

# Combined NMR and DFT study of conformational dynamics in lanthanide DOTA-like complexes

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## Electronic supplementary information

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For all calculated Cartesian coordinates and related energies of intermediates see folder in coordinatesArchive.rar archive.

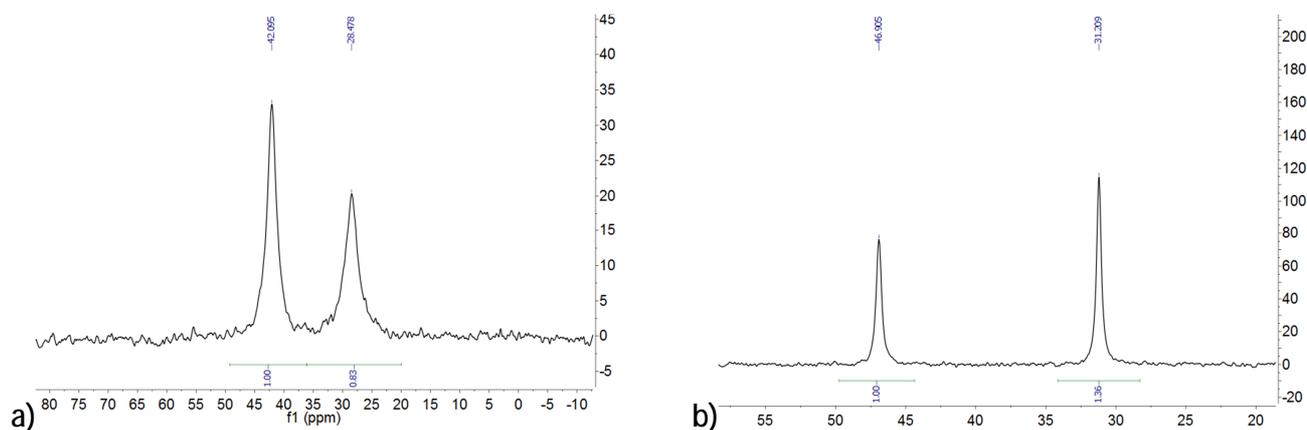
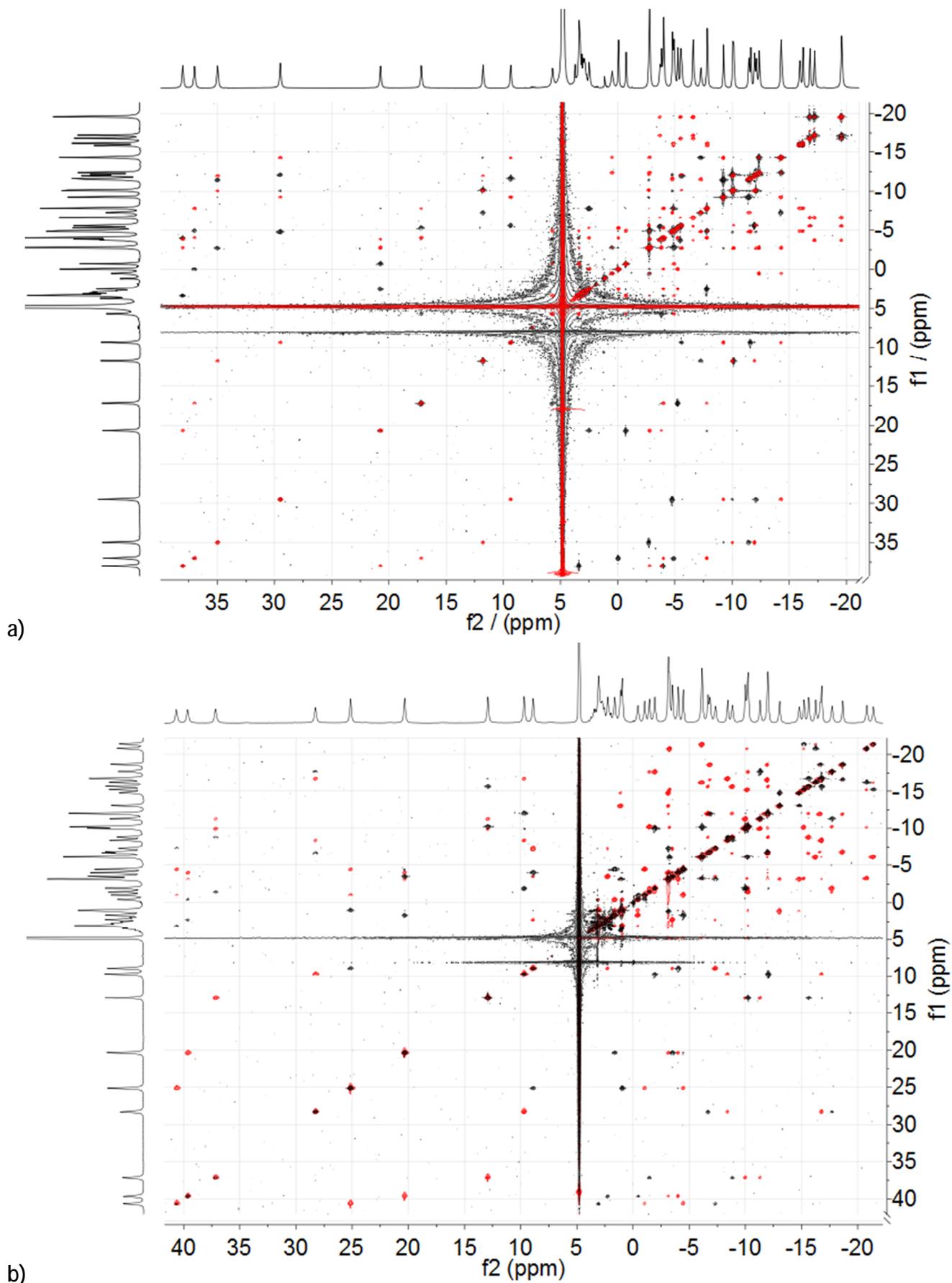


Figure S1:  $^{31}\text{P}$  spectra of a)  $[\text{Eu}(\text{Hdo3ap})(\text{D}_2\text{O})]^-$  (pD = 3.6) and b)  $[\text{Eu}(\text{Hdo3ap})(\text{D}_2\text{O})]^{2-}$  (pD = 8.5) at 5 °C and 162 MHz.

Table S1:  $^1\text{H}$  chemical shifts at 5 °C of axial and equatorial hydrogen nuclei used in 1D-EXSY studies. Supplement to Figure 2 in the main text.

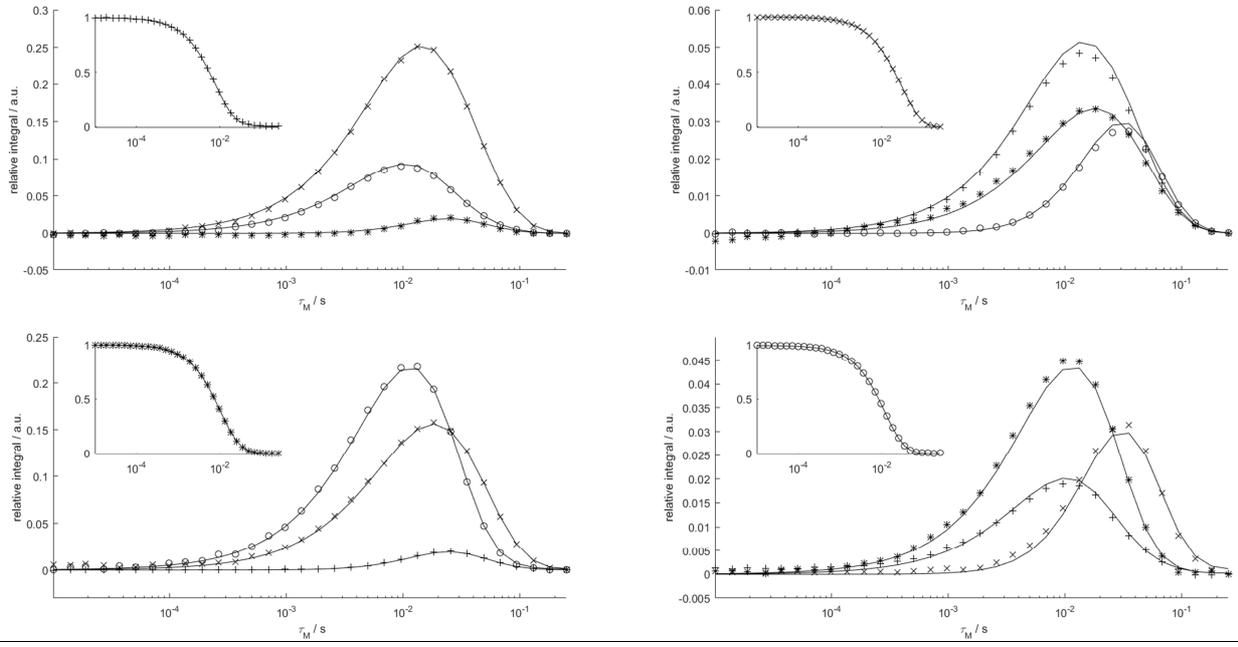
$\delta/\text{ppm}$	dota	Hdo3ap	do3ap
SAP axial 1	36.32	38.02	40.68
SAP axial 2	–	37.00	39.68
SAP axial 3	–	34.98	37.20
SAP axial 4	–	29.50	28.30
TSAP axial 1	13.78	20.74	25.16
TSAP axial 2	–	17.17	20.34
TSAP axial 3	–	11.76	12.93
TSAP axial 4	–	9.34	9.70
SAP equatorial 1	-7.04	-2.78	-1.04
SAP equatorial 2	–	-4.02	-3.15
SAP equatorial 3	–	-10.07	-10.01
SAP equatorial 4	–	-9.26	-8.43
TSAP equatorial 1	-10.06	-3.84	-4.48
TSAP equatorial 2	–	-7.83	-4.03
TSAP equatorial 3	–	-11.98	-11.32
TSAP equatorial 4	–	-14.3	-16.81



