CAM-B3LYP/aug-cc-pVTZ level of theory with GD3BJ empirical dispersion correction, respectively.

^{a)} These are scaled values by 0.98 for skeletal vibrations and 0.95 for CH stretching vibrations, respectively. Values in parentheses are transition intensities in km/mol.

^{b)} +/- on the shoulder means the signs of the linear combinations, see text. Symmetry species in the D_{6h} point group are denoted in parentheses.

Bz	$z(\mathbf{S}_0)$	Bz (S ₁)		$\mathrm{Bz}_{2}\left(\mathrm{S}_{1},\mathrm{SW},D_{\mathrm{6h}}\right)$		$Bz_2 (S_1, T, C_{2v})$	
$v_{\rm calc}$ / cm ^{-1 a)}	assignments ^{b)}	$v_{\rm calc}$ / cm ^{-1 a)}	assignments	$v_{\rm calc}$ / cm ^{-1 a)}	assignments ^{b)}	$v_{\rm calc}$ / cm ^{-1 a)}	assignments
				64 (0)	R _z	-23 (0)	\mathbf{R}_{x}
				118 (0)	β _(x, y)	11 (0)	R _y
				118 (0)	$\beta_{(x, y)}$	41(0)	R _z
				132 (1)	$\mathbf{R}_{(x, y)}$	53 (0)	σ_z
				132 (1)	$\mathbf{R}(x, y)$	61 (0)	β _x
				154 (0)	σ_z	62 (0)	β _y
410 (0)	16 (e _{2u})	246 (0)	16 (e _{2u})	359 (0)	$16^{-}(e_{2g})$	244 (0)	16a (stem)
				382 (0)	$16^{+}(e_{2u})$	247 (0)	16b (stem)
		340 (0)	4 (b _{2g})			346 (0)	4 (stem)
						410 (0)	16b (top)
617 (0)	6 (e _{2g})			534 (0)	$6^{+}(e_{2g})$	410 (0)	16a (top)
		524 (0)	6 (e _{2g})	592 (0)	$6^{-}(e_{2u})$	520 (0)	6b (stem)
						529 (0)	6a (stem)
						562 (120)	11 (stem)
718 (0)	4 (b _{2g})			598 (0)	$4^{-}(b_{1u})$	617 (0)	6b (top)
				616 (0)	$4^{+}(b_{2g})$	617(0)	6a (top)
688 (113)	11 (a _{2u})	562 (147)	11 (a _{2u})	643 (117)	$11^{+}(a_{2u})$	624 (0)	10a (stem)
				675 (0)	$11^{-}(a_{1g})$	624 (0)	10b (stem)
868 (0)	10 (e _{1g})	623 (0)	10 (e _{1g})	778 (0)	$10^{+} (e_{1g})$	689 (126)	11 (top)
				774 (4)	$10^{-}(e_{1u})$	723 (0)	4 (top)
						773 (0)	17a (stem)
						796 (0)	17b (stem)
997 (0)	17 (e _{2u})	778 (0)	17 (e _{2u})	897 (0)	$17^{-}(e_{2g})$	826 (0)	5 (stem)
				906 (0)	$17^{+}(e_{2u})$	870 (0)	10b (top)
						870 (0)	10a (top)
						960 (1)	1 (stem)
1023 (0)	5 (b _{2g})	811 (0)	5 (b _{2g})	920 (0)	$5^{-}(b_{1u})$	978 (2)	18a (stem)
				934 (0)	$5^{+}(b_{2g})$	979 (5)	18b (stem)
1015 (0)	1 (a _{1g})	961 (0)	1 (a _{1g})	910 (50)	$1^{-}(a_{2u})$	1000 (1)	12 (stem)

