

Supporting Information

Dynamics of ethyl cellulose nanoparticle self-assembly at the interface of a nematic liquid crystal droplet

Yining Han^a, Navid Bizmark^a, Nasser Mohieddin Abukhdeir^{a,b} and Marios A. Ioannidis^{a,*}

*To whom correspondence should be addressed. Email: mioannid@uwaterloo.ca

^aDepartment of Chemical Engineering, University of Waterloo, 200 University Avenue West, Waterloo, Ontario N2L 3G1, Canada

^bDepartment of Physics and Astronomy, University of Waterloo, 200 University Avenue West, Waterloo, Ontario N2L 3G1, Canada

Drop-weight (drop-volume) tensiometry

Following the modified Tate's law given by Harkins and Brown,¹ we determined the interfacial tension of 5CB-water from²

$$\gamma = \frac{V(\rho_{5CB} - \rho_{water})g}{2\pi r \psi(r/V^{1/3})} \quad (S1)$$

where V is the volume of the falling drop, r is the internal radius of needle (0.3015 mm), g is the local acceleration of gravity, and ρ_{5CB} and ρ_{water} are the density of 5CB (1028 g L⁻¹) and water (998 g L⁻¹) at the given temperature (22°C), respectively. $\psi(r/V^{1/3})$ is a correction factor² to account for deviations from hemisphericity. A drop of 5CB is formed in water and kept growing to a maximum size before it breaks away. Repeating the procedure for 5 times, we obtained a value of 41.5±0.3 mN m⁻¹ for the interfacial tension of 5CB-water.

# run	$V \times 10^3$ (L)	$r/V^{1/3}$	ψ	γ (mN m ⁻¹)
1	0.268	0.0468	1	41.63
2	0.269	0.0467	1	41.71
3	0.267	0.0468	1	41.48
4	0.265	0.0469	1	41.17
5	0.268	0.0468	1	41.63
AVE				41.53
error				0.27

