

Electronic supplementary information to:

Revealing tunnelling details by normalized differential conductance analysis of transport across molecular junctions

1. Derivation of Eqs. 7,8

Here is a short derivation of the relation between the $V_{t,q}$ values at an arbitrary $NDC=q$ and V_0 and S parameters:

Inserting Eqs. 1 and 2 into Eq. 4 of main text yields:

$$NDC = G \frac{V}{I} = \frac{1 + 2S\left(\frac{V}{V_0}\right) + 3\left(\frac{V}{V_0}\right)^2}{1 + S\left(\frac{V}{V_0}\right) + \left(\frac{V}{V_0}\right)^2} \quad (S.1)$$

Rearranging S.1 and setting $NDC = q$ and $V = V_q$, yields:

$$\left(\frac{V_q}{V_0}\right)^2 + \left(\frac{V_q}{V_0}\right) \cdot S \frac{2-q}{3-q} - \frac{q-1}{3-q} = 0 \quad (S.2)$$

Eq. S.2 is a quadratic equation, with:

$$x^2 + x \cdot SA - B = 0 \quad (S.3)$$

$$x = V_q/V_0; \quad (S.3a)$$

$$A = (2-q)/(3-q); \quad (S.3b)$$

$$B = (q-1)/(3-q); \quad (S.3c)$$

Notice that both A and B are positive for $1 < q < 2$, which is the normal definition range of q .

Solving Eq. S.3 for x , and setting $V_q = V_0 \cdot x$, yields:

$$V_{q\pm} = V_0 \cdot \frac{-SA \pm \sqrt{S^2A^2 + 4B}}{2} \quad (S.4)$$

To extract V_0 the SA term should be eliminated; this can be done using $(-a+b)(-a-b) = -(b^2-a^2)$:

$$-V_{q-} \cdot V_{q+} = \frac{V_0^2}{4} \cdot [S^2A^2 + 4B - S^2A^2] = V_0^2 \cdot B \quad (S.5)$$

And therefore:

$$V_0^2 = \frac{-V_{q-} \cdot V_{q+}}{B} \xrightarrow{S.3c} V_0 = \sqrt{-V_{q-} \cdot V_{q+} \frac{3-q}{q-1}} \quad (S.6)$$

The simplest way to extract S , is by relying on the above-extracted V_0 and using the sum of $V_{q\pm}$ values to eliminate the square-root term:

$$V_{q+} + V_{q-} = -V_0 S A \rightarrow S = -\frac{V_{q+} + V_{q-}}{V_0 A} \xrightarrow{S.3b} S = -\frac{V_{q+} + V_{q-}}{V_0} \cdot \frac{3-q}{2-q} \quad (S.7)$$

2. Statistic over full data sets

The next two figures show that the reproducibility in NDC-V traces is as good as or even better than the reproducibility of the raw data (see heat maps). The smooth Ag gave narrower distribution of NDC (Fig. S1c) and V_0 (Fig. S1d) than the rough Ag (Figs. S2c,d); the poorer reproducibility of the latter is in line with the explanation of ill-controlled defects.

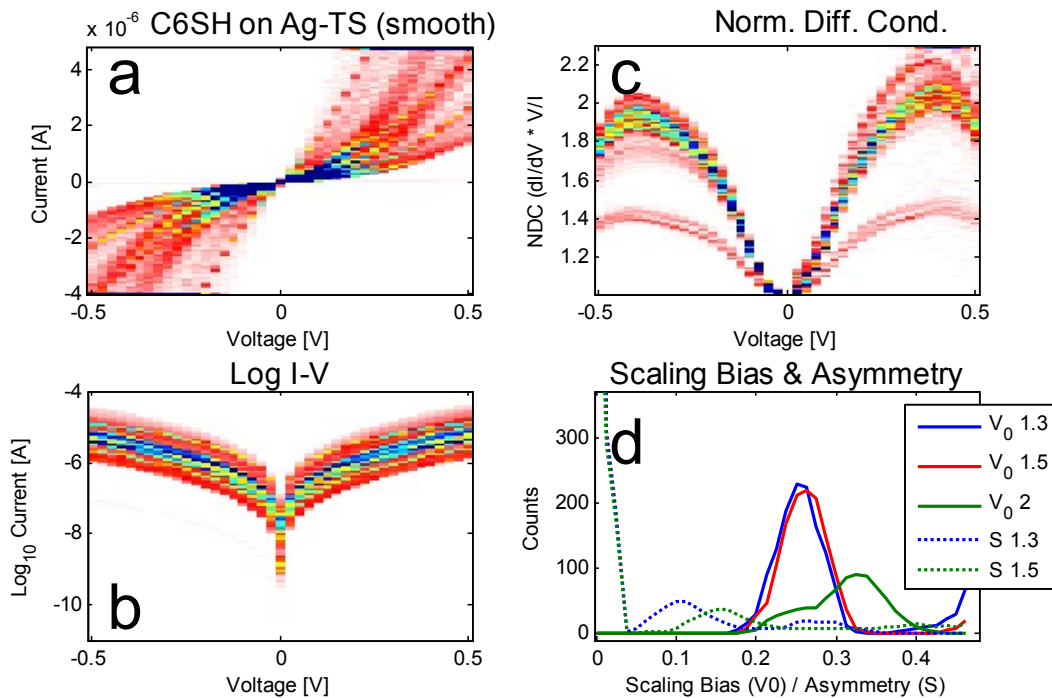


Figure S1: Statistical summary for smooth Ag^{TS}-SC/EGaIn, showing a) heat-maps for linear I-V traces; b) heat-maps for log₁₀(I)-V; c) heat-maps for NDC-V plots; d) histograms of the extracted V_0 and S values (solid and dotted lines respectively), extracted using three values of $q = 1.3, 1.5$

or 2. There is no S value for $q=2$ because S is ill-defined within the parabolic approximation at $q=2$.