1020 (0)	12 (b _{1u})	1000 (0)	12 (b _{1u})	1012 (0)	$12^{-}(b_{2g})$	1000 (0)	17a (top)
				1012 (0)	$12^{+}(b_{1u})$	1001 (0)	17b (top)
				994 (0)	$1^{+}(a_{1g})$	1012 (0)	1 (top)
1054 (11)	18 (e _{1u})	979 (9)	18 (e _{1u})	1018 (6)	$18^{+}(e_{1u})$	1020 (0)	12 (top)
				1023 (0)	$18^{-}(e_{1g})$	1029 (0)	5 (top)
						1054 (5)	18b (top)
						1054 (4)	18a (top)
1150 (0)	15 (b _{2u})	1159 (0)	15 (b _{2u})	1160 (0)	$15^{-}(b_{1g})$	1152 (0)	15 (top)
				1161 (0)	$15^{+}(b_{2u})$	11572 (1)	15 (stem)
1182 (0)	9 (e _{2g})	1163 (0)	9 (e _{2g})	1153 (0)	$9^{-}(e_{2u})$	1161 (1)	9a (stem)
				1175 (0)	$9^{+}(e_{2g})$	1164 (1)	9b (stem)
						1183 (0)	9a (top)
						1183 (0)	9b (top)
1370 (0)	3 (a _{2g})	1351 (0)	3 (a _{2g})	1359 (0)	$3^{-}(a_{1u})$	1307 (0)	14 (top)
				1360 (0)	$3^{+}(a_{2g})$	1351 (0)	3 (stem)
1306 (0)	14 (b _{2u})	1538 (0)	14 (b _{2u})	1414 (0)	$14^{+}(b_{2u})$	1371 (0)	3 (top)
1504 (15)	19 (e _{1u})	1442 (8)	19 (e _{1u})	1472 (16)	$19^{+}(e_{1u})$	1440 (6)	19a (stem)
				1474 (0)	$19^{-}(e_{1g})$	1442 (2)	19b (stem)
						1505 (9)	19a (top)
						1505 (8)	19b (top)
				1428 (0)	$14^{-}(b_{1g})$	1536 (1)	14 (stem)
1638 (0)	8 (e _{2g})	1571 (0)	8 (e _{2g})	1542 (0)	$8^{-}(e_{2u})$	1570 (0)	8b (stem)
				1609 (0)	$8^{+}(e_{2g})$	1570 (0)	8a (stem)
						1636 (0)	8b (top)
						1636 (1)	8a (top)
3022 (0)	13 (b _{1u})	3049 (0)	13 (b _{1u})	3036 (0)	13 ⁻ (b _{2g})	3025 (0)	13 (top)
				3037 (0)	$13^{+}(b_{1u})$	3033 (0)	7b (top)
3032 (0)	7 (e _{2g})	3054 (0)	7 (e _{2g})	3043 (0)	$7^{+}(e_{2g})$	3034 (0)	7a (top)
				3044 (0)	$7^{-}(e_{2u})$	3048 (19)	20b (top)
						3048 (0)	13 (stem)
						3049 (20)	20a (top)
3046 (54)	20 (e _{1u})	3069 (27)	20 (e _{1u})	3057 (0)	$20^{-}(e_{1g})$	3052 (0)	7b (stem)
				3059 (30)	$20^{+}(e_{1u})$	3057 (0)	2 (top)
						3059 (11)	7a (stem)
						3067 (14)	20b (stem)
3056 (0)	2 (a _{1g})	3079 (0)	2 (a _{1g})	3063 (28)	$2^{-}(a_{2u})$	3074 (2)	2 (stem)
				3070 (0)	$2^{+}(a_{1g})$	3100 (4)	20a (stem)

Table S5 Comparison between theoretical average frequencies of the S₀ and S₁ states (v_{ave}) and the EXC state (v_{EXC}) calculated at CAM-B3LYP/aug-cc-pVTZ and TD-CAM-B3LYP/aug-cc-pVTZ level of theory with GD3BJ empirical dispersion correction, respectively. The second column lists frequencies in the EXC state, v_{EXC} , and absolute values of splitting of the modes, $|\Delta v_{EXC}(+/-)| = |v_{EXC}(+) - v_{EXC}(-)|$, and percentage of the splitting to the average frequencies $\langle v_{EXC} \rangle = (v_{EXC}(+) + v_{EXC}(-))/2$. The third column shows deviations from the average values ($\Delta v = v_{EXC} - v_{ave}$) and percentages of difference to the average values.