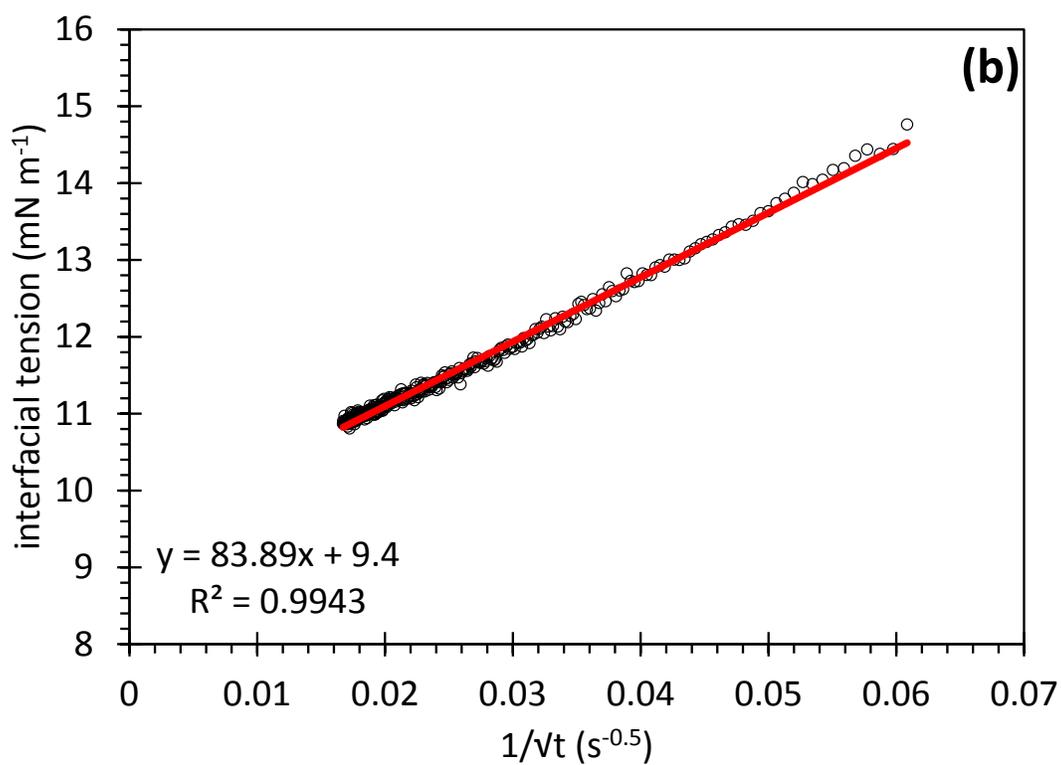
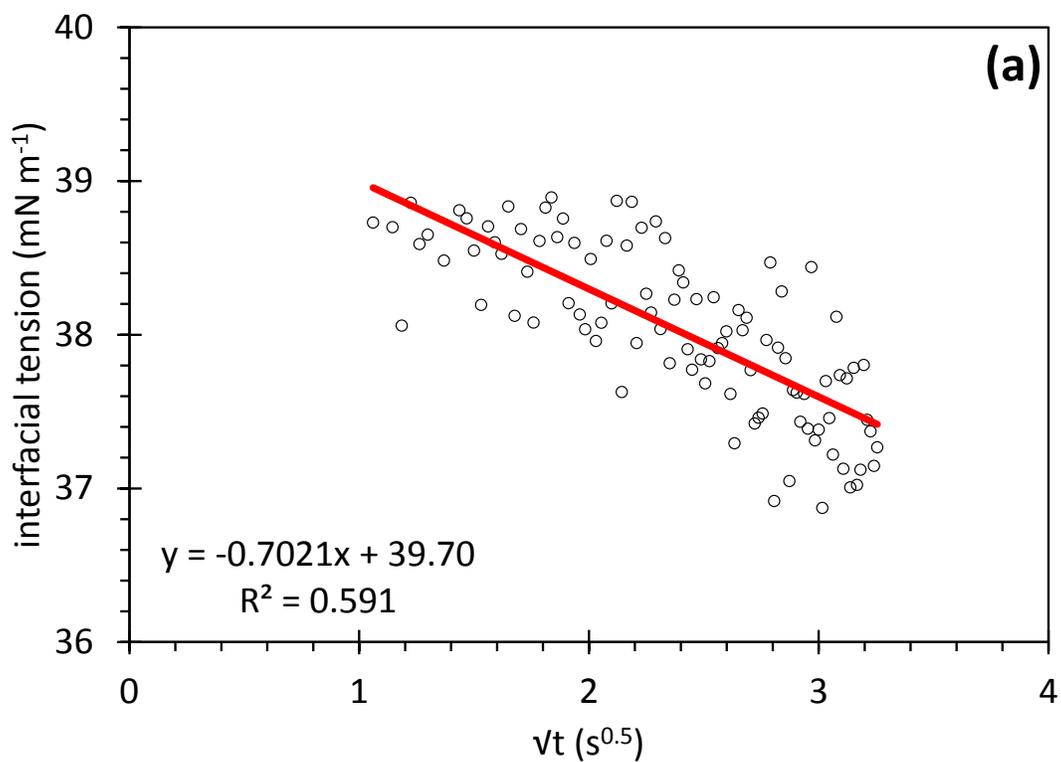
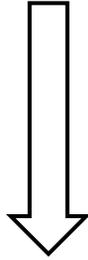


Figure S1. Analysis of (a) early- and (b) late-time dynamic IFT data at a concentration of 0.5 g L⁻¹ EC nanoparticles *via* (a) Eq. (3) and (b) Eq. (4).

Table S1. Statistical pair-comparison of 5CB-water IFT determined from early-time dynamic IFT data interpretation (γ_0). It is assumed that each set of measurements has the same variance and the conclusions are based on 95% confidence interpretation.

Case #	EC concentration (g L ⁻¹)	γ_0 (mN m ⁻¹)	Standard deviation	Number of measurements
I	0 (pristine 5CB-water interface)	40.6	1.15	4
II	0.3	38.5	1.24	5
III	0.5	39.7	1.27	5



Hypothesis test:

Null hypothesis: No difference between the mean values

Alternative hypothesis: There is a difference between the mean values.

Comparison pair	$t_{obs.}$	$T_{critical}$ (from t-distribution table)	Conclusion
I vs. II	2.48	2.36	$t_{obs.} < T_{critical} \rightarrow$ Fail to reject the null hypothesis \rightarrow No difference between γ_0 at different levels of EC concentration is detected.
I vs. III	1.1	2.36	
II vs. III	1.26	2.31	

Table S2. Statistical pair-comparison of adsorption energy ($|\Delta E|$) computed from different approaches and at different EC nanoparticle concentrations. It is assumed that each set of measurements has the same variance and the conclusions are based on 95% confidence interpretation.