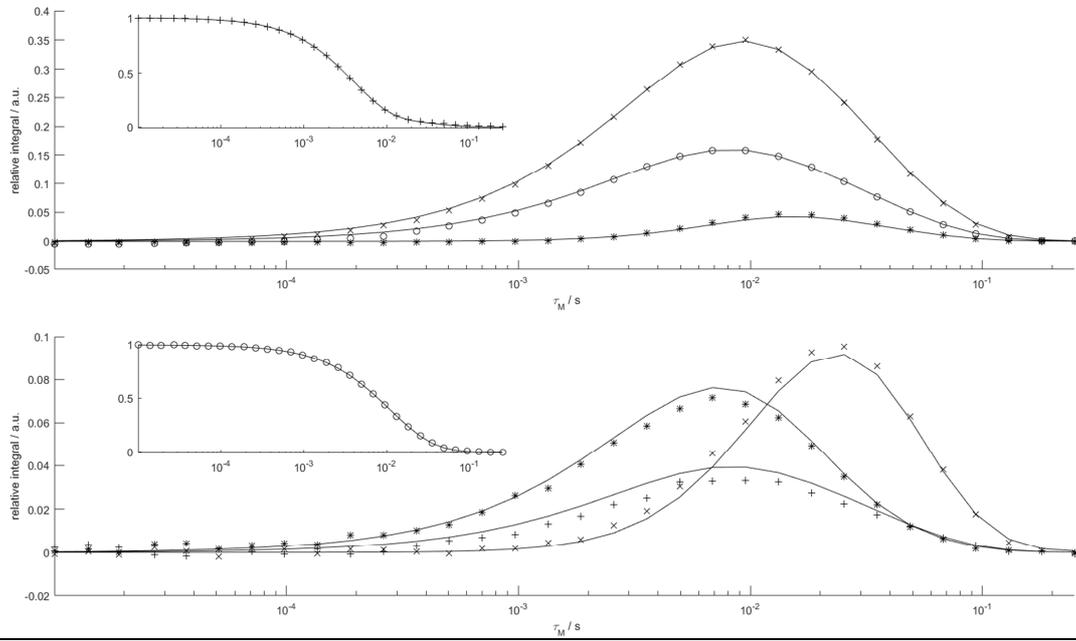
b)

Figure S2:  $^1\text{H}$ - $^1\text{H}$  2D-COSY (black) and  $^1\text{H}$  2D-EXSY spectra (red) of a)  $[\text{Eu}(\text{Hdo3ap})(\text{D}_2\text{O})]^-$  ( $\text{pD} = 3.6$ ) and b)  $[\text{Eu}(\text{do3ap})(\text{D}_2\text{O})]^{2-}$  ( $\text{pD} = 8.5$ );  $5^\circ\text{C}$ ,  $600\text{ MHz}$ , mixing time  $5\text{ ms}$  for (a) and  $10\text{ ms}$  for (b).

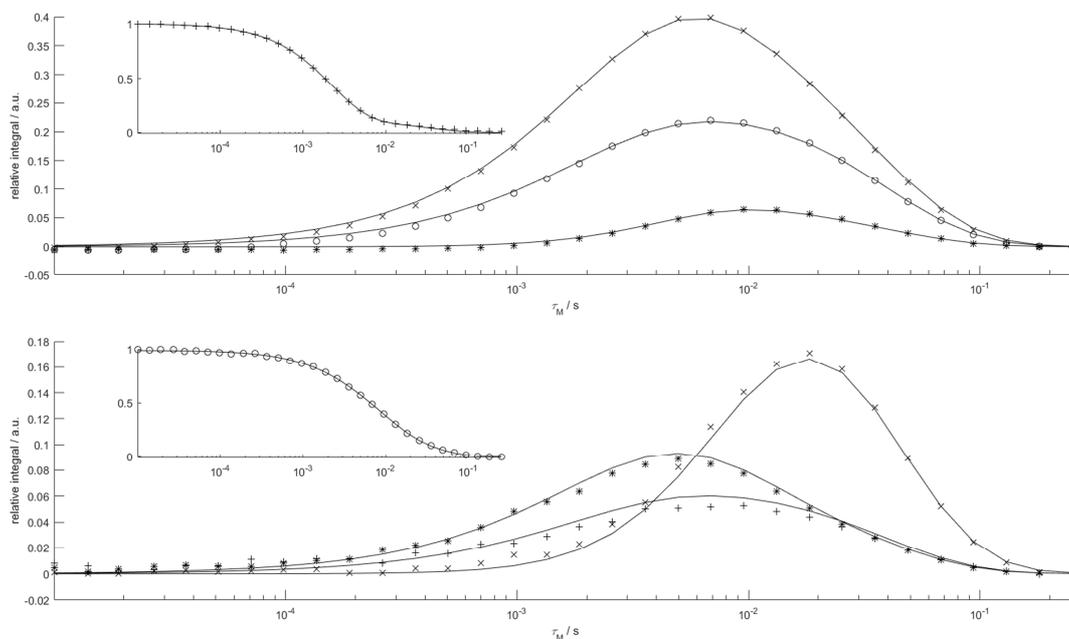
a)



b)



c)



d)