-			-
Mode	$v_{\rm ave}$ / cm ⁻¹	$v_{\rm EXC}$ / cm ⁻¹	$\Delta v / \mathrm{cm}^{-1}$
Mode	$(v(S_0); v(S_1); \Delta v(S_1/S_0))$	$(\Delta v_{\text{EXC}}(+/-) ; \Delta v_{\text{EXC}}(+/-) /\langle v_{\text{EXC}}\rangle)$	$(\Delta v / v_{\rm ave})$
<i>v</i> ₁₆	331	359 (-), 382 (+)	+29, +52
(e _{2u} ; op)	(410; 246; -163)	(23; 6.2 %)	(+8.8 %, +15.7 %)
v_6	570	534 (+), 592 (-)	-37, +22
(e _{2g} ; ip)	(617; 523; -93)	(59; 10.4 %)	(-6.4 %, +3.9 %)
v_4	529	598 (-), 616 (+)	+69, +87
(b _{2g} ; op)	(718; 340; -378)	(18; 3.0 %)	(+13.0 %, +16.4 %)
<i>v</i> ₁₁	625	643 (+), 675 (-)	+18, +50
(a _{2u} ; op)	(688; 562; -126)	(32; 4.8 %)	(+3.0 %, +8.1 %)
<i>v</i> ₁₀	746	778 (+), 774 (-)	+33, +28
(e _{1g} ; op)	(868; 623; -246)	(5; 0.6 %)	(+4.4 %, +3.8 %)
<i>v</i> ₁₇	888	897 (-), 906 (+)	+10, +18
(e _{2u} ; op)	(997; 778; -219)	(9; 1.0 %)	(+1.1 %, +2.1 %)
<i>v</i> ₅	917	920 (-), 934 (+)	+3, +17
(b _{2g} ; op)	(1023; 811; -211)	(14; 1.5 %)	(+0.3 %, +1.8 %)
v_1	988	910 (-), 994 (+)	-78, +6
(a _{1g} ; ip)	(1015; 961; -54)	(83; 8.8 %)	(-7.9 %, +0.6 %)
<i>v</i> ₁₂	1010	1012 (-), 1012 (+)	+2, +3
(b _{1u} ; ip)	(1020; 1000; -20)	(0; 0.0 %)	(+0.2 %, +0.3 %)
v_{18}	1016	1018 (+), 1023 (-)	+2, +7
(e _{1u} ; ip)	(1054; 979; -75)	(5; 0.4 %)	(+0.2 %, +0.7 %)
<i>v</i> ₁₅	1155	1160 (-), 1161 (+)	+5, +6
(b _{2u} ; ip)	(1150; 1159; +9)	(1; 0.1 %)	(+0.4 %, +0.5 %)
<i>v</i> ₉	1173	1153 (-), 1175 (+)	-20, +2
(e _{2g} ; ip)	(1182; 1163; -19)	(22; 1.9 %)	(-1.7 %, +0.2 %)
<i>v</i> ₃	1361	1359 (-), 1360 (+)	-1, -0
(a _{2g} ; ip)	(1370; 1351; -19)	(1; 0.1 %)	(-0.1 %, -0.0 %)
<i>v</i> ₁₄	1422	1414 (+), 1428 (-)	-8, +6
(b _{2u} ; ip)	(1306; 1538; +232)	(13.89; 0.98 %)	(-0.5 %, +0.4 %)
<i>v</i> ₁₉	1473	1472 (+), 1474 (-)	-1, +1
(e _{1u} ; ip)	(1504; 1442; -62)	(2; 0.2 %)	(-0.1 %, +0.1 %)
v_8	1605	1542 (-), 1609 (+)	-63, +4

(e _{2g} ; ip)	(1638; 1571; -67)	(67; 4 %)	(-3.9 %, +0.2 %)
<i>v</i> ₁₃	3036	3036 (-), 3037 (+)	+0, +2
(b _{2u} ; ip)	(3022; 3049; +27)	(1; 0.1 %)	(+0.0 %, +0.1 %)
v_7	3043	3043 (+), 3044 (-)	-0, -1
(e _{2g} ; ip)	(3032; 3054; +22)	(1; 0.0 %)	(-0.0 %, -0.0 %)
<i>v</i> ₂₀	3058	3057 (-), 3059 (+)	-0, +2
(e _{1u} ; ip)	(3046; 3069; +22)	(2; 0.1 %)	(-0.0 %, +0.1 %)
<i>v</i> ₂	3067	3063 (-), 3070 (+)	-4, +2
(a _{1g} ; ip)	(3056; 3079; +23)	(6; 0.2 %)	(-0.1 %, +0.1 %)