Approach	EC concentration (g L ⁻¹)	
	0.3	0.5
Bizmark et al. ³	(I) 5.7±0.3 # runs = 5	(II) 5.6±0.9 # runs = 5
	(III) 5.3±0.2 # runs = 5	(IV) 5.2±0.2 # runs = 5
Pieranski ^{5,6}	(V)	5.1±0.3 # runs = 4

Hypothesis test:

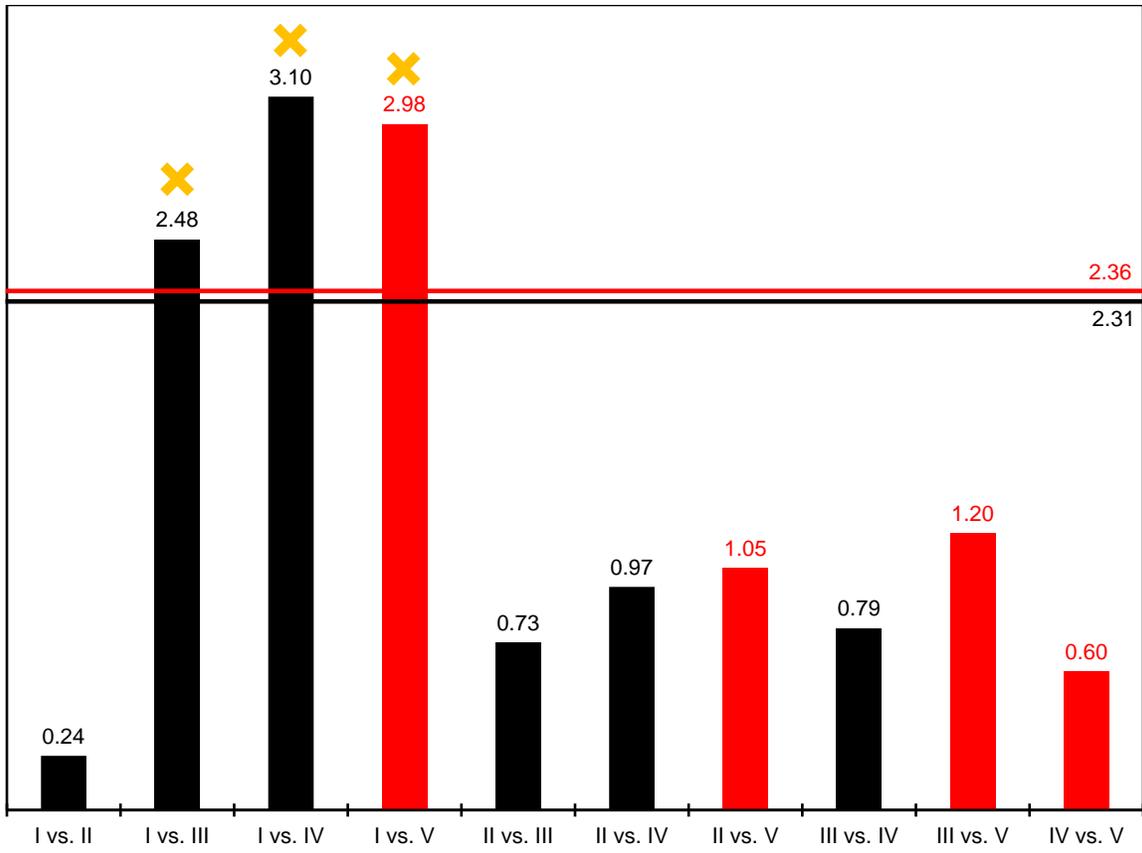
Null hypothesis: No difference between the mean values

Alternative hypothesis: There is a difference between the mean values.

1. $t_{obs.} < T_{critical}$ → Fail to reject the null hypothesis → There is no significant difference between the slopes.
2. $t_{obs.} > T_{critical}$ → Reject the null hypothesis (marked by a ×) → There is a significant difference between the slopes.

All of possible comparisons are shown in the following figure. t_{obs} is calculated from $\frac{|\bar{x}_1 - \bar{x}_2|}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$,

where \bar{x} , s , and n are the mean value, standard deviation, and the number of replicates, respectively and subscripts 1 and 2 show two different series. $T_{critical}$ is found from t-table at a 95% confidence level. The black and red bars should be compared to the $T_{critical}$ indicated by the black and red lines, respectively. Only in three comparisons we rejected the null hypothesis (see the following graph).



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