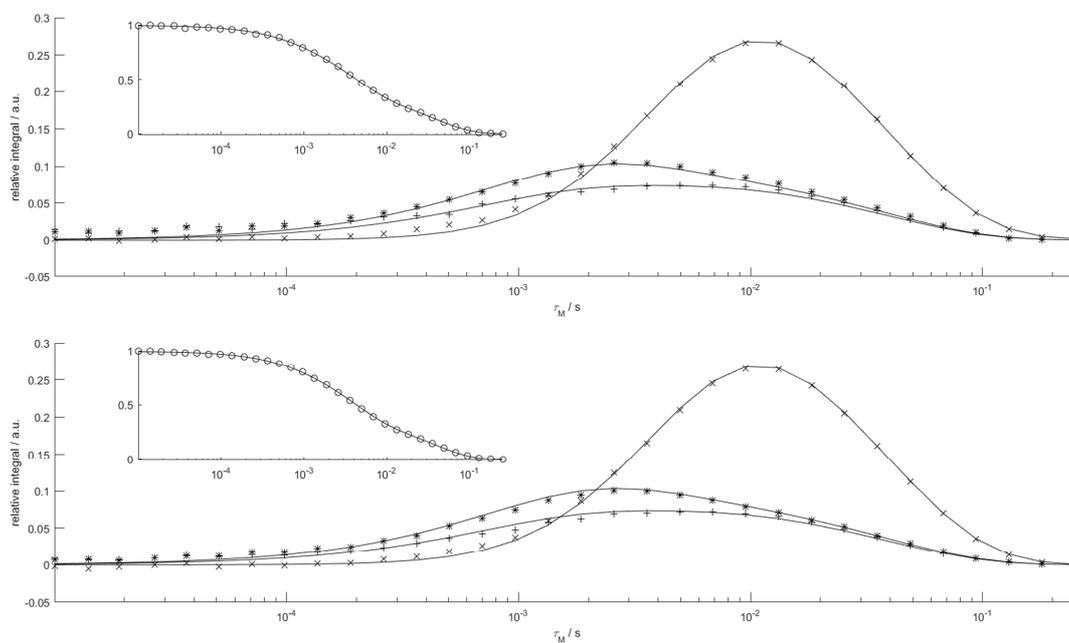
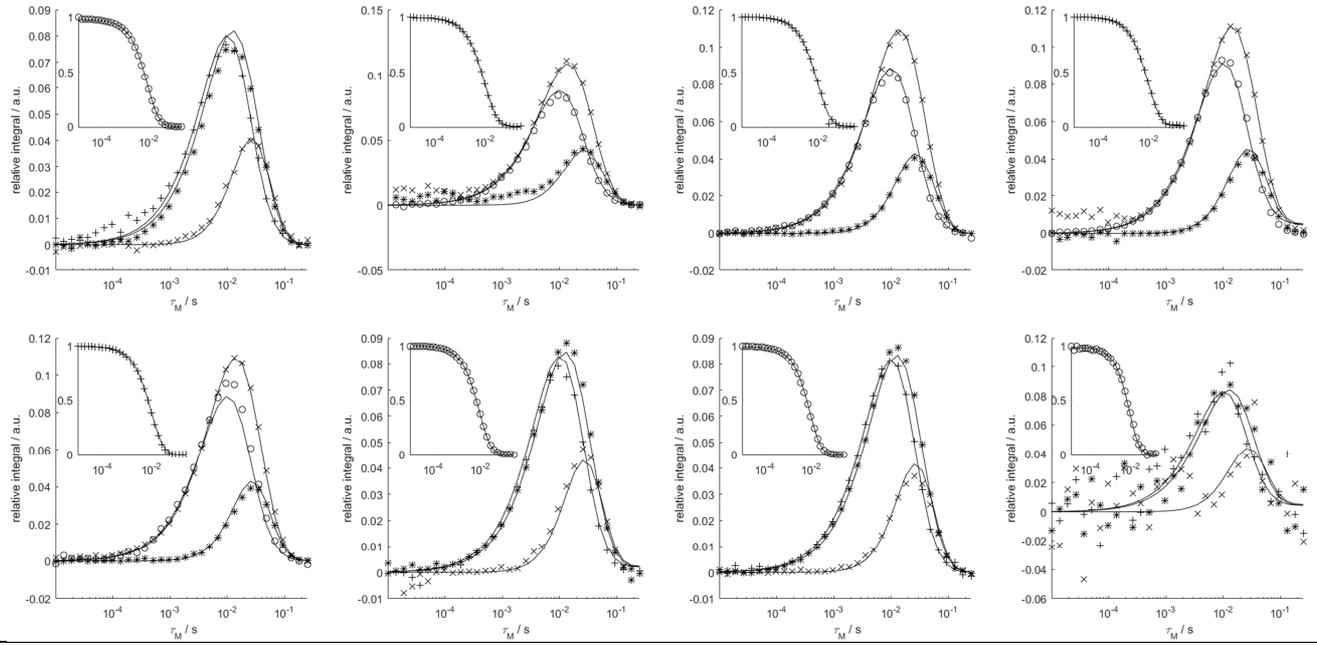
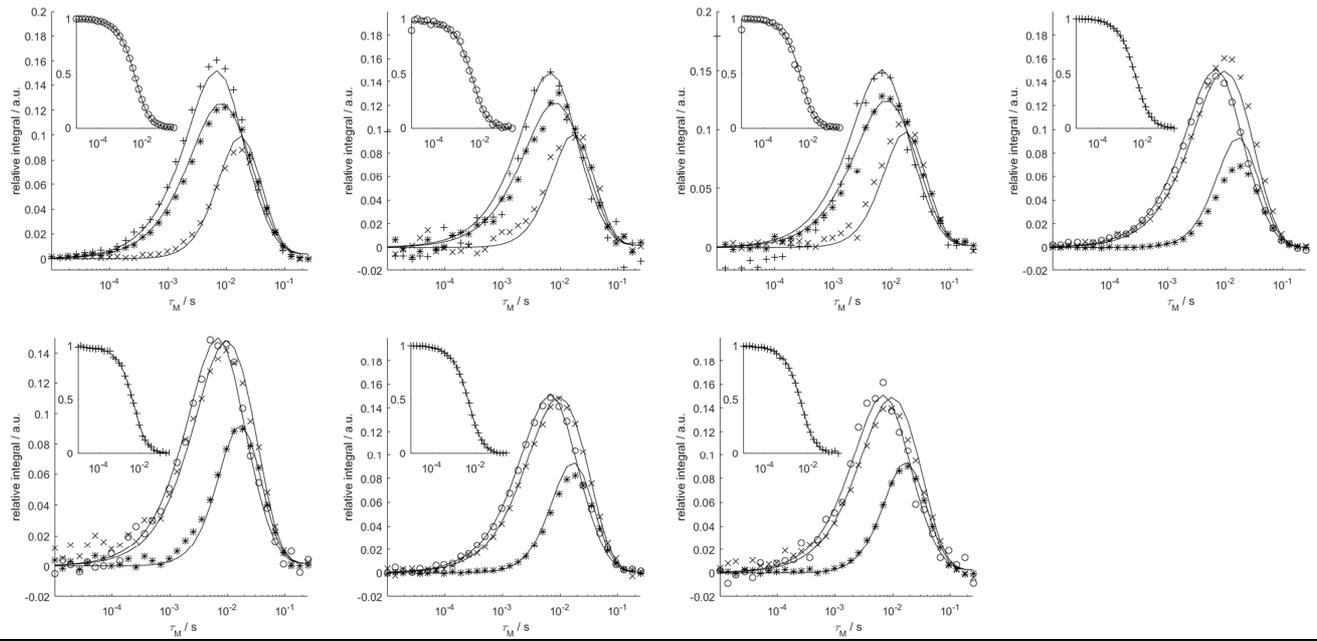


Figure S3. Relative areas of proton NMR signals of  $[\text{Eu}(\text{dota})(\text{D}_2\text{O})]^-$  as a function of the mixing time obtained from 1D-EXSY experiments at a) 5 °C b) 15 °C c) 25 °C and d) 35 °C at pD = 7.0. The insets show the evolution of the magnetisation of the signal to which the refocusing selective  $180^\circ$  pulse was applied. Symbols:  $\text{TSAP}_{\text{ax}}$  (+),  $\text{SAP}_{\text{eq}}$  (x),  $\text{TSAP}_{\text{eq}}$  (\*),  $\text{SAP}_{\text{ax}}$  (o). The solid lines represent the simultaneous fit of all four data sets using Equation [2].

a)



b)