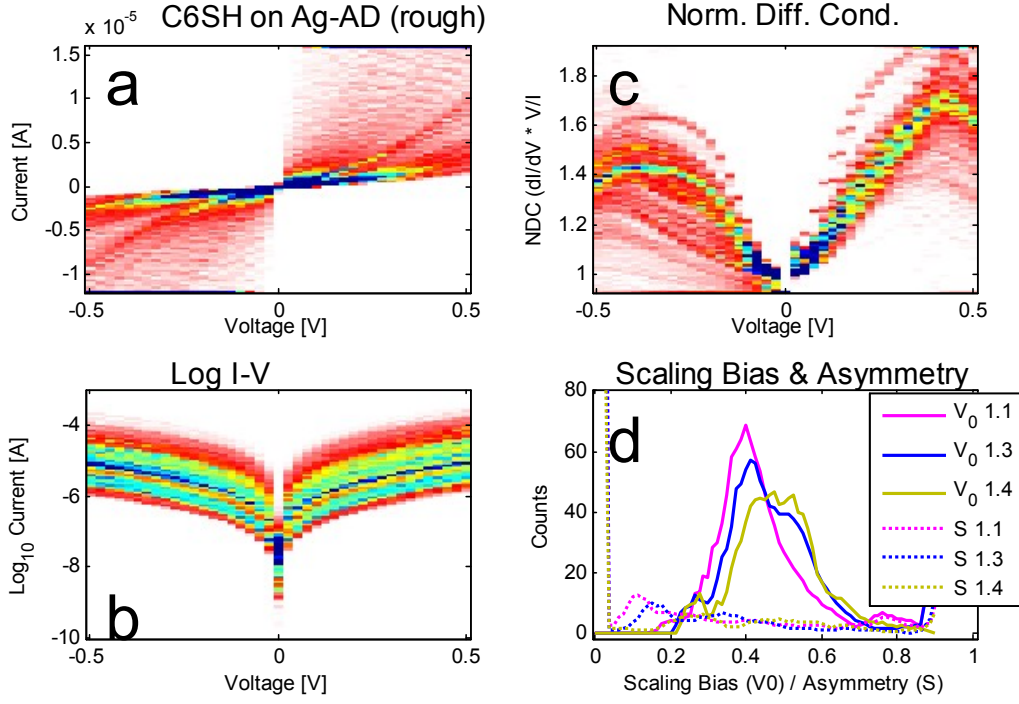


Figure S2: Statistical summary for rough $\text{Ag}^{\text{AD}}\text{-SC/EGaIn}$, showing a) heat-maps for linear I-V traces; b) heat-maps for $\log_{10}(\text{I})\text{-V}$; c) heat-maps for NDC-V plots; d) histograms of the extracted V_0 and S values (solid and dotted lines respectively), extracted using three values of $q = 1.1, 1.3$, or 1.4 . The chosen q values are lower than in Fig. S1, because NDC of Ag^{AD} reaches lower values.

3. Derivation the effective G_{eq} and V_0 in the presence of shunt conductance (Eq. 9)

Substituting the parabolic approximation (Eq. 2) into the tunnelling term (I_{Tnl}) of Eq. 9 yields:

$$I_{\text{Total}} = G_{eq} V \left[1 + \left(\frac{V}{V_0} \right)^2 \right] + G_{\text{shunt}} \cdot V \quad (\text{S.8})$$

where the S term is ignored for shortness. Collecting terms:

$$I_{\text{Total}} = (G_{eq} + G_{\text{shunt}}) V + G_{eq} \frac{V^3}{V_0^2} \quad (\text{S.9})$$

The coefficient multiplying V is the effective equilibrium conductance:

$$G_{eq,eff} = G_{eq} + G_{Shunt} \quad (S.10)$$

Eq. S.9 can be re-written in the form of Eq. 2 by dividing and multiplying the V^3 term by $G_{eq,eff}$:

$$I_{Total} = G_{eq,eff}V + G_{eq,eff}V \cdot \frac{G_{eq} V^2}{G_{eq,eff}V_0^2} \quad (S.11a)$$

Or:

$$I_{Total} = G_{eq,eff}V \left[1 + \left(\frac{V}{V_{0,eff}} \right)^2 \right] \quad (S.11b)$$

It implies that the apparent $V_{0,eff}$ contains an artificial factor:

$$\frac{1}{V_{0,eff}^2} = \frac{G_{eq}}{G_{eq,eff}V_0^2} \quad (S.12)$$

$$\left(\frac{V_{0,eff}}{V_0} \right)^2 = \frac{G_{eq,eff}}{G_{eq}} \quad (S.13)$$