Table S6 Comparison between average frequencies in the S₀ and S₁ states (v_{ave}) and those in the EXC state (v_{EXC}). Difference of these values ($\Delta v = v_{EXC} - v_{ave}$) are listed in the third column. Calculated values obtained by CAM-B3LYP/aug-cc-pVTZ and TD-CAM-B3LYP/aug-cc-pVTZ levels of theory with GD3BJ empirical dispersion correction are shown below the experimental values. Two IR active modes are possible for combination modes from degenerate species, see text.

Mada		$v_{\rm ave}$ / cm ⁻¹	$v_{\rm EXC}$ / cm ⁻¹	$\Delta v / \mathrm{cm}^{-1}$
Mode		$(S_0; S_16^1)$	$(FWHM / cm^{-1})$	$(\Delta v / v_{\rm ave})$
	01	980	989	+9
v_{18}	Obs	(1040; 920)	(12)	(+0.9 %)
(in plane)	0.1	1016	1010	+2
	Calc	(1054; 979; -75)	1018	(+0.2 %)
	01	_	_	_
$v_5 + v_{16}$	Obs	(1390; –)	(-)	()
(out-of-plane)	0.1	1245	1280, 1317	+34, +71
	Calc	(1433; 1053)		(+2.8 %, +5.7 %)
	01	1308	1340	+32
$v_{10} + v_{11}$	Obs	(1519; 1096)	(~60)	(+2.4 %)
(out-of-plane)	0.1	1370	1401 1440	+51, +78
	Calc	(1556; 1185)	1421, 1449	(+3.7 %, +5.7 %)
	01	1444	1439	-5
v_{19}	Obs	(1485; 1402)	(9)	(-0.3 %)
(in plane)	Cala	1473	1472	-1
	Calc	(1504; 1442)	1472	(-0.1 %)
	Oha	1557	1570	+13
$v_{10} + v_{17}$	Obs	(1814; 1300)	(~80)	(+0.8 %)
(out-of-plane)	Cala	1633	1671 1694	+37, +51
	Calc	(1865; 1401)	10/1, 1084	(+2.3 %, +3.1 %)
	01	1713	1700	-13
$v_5 + v_{17}$	Obs	(1960; 1465)	(~60)	(-0.6 %)
(out-of-plane)	Cal	1805	1817, 1840	+12, +35
	Calc	(2020; 1590)		(+0.7 %, +2.0 %)
	Oha	3072	3075	+3
v_{20}	Obs	(3065; 3079) ^{a)}	(6)	(+0.1 %)
(in plane)	Cala	3057	2050	+2
	Calc	(3046; 3069)	3039	(+0.1 %)

^{a)} Deperturbed values taken from ref. 84 and ref. 87.



Figure S2 Comparison of vibration frequencies of (a) Bz in S_0 , (b) Bz in S_1 and (c) Bz₂ in S_1 states (SW structure) obtained by CAM-B3LYP/aug-cc-pVTZ and TD-CAM-B3LYP/aug-cc-pVTZ levels of theory with the GD3BJ empirical dispersion correction, and the experimental spectrum (d). Positions of the combination bands are calculated as simple sums of the respective fundamental frequencies. Black circles indicate the average positions of the vibration frequencies in the S_0 and S_1 states of Bz. Vertical lines drown from the circles compare the average positions with frequencies calculated for the SW EXC state. In the panel (c), two bars with the same color show positions of two different IR active combinations, see the main text. This is a figure corresponding to Figure 5 in the main text but with the CAM-B3LYP functional.

The full expression of the excimer state vibrational energy, $E_{v_{\pm}}^{+/-'}$, derived from the secular determinant given by equation (33) in Appendix.