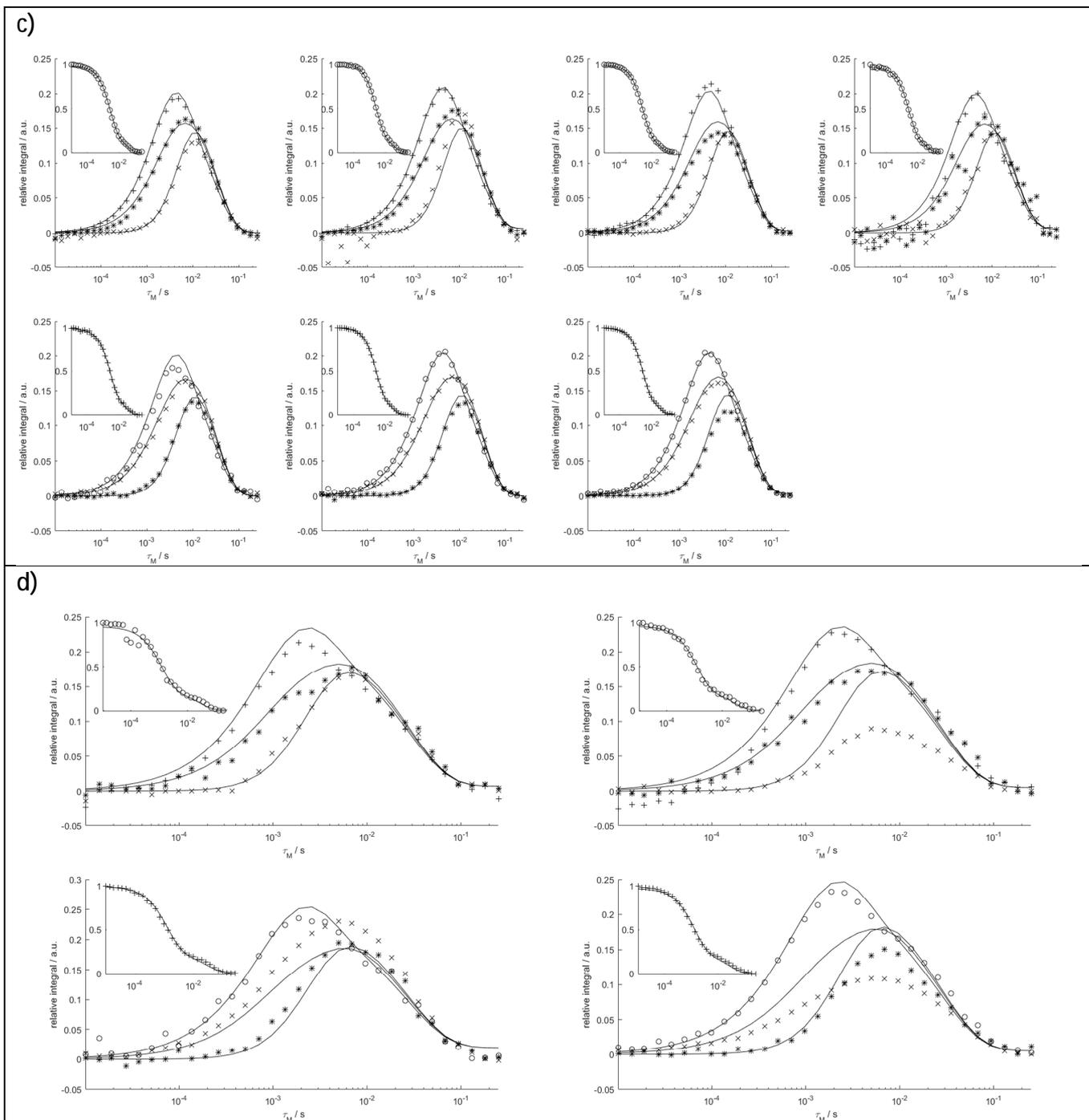
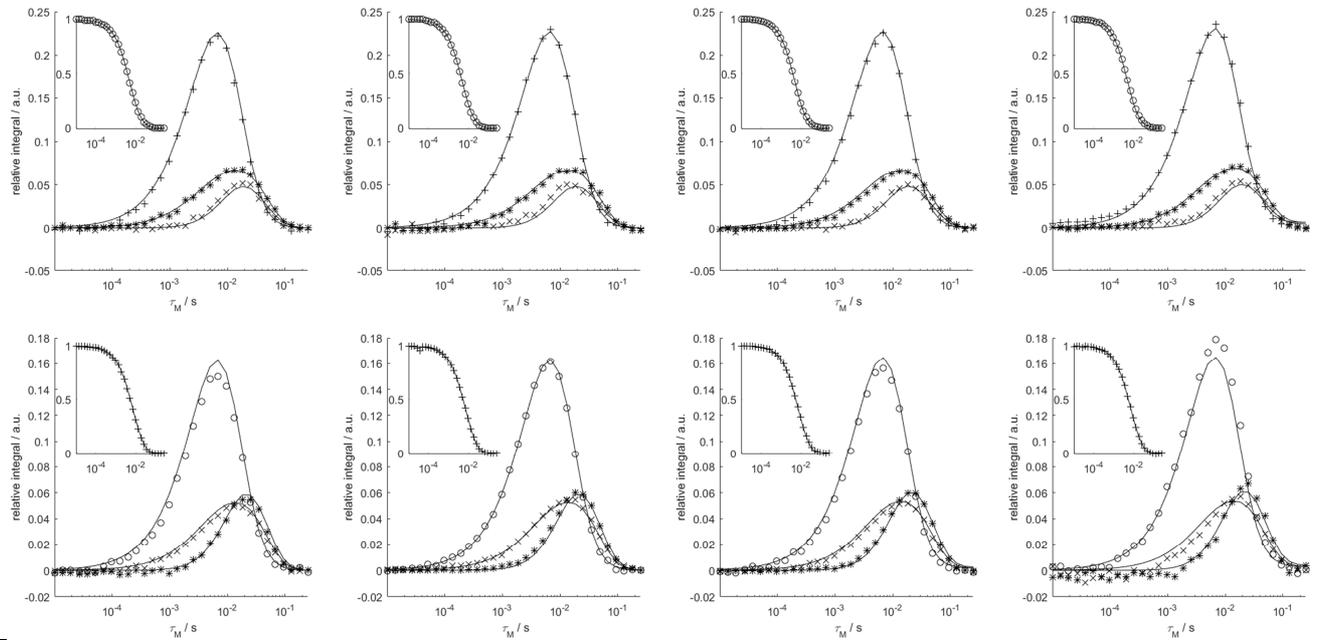
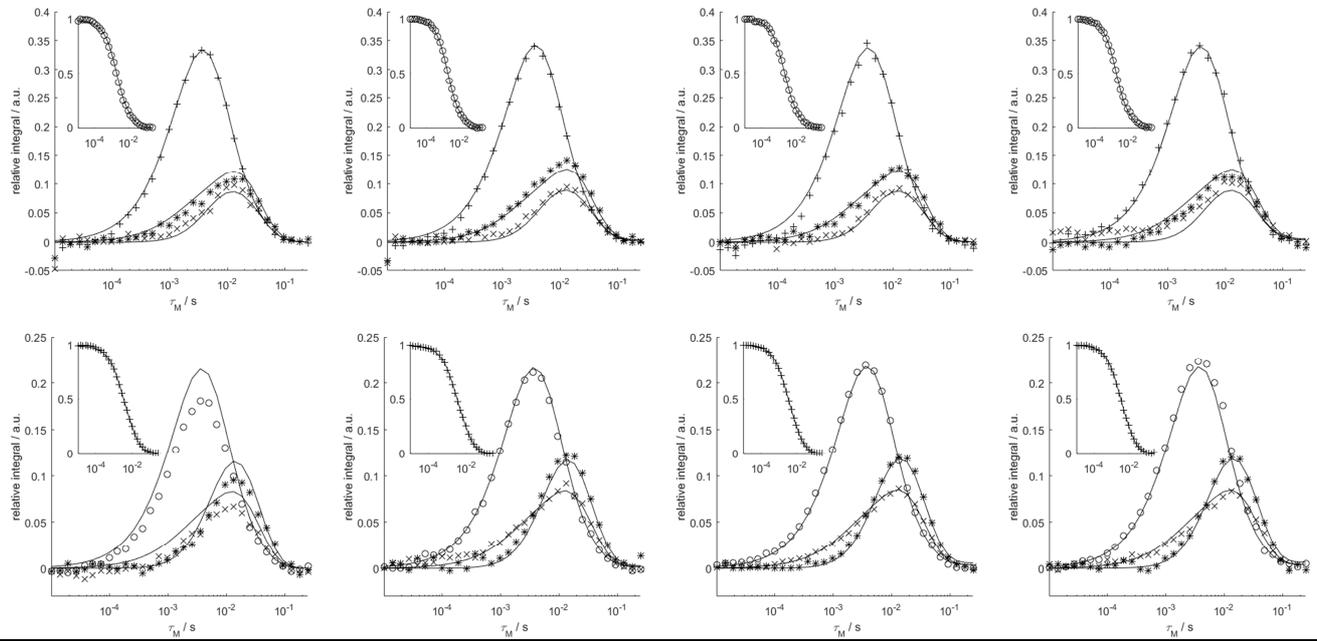


Figure S4. Relative areas of proton NMR signals of  $[\text{Eu}(\text{Hdo3ap})(\text{D}_2\text{O})]^-$  as a function of the mixing time obtained from 1D-EXSY experiments at a) 5 °C b) 15 °C c) 25 °C and d) 35 °C at pD = 3.6. The insets show the evolution of the magnetisation of the signal to which the refocusing selective 180° pulse was applied. Symbols:  $\text{TSAP}_{\text{ax}}$  (+),  $\text{SAP}_{\text{eq}}$  (x),  $\text{TSAP}_{\text{eq}}$  (\*),  $\text{SAP}_{\text{ax}}$  (o). The solid lines represent the simultaneous fit of all four data sets using Equation [2].

a)



b)



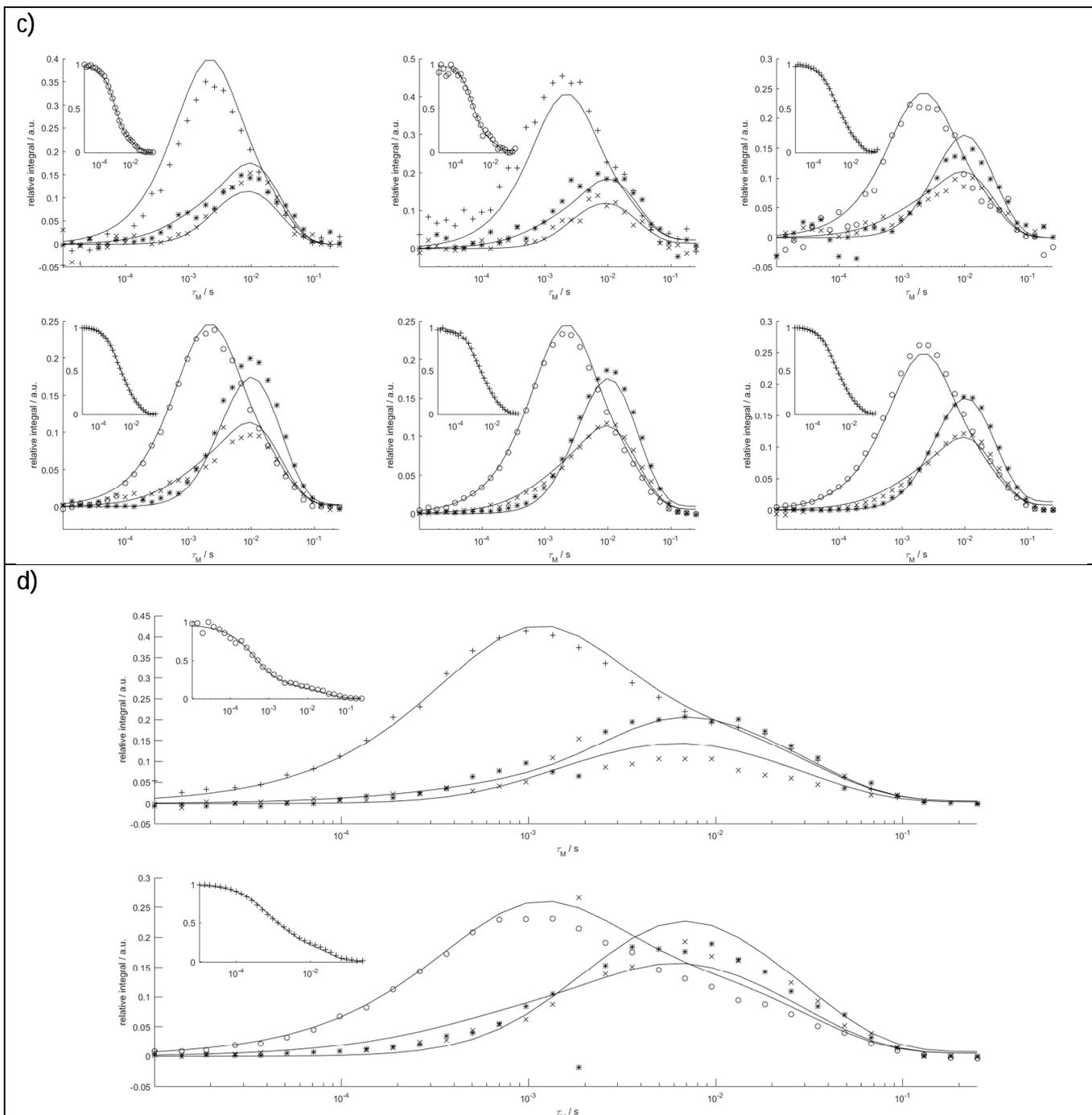


Figure S5. Relative areas of proton NMR signals of  $[\text{Eu}(\text{do3ap})(\text{D}_2\text{O})]^{2-}$  as a function of the mixing time obtained from 1D-EXSY experiments at a) 5 °C b) 15 °C c) 25 °C and d) 35 °C at pD = 8.5. The insets show the evolution of the magnetisation of the signal to which the refocusing selective 180° pulse was applied. Symbols:  $\text{TSAP}_{\text{ax}}$  (+),  $\text{SAP}_{\text{eq}}$  (x),  $\text{TSAP}_{\text{eq}}$  (\*),  $\text{SAP}_{\text{ax}}$  (o). The solid lines represent the simultaneous fit of all four data sets using Equation [2].

