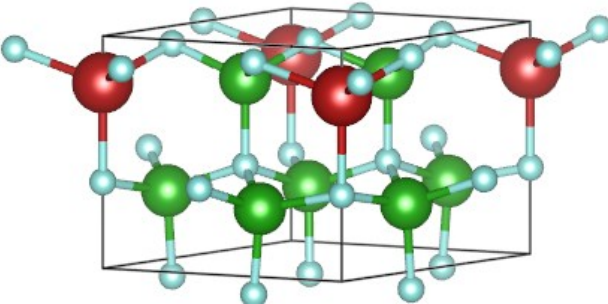
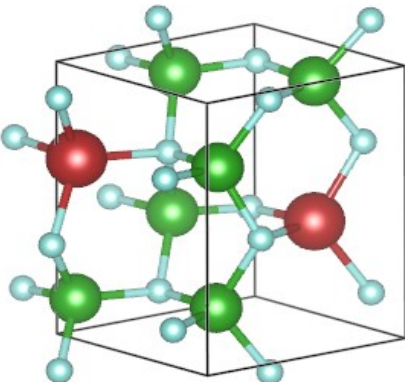
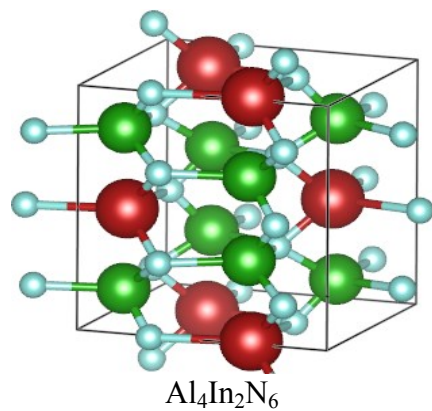


Supplementary information

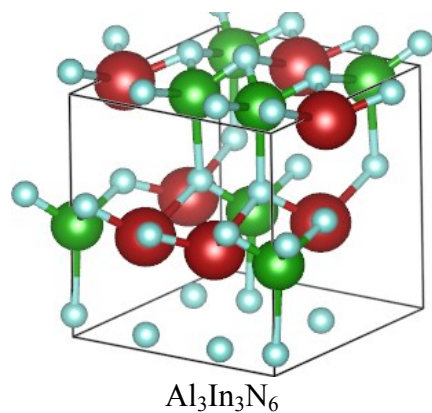
Structure	Corrected bandgap / eV	Lattice parameter / Å	Wyckoff position		
 Al ₅ InN ₆	5.493	$a = 5.451$ $c = 5.054$	Al1	-0.34242	0.00000 0.29396
			Al2	0.33333	0.66667 -0.20399
			In1	0.00000	0.00000 -0.20021
			N1	0.33333	0.66667 0.42142
			N2	-0.36820	0.00000 -0.07634
			N3	0.00000	0.00000 0.37263
 Al ₆ In ₂ N ₈	4.587	$a = 5.504$ $b = 5.088$ $c = 6.381$ $\beta = 89.88$	Al1	-0.08572	0.01087 0.11993
			Al2	0.41300	0.01539 -0.11759
			Al3	0.42543	0.01129 0.36901
			In1	-0.08929	0.01444 -0.36677
			N1	0.09752	0.14455 -0.09969
			N2	-0.41071	0.13870 0.12317
			N3	-0.45679	0.14170 -0.37324
			N4	0.09662	0.09428 0.35356



4.333

$a = 5.568$
 $b = 5.551$
 $c = 5.146$

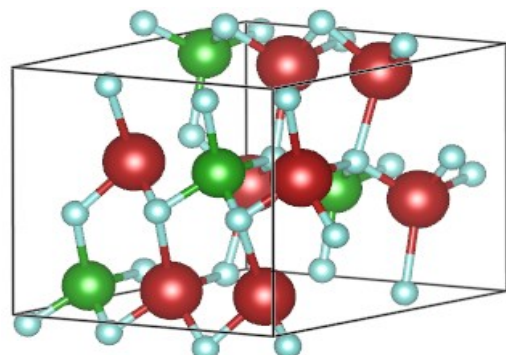
Al1	0.32852	0.33649	-0.43980
In1	0.00000	0.32230	-0.44455
N1	0.00000	-0.29973	0.47446
N2	-0.18443	0.14903	0.42509



2.977

$a = 5.698$
 $b = 5.268$
 $c = 5.680$
 $\beta = 90.02$

Al1	-0.38175	0.33766	-0.05310
Al2	-0.03709	0.00000	0.44829
In1	-0.05268	0.32846	0.45018
In2	-0.36844	0.00000	-0.04856
N1	-0.00946	0.00000	0.08889
N2	-0.39523	0.34948	-0.40728
N3	-0.06263	0.31643	0.04231
N4	-0.34955	0.00000	-0.45649

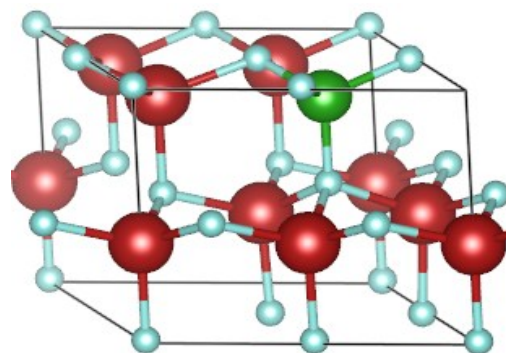


$\text{Al}_2\text{In}_4\text{N}_6$

1.806

$a = 5.808$
 $b = 5.820$
 $c = 6.300$
 $\beta = 58.48$

Al1	-0.43453	0.42299	0.25064
In1	0.23234	0.40952	0.26002
In2	0.39959	0.08949	-0.26710
N1	0.45835	0.43872	-0.39145
N2	-0.40215	0.11173	0.15781
N3	-0.24435	0.42761	-0.37446



AlIn_7N_8

0.486

$a = 6.889$
 $c = 5.539$

Al1	0.33333	0.66667	-0.10470
In1	-0.16731	0.16731	-0.10453
In2	0.49569	-0.49569	0.39568
In3	0.00000	0.00000	0.39473
N1	-0.16799	0.16799	-0.48845
N2	0.48577	-0.48577	0.00704
N3	0.33333	0.66667	-0.44443
N4	0.00000	0.00000	0.01328