## Electronic Supplementary Information

## A Synergistic Combination of Local Tight Binding Theory and Second Harmonic Generation Elucidating Surface Properties of ZnO Nanoparticles

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## Table of Content

- Calculation of surface vs. bulk number density ratio
- Calculation of the damping coefficient
- Figure S1 - Theoretical un-normalized plots of $\left|P_{z}^{(2)}(2 \omega)\right|^{2}$ as a function polarization angle
- Figure S2 - Effect of surface relaxation on $\left|P_{z}^{(2)}(2 \omega)\right|^{2}$ as a function polarization angle
- Figure S3 - Plots of experimental SHG $\left|P_{z}^{(2)}(2 \omega)\right|^{2}$ as a function polarization angle in the presence of varying concentration of C343
- Figure S4 - Plots of experimental SHG $\left|P_{z}^{(2)}(2 \omega)\right|^{2}$ as a function polarization angle in the presence of varying concentration of C3
- References


## Calculation of surface vs bulk number density ratio

Consider a tetrahedron ${ }^{1}$ of side $a_{T}=1.98 \times 10^{-10} \mathrm{~m}$. The area of one side of this is
$A_{0}=a_{T}^{2} \sqrt{3}=6.79 \times 10^{-20} \mathrm{~m}^{2}$. Now consider a cube with a diagonal $d=2\left(1.98 \times 10^{-10} \mathrm{~m}\right)=3.96 \times 10^{-20} \mathrm{~m}$. The side of this cube is $a_{C}=\frac{d}{\sqrt{3}}=2.28 \times 10^{-10} \mathrm{~m}$,

So the volume of this cube is $V_{0}=a_{C}^{3}=1.19 \times 10^{-29} \mathrm{~m}^{3}$. Now the surface number density and the volume number density are given by,

$$
N_{S}=\frac{4 \pi r^{2}}{A_{0}}, N_{B}=\frac{4 \pi r^{3}}{3 V_{0}}
$$

The ratio of the surface to volume densities is

$$
\frac{N_{S}}{N_{V}}=\frac{3 V_{0}}{A_{0} r}=\frac{5.27 \times 10^{-10} \mathrm{~m}}{r}
$$

This indicates that surface contributions do not dominate until the radius of the nanoparticle is less than 5 Å.

## Calculation of the damping coefficient

Here we calculate the value of the damping coefficient, $\gamma$, for C343. We assume that the form is given $b^{2,3}$

$$
\gamma=\frac{1}{4 \pi \varepsilon_{0}} \frac{4 \omega_{0}^{3} e^{2}\langle\pi| r\left|\pi^{*}\right\rangle^{2}}{3 \hbar c^{3}} .
$$

Here we take the constant terms in MKS units to be,

$$
\frac{1}{4 \pi \varepsilon_{0}}=8.99 \times 10^{9} \frac{\mathrm{~N} \cdot \mathrm{~m}^{2}}{C^{2}}, c=3.0 \times 10^{8} \mathrm{~m} / \mathrm{s}, e=1.6 \times 10^{-19} \mathrm{C}, \hbar=1.054 \times 10^{-34} \mathrm{~J} \cdot \mathrm{~s} .
$$

We take the resonant frequency for the C343 molecule to be $\omega_{0}=4.34 \times 10^{15} \mathrm{~Hz}$.
The dipole amplitude is determined by assuming the ionization energy is $E_{P}=-14.14 \mathrm{eV} .{ }^{4}$ We assume the Pi pseudo wave functions can be approximated as $\phi_{P} \approx r e^{-\mu r} \cos (\theta)$. Then we have $-\frac{(\hbar \mu)^{2}}{2 m}=-E_{p}$, which gives us $\mu=1.92 A^{-1}$. With this in mind we take the dipole amplitude to be $\langle\pi| r\left|\pi^{*}\right\rangle \approx 8.5 \times 10^{-8} \mathrm{~m}$.

This large amplitude on the order of hundreds of Angstroms is due to delocalization of the $\pi^{*}$ orbital over the area of the coumarin molecule. We realize this crude calculation will mostly serve to obtain the magnitude of $\gamma$ for this process. Substituting all these quantities into the equation above yields $\gamma \approx 6.4 \times 10^{13} \mathrm{~s}^{-1}$.

This is in agreement with the values reported previously for various substituted coumarin dyes., ${ }^{5,6}$ This term is far too small to affect the denominator in any of the calculations of $\chi_{i j k}^{2}$ in the main text.

## Supplementary Data



Figure S1 Plots of $\left|P_{z}^{(2)}(2 \omega)\right|^{2}$ as a function of polarization angle of the fundamental field (equation 2) as calculated using TB model. These represent SHG contributions from (a) Zn-terminated surfaces, (b) Oterminated surface, and (c) the bulk of ZnO . The overall contribution is shown in (d).


Figure S2 Effect of surface relaxation, as explored by varying the $\mathrm{Zn}-\mathrm{O}$ bond length, on the plots of $\left|P_{z}^{(2)}(2 \omega)\right|^{2}$ as a function of polarization angle of the fundamental field (equation 2 ) as calculated using TB model. These represent SHG contributions from (a) ZnO NP only, without C343 and (b) ZnO NP and C343.


Figure S3 Plots of experimental SHG $\left|P_{z}^{(2)}(2 \omega)\right|^{2}$ as a function of polarization angle of the fundamental field for ZnO NPs with varying concentration of C343 dye ( $5 \mathrm{uM}, 10 \mathrm{uM}, 20 \mathrm{uM}, 35 \mathrm{uM}, 46 \mathrm{uM}$, and 70 uM ). The $\left|P_{z}^{(2)}(2 \omega)\right|^{2}$ of ZnO NP (no dye) is also shown as black markers.


Figure S4 Plots of experimental SHG $\left|P_{z}^{(2)}(2 \omega)\right|^{2}$ as a function of polarization angle of the fundamental field for ZnO NPs with varying concentration of C3 dye ( $5 \mathrm{uM}, 10 \mathrm{uM}, 21 \mathrm{uM}, 30 \mathrm{uM}, 42 \mathrm{uM}$, and 75 uM ). The $\left|P_{z}^{(2)}(2 \omega)\right|^{2}$ of ZnO NP (no dye) is also shown as black markers.

## References

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