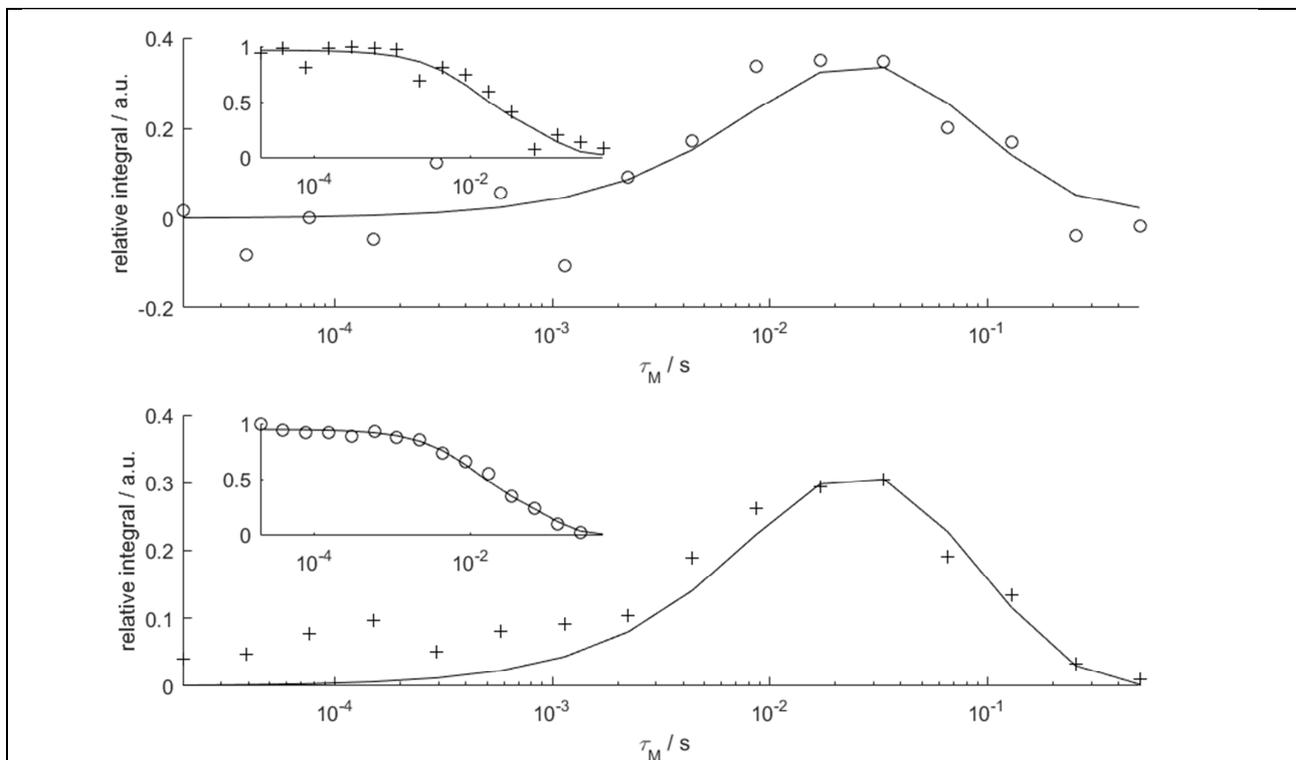


Figure S6. Relative areas of signals of  $[\text{Eu}(\text{Hdo3ap})(\text{D}_2\text{O})]^{2-}$  as a function of the mixing time obtained from  $^{31}\text{P}$  1D-EXSY experiments at  $5\text{ }^\circ\text{C}$ ;  $\text{pD}(25\text{ }^\circ\text{C}) = 3.6$ . The insets show the evolution of the magnetisation of the signal to which the refocusing selective  $180^\circ$  pulse was applied. Symbols: TSAP (+), SAP (o). The solid lines represent the simultaneous fit of both data sets using Equation [2] modified for two-site exchange.

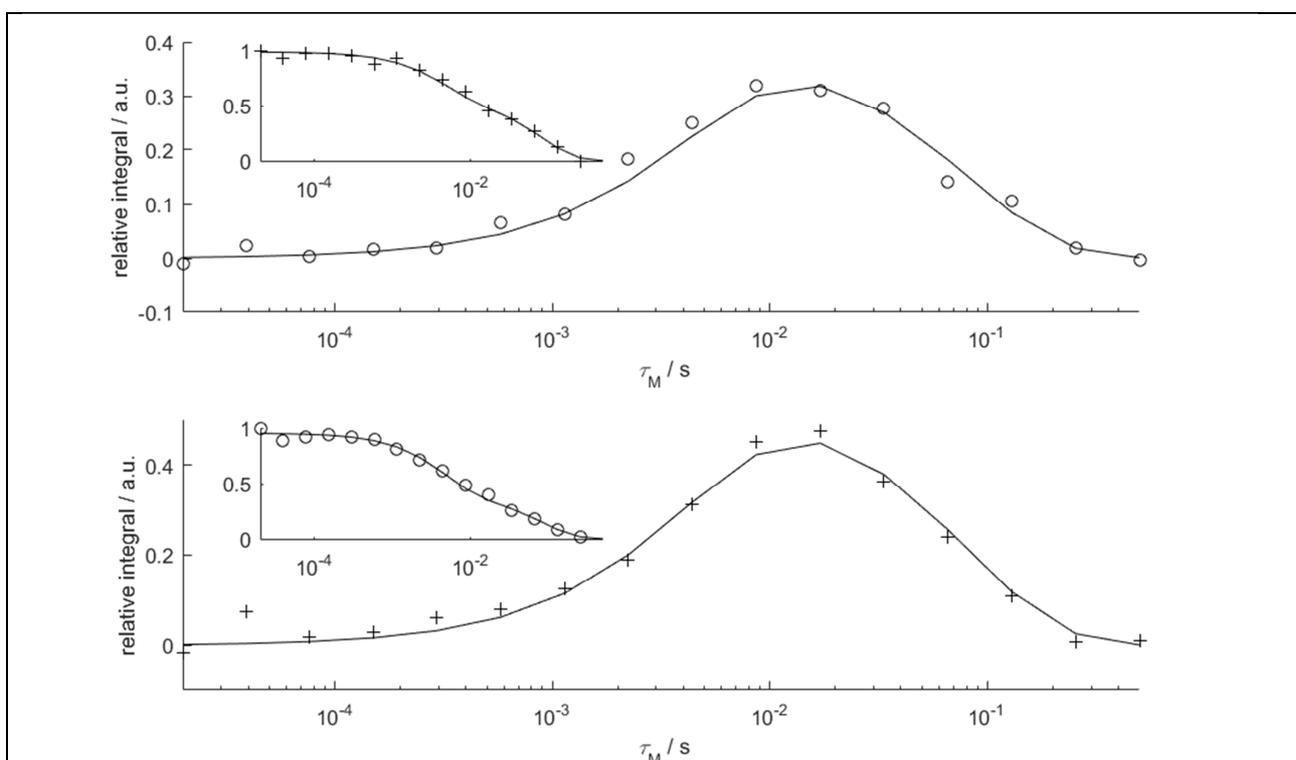
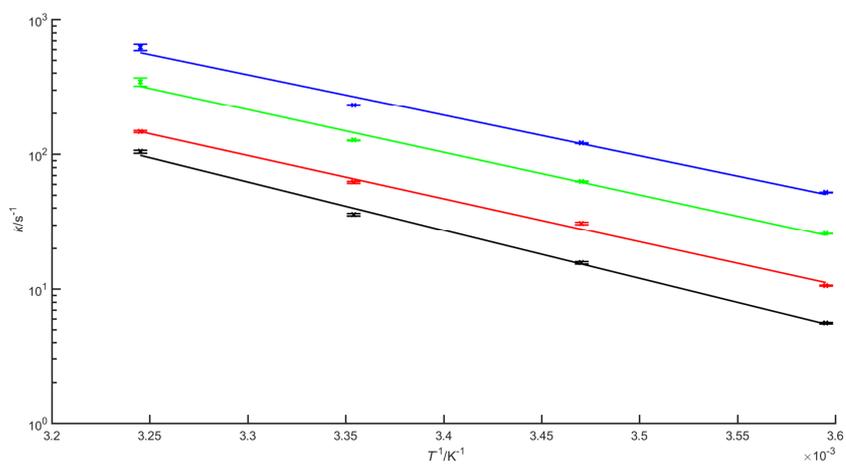
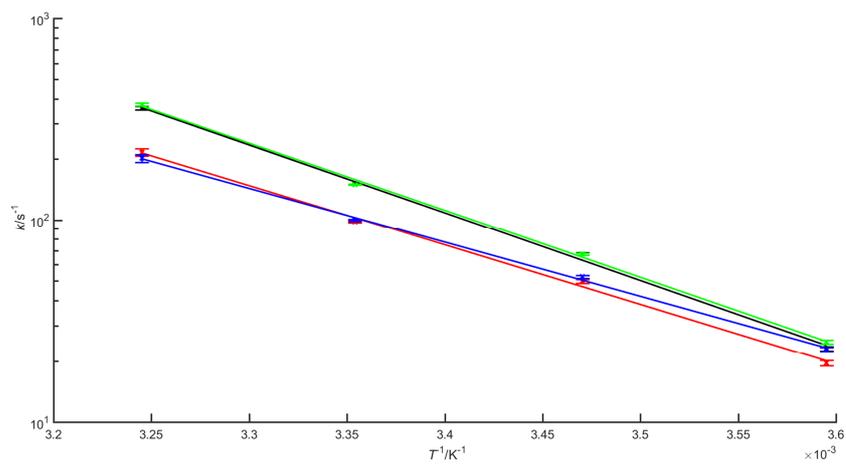