Since the secular determinant derives a quadratic equation, the solution is written in the standard form:

$$E_{\nu_{\pm}}^{+/-\prime} = \frac{B^{+/-\sqrt{C}}}{2A}.$$
 (S1)

Here, factors A, B, and C are expressed as follows (notation of factors follows that in Appendix):

$$A = \left\{ 1 \pm \langle S \rangle \langle FC_{0^{*}\nu}^{\phi} \rangle^{2} FC_{0^{*}0}^{2} \right\} \left\{ 1 \pm \langle S \rangle \langle FC_{\nu^{*}0}^{\phi} \rangle^{2} FC_{0^{*}0}^{2} \right\} - \langle S \rangle^{2} \langle FC_{\nu^{*}0}^{\phi} \rangle^{2} FC_{0^{*}0}^{4}$$
$$= 1 \pm \langle S \rangle \left(\langle FC_{0^{*}\nu}^{\phi} \rangle^{2} + \langle FC_{\nu^{*}0}^{\phi} \rangle^{2} \right) FC_{0^{*}0}^{2} + \langle S \rangle^{2} \left(\langle FC_{0^{*}\nu}^{\phi} \rangle^{2} \langle FC_{\nu^{*}0}^{\phi} \rangle^{2} - \langle FC_{\nu^{*}\nu}^{\phi} \rangle^{2} \right) FC_{0^{*}0}^{4}, \qquad (S2)$$

$$B = \left\{ 1 \pm \langle S \rangle \langle FC_{v^*0}^{\phi} \rangle^2 FC_{0^*0}^{2} \right\} \left\{ hv \pm (\langle EXC \rangle + 2\langle S \rangle \langle T_{0^*v} \rangle) \langle FC_{0^*v}^{\phi} \rangle^2 FC_{0^*0}^{2} \right\} \\ + \left\{ 1 \pm \langle S \rangle \langle FC_{0^*v}^{\phi} \rangle^2 FC_{0^*0}^{2} \right\} \left\{ hv^* \pm (\langle EXC \rangle + 2\langle S \rangle \langle T_{v^*0} \rangle) \langle FC_{v^*0}^{\phi} \rangle^2 FC_{0^*0}^{2} \right\} \\ - 2\langle S \rangle (\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) \langle FC_{v^*0}^{\phi} \rangle^2 FC_{0^*0}^{4} \\ = hv + hv^* \pm \left((\langle EXC \rangle + 2\langle S \rangle \langle T_{0^*v} \rangle) \langle FC_{0^*v}^{\phi} \rangle^2 + (\langle EXC \rangle + 2\langle S \rangle \langle T_{v^*0} \rangle) \langle FC_{v^*0}^{\phi} \rangle^2 + \langle S \rangle \left(\langle FC_{0^*v}^{\phi} \rangle^2 hv^* + \langle FC_{v^*0}^{\phi} \rangle^2 hv \right) \right) FC_{0^*0}^{2} + \\ 2\langle S \rangle \left(\left(\langle EXC \rangle + \langle S \rangle (\langle T_{0^*v} \rangle + \langle T_{v^*0} \rangle) \right) \langle FC_{0^*v}^{\phi} \rangle^2 \langle FC_{v^*0}^{\phi} \rangle^2 - (\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) \langle FC_{v^*v}^{\phi} \rangle^2 \right) FC_{0^*0}^{4}, \quad (S3)$$

$$C = \left[\left\{ 1 \pm \langle S \rangle \langle FC_{v^* 0}^{\phi} \rangle^2 FC_{0^* 0}^{-2} \right\} \left\{ hv \pm (\langle EXC \rangle + 2\langle S \rangle \langle T_{0^* v} \rangle) \langle FC_{0^* v}^{\phi} \rangle^2 FC_{0^* 0}^{-2} \right\} - \left\{ 1 \pm \langle S \rangle \langle FC_{0^* v}^{\phi} \rangle^2 FC_{0^* 0}^{-2} \right\} \left\{ hv^* \pm (\langle EXC \rangle + 2\langle S \rangle \langle T_{v^* 0} \rangle) \langle FC_{v^* 0}^{\phi} \rangle^2 FC_{0^* 0}^{-2} \right\} \right]^2 + 4 \langle FC_{v^* v}^{\phi} \rangle^2 FC_{0^* 0}^{-4} \left[\{ \langle S \rangle hv - (\langle EXC \rangle + \langle S \rangle \langle T_{v^* v} \rangle) \} \pm \langle S \rangle^2 (2\langle T_{0^* v} \rangle - \langle T_{v^* v} \rangle) \langle FC_{0^* v}^{\phi} \rangle^2 FC_{0^* 0}^{-2} \right] \left[\{ \langle S \rangle hv^* - (\langle EXC \rangle + \langle S \rangle \langle T_{v^* v} \rangle) \} \pm \langle S \rangle^2 (2\langle T_{v^* 0} \rangle - \langle T_{v^* v} \rangle) \langle FC_{0^* v}^{\phi} \rangle^2 FC_{0^* 0}^{-2} \right] \left[\{ \langle S \rangle hv^* - (\langle EXC \rangle + \langle S \rangle \langle T_{v^* v} \rangle) \} \pm \langle S \rangle^2 (2\langle T_{v^* 0} \rangle - \langle T_{v^* v} \rangle) \langle FC_{0^* v}^{\phi} \rangle^2 FC_{0^* 0}^{-2} \right] \left[\{ \langle S \rangle hv^* - (\langle EXC \rangle + \langle S \rangle \langle T_{v^* v} \rangle) \} \pm \langle S \rangle^2 (2\langle T_{v^* 0} \rangle - \langle T_{v^* v} \rangle) \langle FC_{v^* 0}^{\phi} \rangle^2 FC_{0^* 0}^{-2} \right] \right]$$