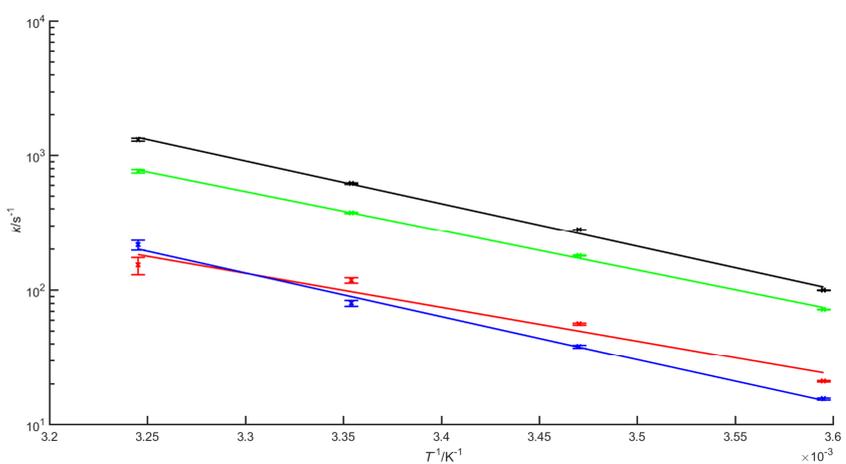
Figure S7. Relative areas of signals of  $[\text{Eu}(\text{do3ap})(\text{D}_2\text{O})]^{2-}$  as a function of the mixing time obtained from  $^{31}\text{P}$  1D-EXSY experiments at  $5\text{ }^\circ\text{C}$ ;  $\text{pD}(25\text{ }^\circ\text{C}) = 8.5$ . The insets show the evolution of the magnetisation of the signal to which the refocusing selective  $180^\circ$  pulse was applied. Symbols: TSAP (+), SAP (o). The solid lines represent the simultaneous fit of both data sets using Equation [2] modified for two-site exchange.



a)



b)



c)

Figure S8: Temperature dependence of exchange rates  $k_{\text{PendSAP}}$  (black),  $k_{\text{CycleSAP}}$  (red),  $k_{\text{PendTSAP}}$  (green) and  $k_{\text{CycleTSAP}}$  (blue) of a)  $[\text{Eu}(\text{dota})(\text{D}_2\text{O})]^-$  b)  $[\text{Eu}(\text{Hdo3ap})(\text{D}_2\text{O})]^-$  c)  $[\text{Eu}(\text{do3ap})(\text{D}_2\text{O})]^{2-}$  fitted using Eyring equation (black line) [4].

Table S2: Exchange and relaxation rates of  $[\text{Eu}(\text{dota})(\text{D}_2\text{O})]^{-}$  [a]

Parameter	Temperature / °C			
	5	15	25	35
$k_{\text{PendSAP}}$	5.58(6)	15.6(3)	35.8(6)	104(3)
$k_{\text{CycleSAP}}$	10.60(7)	30.8(5)	62(1)	147(3)
$k_{\text{PendTSAP}}$	25.81(7)	63.0(4)	126.6(9)	345(24)
$k_{\text{CycleTSAP}}$	52.30(8)	120.4(5)	231(1)	624(31)
$K_{\text{EXSY}}$	0.207(5)	0.25(1)	0.27(1)	0.26(4)
$R_{1\text{Ax. SAP}}$	69.1(1)	55.1(6)	43(1)	30(3)
$R_{1\text{Eq. SAP}}$	22.53(7)	16.2(5)	11(1)	0(5)
$R_{1\text{Ax. TSAP}}$	47.6(2)	45.9(7)	41(1)	130(25)
$R_{1\text{Eq. TSAP}}$	18.3(1)	34(4)	54(8)	17(15)

[a]  $k / \text{s}^{-1}$  are exchange rates,  $R_1 / \text{s}^{-1}$  are longitudinal relaxation rates and  $K_{\text{EXSY}}$  is equilibrium constants calculated as  $K_{\text{EXSY}} = (k_{\text{PendSAP}} + k_{\text{CycleSAP}}) / (k_{\text{PendTSAP}} + k_{\text{CycleTSAP}})$ .

Table S3: Exchange and relaxation rates of  $[\text{Eu}(\text{Hdo3ap})(\text{D}_2\text{O})]^{-}$  [a]

Parameter	Temperature / °C			
	5	15	25	35
$k_{\text{PendSAP}}$	23.2(5)	68(1)	150(1)	357(7)
$k_{\text{CycleSAP}}$	19.6(6)	50(1)	98(1)	216(9)
$k_{\text{PendTSAP}}$	25.0(5)	67.6(8)	150(1)	374(8)
$k_{\text{CycleTSAP}}$	23.0(6)	52.3(9)	100(1)	202(9)
$K_{\text{EXSY}}$	0.89(9)	0.98(7)	0.99(4)	1.0(1)
$R_{1\text{Ax. SAP}}$	69.4(9)	63(1)	57(1)	68(9)
$R_{1\text{Eq. SAP}}$	20(3)	8(3)	9(3)	43(29)
$R_{1\text{Ax. TSAP}}$	54.1(9)	55(1)	52(1)	37(9)
$R_{1\text{Eq. TSAP}}$	22(3)	32(4)	22(3)	0(28)

[a]  $k / \text{s}^{-1}$  are exchange rates,  $R_1 / \text{s}^{-1}$  are longitudinal relaxation rates and  $K_{\text{EXSY}}$  is equilibrium constants calculated as  $K_{\text{EXSY}} = (k_{\text{PendSAP}} + k_{\text{CycleSAP}}) / (k_{\text{PendTSAP}} + k_{\text{CycleTSAP}})$ .

Table S4: Exchange and relaxation rates of  $[\text{Eu}(\text{do3ap})(\text{D}_2\text{O})]^{2-}$  [a]

Parameter	Temperature / °C			
	5	15	25	35
$k_{\text{PendSAP}}$	99.7(3)	280(1)	619(8)	1305(30)
$k_{\text{CycleSAP}}$	21.0(3)	56(1)	118(5)	152(22)
$k_{\text{PendTSAP}}$	71.7(3)	180(1)	374(5)	762(23)
$k_{\text{CycleTSAP}}$	15.5(2)	38.2(9)	80(4)	215(18)
$K_{\text{EXSY}}$	1.39(5)	1.54(8)	1.6(2)	1.5(4)
$R_{1\text{Ax. SAP}}$	73.2(4)	59(1)	42(7)	122(24)
$R_{1\text{Eq. SAP}}$	16(2)	0(6)	0(29)	0(110)
$R_{1\text{Ax. TSAP}}$	59.0(3)	63(1)	58(4)	0(19)
$R_{1\text{Eq. TSAP}}$	23(2)	35(4)	40(18)	32(72)

[a]  $k / \text{s}^{-1}$  are exchange rates,  $R_1 / \text{s}^{-1}$  are longitudinal relaxation rates and  $K_{\text{EXSY}}$  is equilibrium constants calculated as  $K_{\text{EXSY}} = (k_{\text{PendSAP}} + k_{\text{CycleSAP}}) / (k_{\text{PendTSAP}} + k_{\text{CycleTSAP}})$ .

Table S5: Exchange and relaxation rates of  $[\text{Eu}(\text{Hdo3ap})(\text{D}_2\text{O})]^{2-}$  and  $[\text{Eu}(\text{do3ap})(\text{D}_2\text{O})]^{2-}$  as determined by  $^{31}\text{P}$  1D-EXSY at 5 °C.<sup>[a]</sup>

Parameter	$[\text{Eu}(\text{Hdo3ap})(\text{D}_2\text{O})]^{2-}$	$[\text{Eu}(\text{do3ap})(\text{D}_2\text{O})]^{2-}$
$k_{\text{SAP}}$	42(3)	120(3)
$k_{\text{TSAP}}$	45(3)	82(3)
$K_{\text{EXSY}}$	0.93(6)	1.46(4)
$R_{\text{SAP}}$	12(3)	7(2)
$R_{\text{TSAP}}$	9(3)	16(2)

[a]  $k_{\text{SAP}} / \text{s}^{-1}$ ,  $k_{\text{TSAP}} / \text{s}^{-1}$  are exchange rates of exchange from SAP  $\rightarrow$  TSAP and backward respectively,  $R_1 / \text{s}^{-1}$  are longitudinal relaxation rates and  $K_{\text{EXSY}}$  equilibrium constants calculated as  $K_{\text{EXSY}} = k_{\text{SAP}}/k_{\text{TSAP}}$ . It should be highlighted that arm rotation and cycle inversion cannot be separated by  $^{31}\text{P}$  1D-EXSY as a sum of both processes is observed.

Table S6: Calculated energy profile of cyclen inversion of  $[\text{Eu}(\text{dota})(\text{H}_2\text{O})]^-$ . The most favourable pathway is in bold and the rate-determining step is underlined.

Sequence of chelate ring inversions				$\Delta G_{\text{calc}}^{\ddagger}(25\text{ °C}) / \text{kJ mol}^{-1}$								
				SAP	TS 1	int 1	TS 2	int 2	TS 3	int 3	TS 4	TSAP
2	<u>3</u>	4	1	0.00	60.54	19.05	<u>61.99</u>	28.91	57.87	24.77	60.08	-2.84
3	2	4	1	0.00	60.54	21.37	66.90	28.91	57.87	24.77	60.08	-2.84
2	4	3	1	0.00	60.54	19.05	64.48	27.28	63.28	24.77	60.08	-2.84
4	2	3	1	0.00	60.54	21.88	68.08	27.28	63.28	24.77	60.08	-2.84
4	3	2	1	0.00	60.54	21.87	67.01	30.37	72.08	24.77	60.08	-2.84
3	4	2	1	0.00	60.54	21.37	67.42	30.37	72.08	24.77	60.08	-2.84

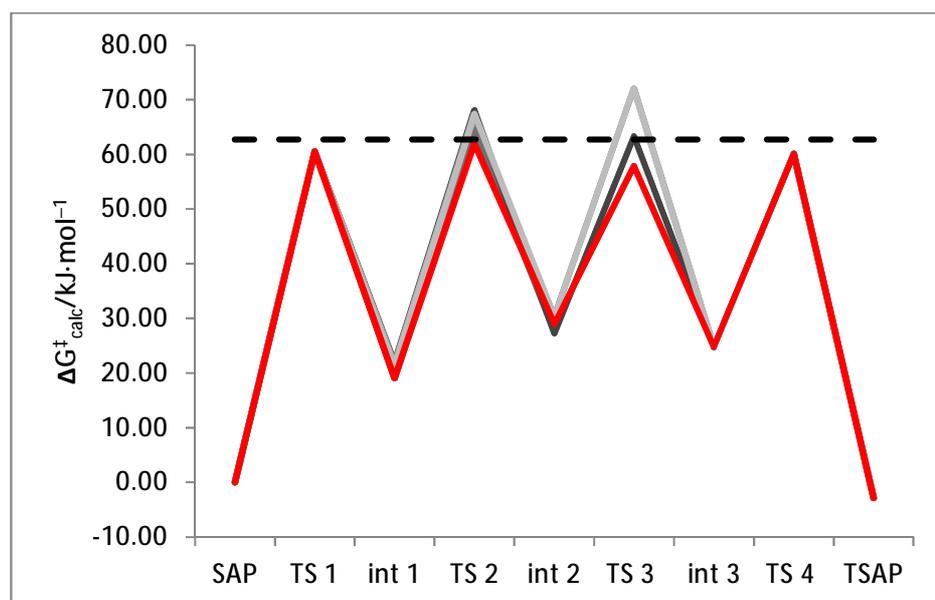


Figure S9: Energy profile calculated for the cyclen inversion of  $[\text{Eu}(\text{dota})(\text{H}_2\text{O})]^-$  at 25 °C. The lowest energy pathway is highlighted in red while the experimental activation free energy is represented by a black dashed line.

Table S7: Calculated energy profile of cyclen inversion of  $[\text{Eu}(\text{Hdo3ap})(\text{H}_2\text{O})]^-$ . The most favourable pathway is in bold and the rate-determining step is underlined.

Sequence of chelate ring inversion				$\Delta G_{\text{calc}}^{\ddagger}(25\text{ }^{\circ}\text{C}) / \text{kJ mol}^{-1}$								
				SAP	TS 1	int 1	TS 2	int 2	TS 3	int 3	TS 4	TSAP
1	2	3	4	0	63.6	19.8	64.7	26.9	55.5	19.2	56.8	-2.6
2	1	3	4	0	51.5	19.4	66.2	26.9	55.5	19.2	56.8	-2.6
1	3	2	4	0	63.6	19.8	72.6	32.4	55.0	19.2	56.8	-2.6
3	1	2	4	0	63.7	21.7	69.8	32.4	55.0	19.2	56.8	-2.6
3	2	1	4	0	63.7	21.7	57.5	24.6	65.9	19.2	56.8	-2.6
2	3	1	4	0	51.5	19.4	60.6	24.6	65.9	19.2	56.8	-2.6
1	2	4	3	0	63.6	19.8	64.7	26.9	69.5	23.0	62.3	-2.6
2	1	4	3	0	51.5	19.4	66.2	26.9	69.5	23.0	62.3	-2.6
1	4	2	3	0	63.6	19.8	62.9	25.7	63.0	23.0	62.3	-2.6
4	1	2	3	0	59.6	21.8	71.6	25.7	63.0	23.0	62.3	-2.6
4	2	1	3	0	59.6	21.8	62.8	29.6	66.4	23.0	62.3	-2.6
2	4	1	3	0	51.5	19.4	65.0	29.6	66.4	23.0	62.3	-2.6
1	4	3	2	0	63.6	19.8	62.9	25.7	71.8	27.9	51.7	-2.6
4	1	3	2	0	59.6	21.8	71.6	25.7	71.8	27.9	51.7	-2.6
1	3	4	2	0	63.6	19.8	72.6	32.4	65.7	27.9	51.7	-2.6
3	1	4	2	0	63.7	21.7	69.8	32.4	65.7	27.9	51.7	-2.6
3	4	1	2	0	63.7	21.7	65.5	34.6	67.4	27.9	51.7	-2.6
4	3	1	2	0	59.6	21.8	68.0	34.6	67.4	27.9	51.7	-2.6
4	2	3	1	0	59.6	21.8	62.8	29.6	62.9	20.0	59.4	-2.6
2	4	3	1	0	51.5	19.4	65.0	29.6	62.9	20.0	59.4	-2.6
4	3	2	1	0	59.6	21.8	68.0	34.6	64.0	20.0	59.4	-2.6
3	4	2	1	0	63.7	21.7	65.5	34.6	64.0	20.0	59.4	-2.6
3	2	4	1	0	63.7	21.7	57.5	24.6	56.4	20.0	59.4	-2.6
2	3	4	1	0	51.5	19.4	60.6	24.6	56.4	20.0	59.4	-2.6

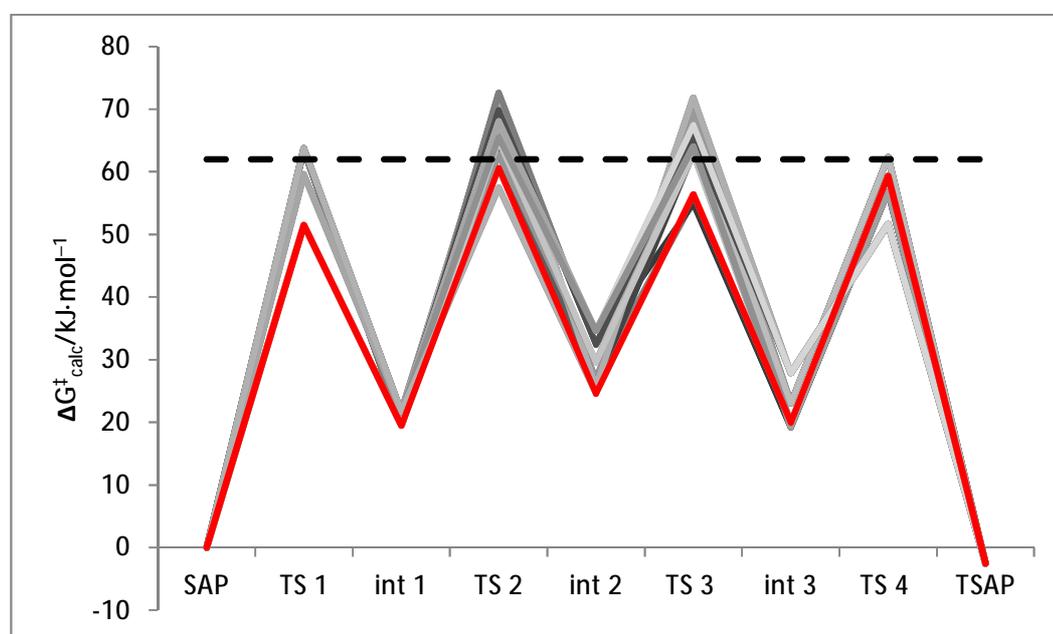


Figure S10: Energy profile calculated for the cyclen inversion of  $[\text{Eu}(\text{Hdo3ap})(\text{H}_2\text{O})]^-$  at 25 °C. The lowest energy pathway is highlighted in red, while the experimental activation free energy is represented by a black dashed line.

Table S8: Calculated energy profile of cyclen inversion of  $[\text{Eu}(\text{do3ap})(\text{H}_2\text{O})]^{2-}$ . The most favourable pathway is in bold and the rate-determining step is underlined.