In the case of a non-totally symmetric mode, two FC factors vanish due to a requirement of the symmetry, $\langle FC_{0^*\nu}^{\phi} \rangle = \langle FC_{\nu^*0}^{\phi} \rangle = 0$. This condition reduces the above terms as follows:

$$A = 1 - \langle S \rangle^2 \langle F C_{v^* v}^{\phi} \rangle^2 F C_{0^* 0}^{4}, \tag{S2'}$$

$$B = h\nu + h\nu^* - 2\langle S \rangle (\langle EXC \rangle + \langle S \rangle \langle T_{\nu^*\nu} \rangle) \langle FC^{\phi}_{\nu^*\nu} \rangle^2 FC_{0^*0}^{4}, \qquad (S3')$$

$$C = (h\nu - h\nu^{*})^{2} + 4 \langle FC_{\nu^{*}\nu}^{\phi} \rangle^{2} FC_{0^{*}0}^{4} \{ \langle S \rangle h\nu - (\langle EXC \rangle + \langle S \rangle \langle T_{\nu^{*}\nu} \rangle) \} \{ \langle S \rangle h\nu^{*} - (\langle EXC \rangle + \langle S \rangle \langle T_{\nu^{*}\nu} \rangle) \}$$

$$= \left\{ 1 - \langle S \rangle^{2} \langle FC_{\nu^{*}\nu}^{\phi} \rangle^{2} FC_{0^{*}0}^{4} \right\} (h\nu - h\nu^{*})^{2} + \left\{ 2(\langle EXC \rangle + \langle S \rangle \langle T_{\nu^{*}\nu} \rangle) - \langle S \rangle (h\nu + h\nu^{*}) \right\}^{2} \langle FC_{\nu^{*}\nu}^{\phi} \rangle^{2} FC_{0^{*}0}^{4}.$$

(S4')

The first term of equation (S4') is considered to be much smaller than the second term because of a factor of vibrational energy difference. Thus, square root of equation (S4') can be expanded as follows: $\sqrt{C} =$

$$\{2(\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) - \\ \langle S \rangle(hv + hv^*) \} \langle FC_{v^*v}^{\phi} \rangle FC_{0^*0}^{-2} \left(1 + \frac{\{1 - \langle S \rangle^2 \langle FC_{v^*v}^{\phi} \rangle^2 FC_{0^*0}^{-4} \}(hv - hv^*)^2}{\{2(\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) - \langle S \rangle(hv + hv^*) \}^2 \langle FC_{v^*v}^{\phi} \rangle^2 FC_{0^*0}^{-4}} \right)^{\frac{1}{2}} \\ \approx \{2(\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) - \langle S \rangle(hv + hv^*) \} \langle FC_{v^*v}^{\phi} \rangle FC_{0^*0}^{-2} + \frac{1}{2} \frac{\{1 - \langle S \rangle^2 \langle FC_{v^*v}^{\phi} \rangle^2 FC_{0^*0}^{-4} \}(hv - hv^*)^2}{\{2(\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) - \langle S \rangle(hv + hv^*) \} \langle FC_{v^*v}^{\phi} \rangle FC_{0^*0}^{-2} + \frac{1}{2} \frac{\{1 - \langle S \rangle^2 \langle FC_{v^*v}^{\phi} \rangle^2 FC_{0^*0}^{-4} \}(hv - hv^*)^2}{\{2(\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) - \langle S \rangle(hv + hv^*) \} \langle FC_{v^*v}^{\phi} \rangle FC_{0^*0}^{-2} + \frac{1}{2} \frac{\{1 - \langle S \rangle^2 \langle FC_{v^*v}^{\phi} \rangle^2 FC_{0^*0}^{-4} \}(hv - hv^*)^2}{\{2(\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) - \langle S \rangle(hv + hv^*) \} \langle FC_{v^*v}^{\phi} \rangle FC_{0^*0}^{-2} + \frac{1}{2} \frac{\{1 - \langle S \rangle^2 \langle FC_{v^*v}^{\phi} \rangle^2 FC_{0^*0}^{-4} \}(hv - hv^*)^2}{\{2(\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) - \langle S \rangle(hv + hv^*) \} \langle FC_{v^*v}^{\phi} \rangle FC_{0^*0}^{-2} + \frac{1}{2} \frac{\{1 - \langle S \rangle^2 \langle FC_{v^*v}^{\phi} \rangle^2 FC_{0^*0}^{-4} \}(hv - hv^*)^2}{\{2(\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) - \langle S \rangle(hv + hv^*) \} \langle FC_{v^*v}^{\phi} \rangle FC_{0^*0}^{-2} + \frac{1}{2} \frac{\{1 - \langle S \rangle^2 \langle FC_{v^*v}^{\phi} \rangle^2 FC_{0^*0}^{-4} \}(hv - hv^*)^2}{\{2(\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) - \langle S \rangle(hv + hv^*) \} \langle FC_{v^*v}^{\phi} \rangle FC_{0^*0}^{-2} + \frac{1}{2} \frac{\{1 - \langle S \rangle^2 \langle FC_{v^*v}^{\phi} \rangle^2 FC_{0^*0}^{-4} \}(hv - hv^*)^2}{\{2(\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) - \langle S \rangle(hv + hv^*) \} \langle FC_{v^*v}^{\phi} \rangle FC_{0^*0}^{-2} + \frac{1}{2} \frac{\{1 - \langle S \rangle^2 \langle FC_{v^*v}^{\phi} \rangle^2 FC_{0^*0}^{-4} \}(hv - hv^*)^2}{\{2(\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) - \langle S \rangle(hv + hv^*) \} \langle FC_{v^*v}^{\phi} \rangle FC_{0^*0}^{-2} + \frac{1}{2} \frac{\{1 - \langle S \rangle^2 \langle FC_{v^*v}^{\phi} \rangle^2 FC_{0^*0}^{-4} \}(hv - hv^*)^2}{\{2(\langle EXC \rangle + \langle S \rangle \langle T_{v^*v} \rangle) - \langle S \rangle(hv + hv^*) \}(hv - hv^*)^2}}$$

Then, the expression of $E_{v_{\pm}}^{+/-'}$, which is used in the appendix as equation (36), can be obtained by substituting equation (S2')–(S5') into (S1).

$$E_{\nu_{\pm}}^{+/-'} \approx \frac{(h\nu + h\nu^{*})}{2(1^{+}/-\langle S \rangle \langle FC_{\nu^{*}\nu}^{\phi} \rangle FC_{0^{*}0}^{2})} + /-\frac{(\langle EXC \rangle + \langle S \rangle \langle T_{\nu^{*}\nu} \rangle) \langle FC_{\nu^{*}\nu}^{\phi} \rangle FC_{0^{*}0}^{2}}{(1^{+}/-\langle S \rangle \langle FC_{\nu^{*}\nu}^{\phi} \rangle FC_{0^{*}0}^{2})} + /-\frac{(h\nu - h\nu^{*})^{2}}{4\{2\langle EXC \rangle + 2\langle S \rangle \langle T_{\nu^{*}\nu} \rangle - \langle S \rangle (h\nu + h\nu^{*})\} \langle FC_{\nu^{*}\nu}^{\phi} \rangle FC_{0^{*}0}^{2}}$$
(S6)