Sequence of chelate ring inversion				$\Delta G_{\text{calc}}^{\ddagger}(25\text{ }^{\circ}\text{C}) / \text{kJ mol}^{-1}$								
				SAP	TS 1	int 1	TS 2	int 2	TS 3	int 3	TS 4	TSAP
4	3	2	1	0.0	68.1	23.9	67.1	30.5	60.2	21.3	49.6	0.9
4	3	1	2	0.0	68.1	23.9	67.1	30.5	62.9	24.1	66.6	0.9
4	2	3	1	0.0	68.1	23.9	71.8	31.8	67.4	21.3	49.6	0.9
4	2	1	3	0.0	68.1	23.9	71.8	31.8	61.1	31.8	67.7	0.9
4	1	2	3	0.0	68.1	23.9	60.5	33.9	81.7	31.8	67.7	0.9
4	1	3	2	0.0	68.1	23.9	60.5	33.9	66.2	24.1	66.6	0.9
3	4	2	1	0.0	64.4	22.4	70.4	30.5	60.2	21.3	49.6	0.9
3	4	1	2	0.0	64.4	22.4	70.4	30.5	62.9	24.1	66.6	0.9
3	2	4	1	0.0	64.4	22.4	67.7	30.4	71.0	21.3	49.6	0.9
3	2	1	4	0.0	64.4	22.4	67.7	30.4	67.8	33.8	65.1	0.9
3	1	2	4	0.0	64.4	22.4	64.1	34.9	70.9	33.8	65.1	0.9
3	1	<u>4</u>	2	0.0	64.4	22.4	64.1	34.9	64.6	24.1	<u>66.6</u>	0.9
2	3	4	1	0.0	71.1	21.1	68.7	30.4	71.0	21.3	49.6	0.9
2	3	1	4	0.0	71.1	21.1	68.7	30.4	67.8	33.8	65.1	0.9
2	4	3	1	0.0	71.1	21.1	77.5	31.8	67.4	21.3	49.6	0.9
2	4	1	3	0.0	71.1	21.1	77.5	31.8	61.1	31.8	67.7	0.9
2	1	4	3	0.0	71.1	21.1	73.5	37.9	63.9	31.8	67.7	0.9
2	1	3	4	0.0	71.1	21.1	73.5	37.9	79.1	33.8	65.1	0.9
1	3	2	4	0.0	57.7	26.3	73.5	34.9	70.9	33.8	65.1	0.9
1	3	4	2	0.0	57.7	26.3	73.5	34.9	64.6	24.1	66.6	0.9
1	2	3	4	0.0	57.7	26.3	81.5	37.9	79.1	33.8	65.1	0.9
1	2	4	3	0.0	57.7	26.3	81.5	37.9	63.9	31.8	67.7	0.9
1	4	2	3	0.0	57.7	26.3	67.2	33.9	81.7	31.8	67.7	0.9
1	4	3	2	0.0	57.7	26.3	67.2	33.9	66.2	24.1	66.6	0.9

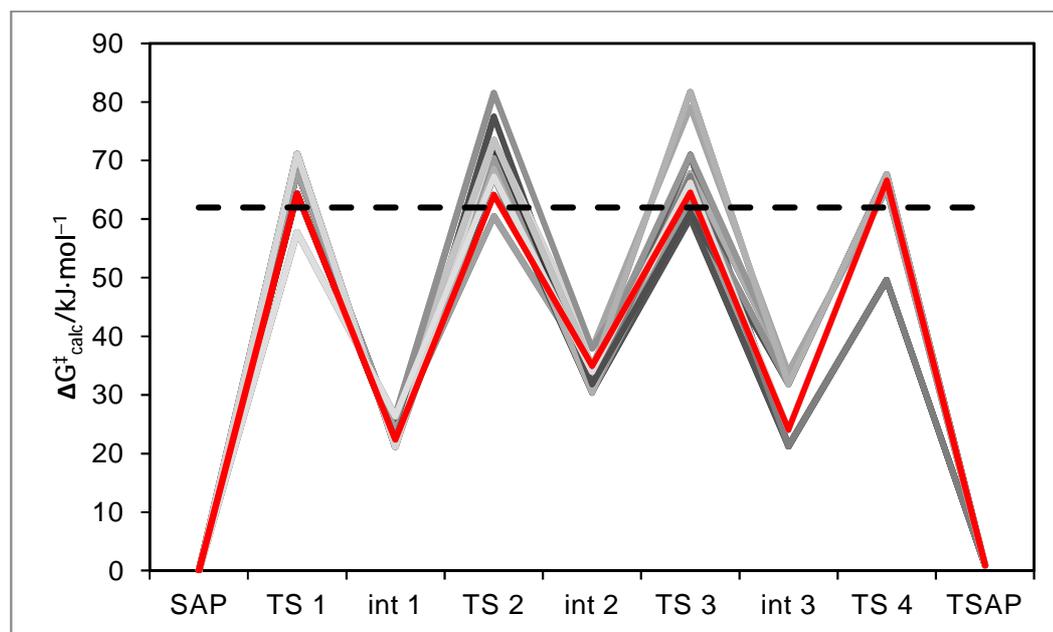


Figure S11: Energy profile calculated for the cyclen inversion of  $[\text{Eu}(\text{do3ap})(\text{H}_2\text{O})]^{2-}$  at 25 °C. The lowest energy pathway is highlighted in red, while the experimental activation free energy is represented by a black dashed line.

Table S9: Contributions to the activation entropy (in  $\text{J K}^{-1} \text{mol}^{-1}$ ) for the ring inversion process responsible for the SAP  $\rightarrow$  TSAP interconversion process (at 25  $^{\circ}\text{C}$ ).

Anion	$\Delta S^{\ddagger}_{\text{CycleSAP}}$		
	Overall	Rotation	Vibration
dota	-3.28	-0.054	-3.23
Hdo3ap	-8.77	0.033	-8.80
do3ap	-14.6	0.12	-14.7

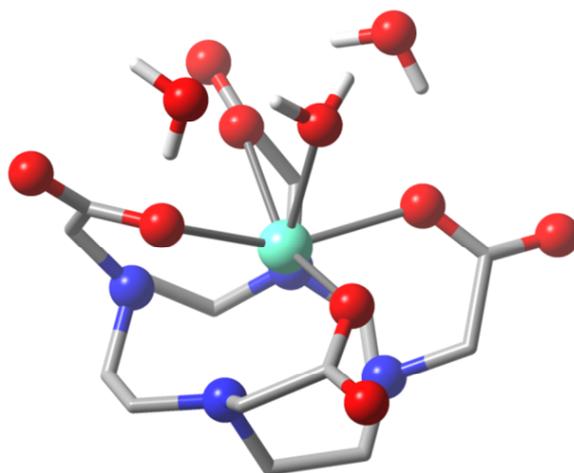


Figure S12. Calculated molecular structure of  $[\text{Eu}(\text{dota})(\text{H}_2\text{O})]^{-}\cdot 2\text{H}_2\text{O}$  in SAP geometry. Hydrogen atoms bonded to carbon atoms are omitted for the sake of clarity.

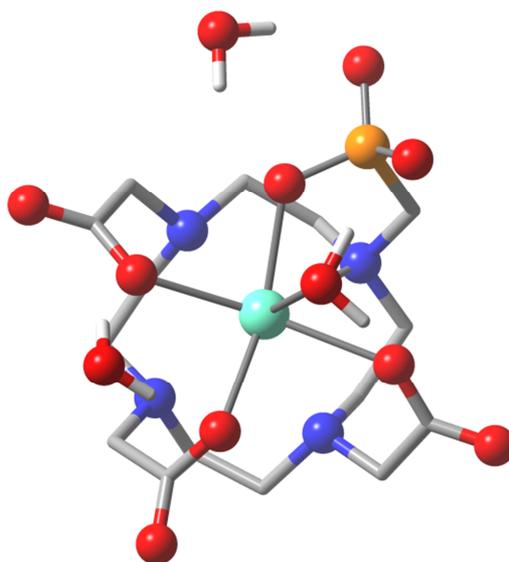


Figure S13. Calculated molecular structure of  $[\text{Eu}(\text{do3ap})(\text{H}_2\text{O})]^{2-}\cdot 2\text{H}_2\text{O}$  in SAP geometry. Hydrogen atoms bonded to carbon atoms are omitted for the sake of clarity.

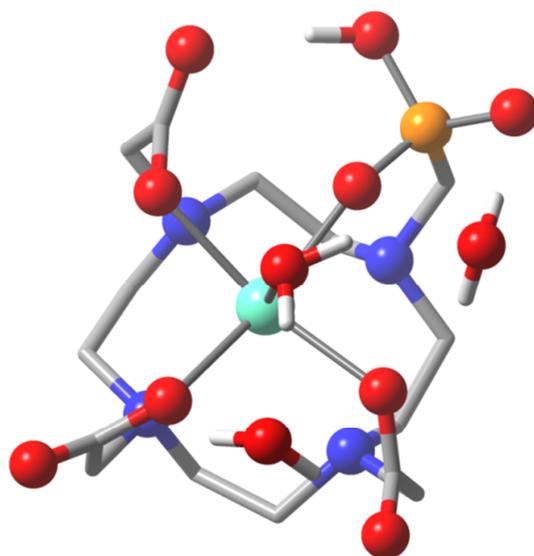


Figure S14. Calculated molecular structure of  $[\text{Eu}(\text{Hdo3ap})(\text{H}_2\text{O})]^- \cdot 2\text{H}_2\text{O}$  in SAP geometry. Hydrogen atoms bonded to carbon atoms are omitted for the sake of clarity.

