

Electronic Supplementary Information for “Ultrafast Coherent Vibrational Dynamics in Dimethyl Methylphosphonate Radical Cation”

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SI Measurement of Pulse Duration (FROG)

A home-built Frequency Resolved Optical Gating (FROG) setup was used to measure the spectrograms for each pulse and the time-dependent electric fields were retrieved with an open-source MATLAB code ¹ based on the retrieval algorithm in Ref. ². Figure S1 shows the spectrograms (top panels) and retrieved temporal electric fields (bottom panels) for the 800 nm, 1200 nm, and 1500 nm pump pulses, as well as the 800 nm probe pulse. The time-dependent intensity is shown in blue and the temporal phase shown in red. The retrieved FWHM pulse durations are indicated in each panel.

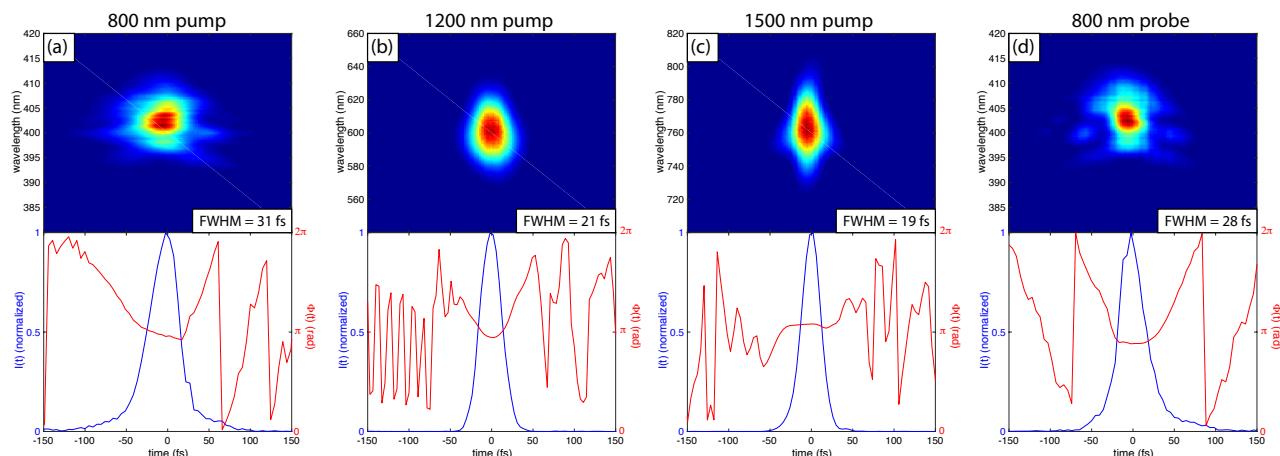


Figure S1: Two-dimensional spectrograms recorded with SHG-FROG setup (top panels) and retrieved time-dependent electric fields (bottom panels).

SII Xe⁺ Cross-Correlation Measurements

In order to both verify the pulse duration and identify the zero delay position of the stage, the vacuum chamber was filled with Xe gas and pump-probe measurements taken using $6 \times 10^{13} \text{ W cm}^{-2}$ pump pulses at 800 and 1500 nm and $1 \times 10^{13} \text{ W cm}^{-2}$ probe pulses at 800 nm. The transient Xe⁺ signals are shown in Figure S2.

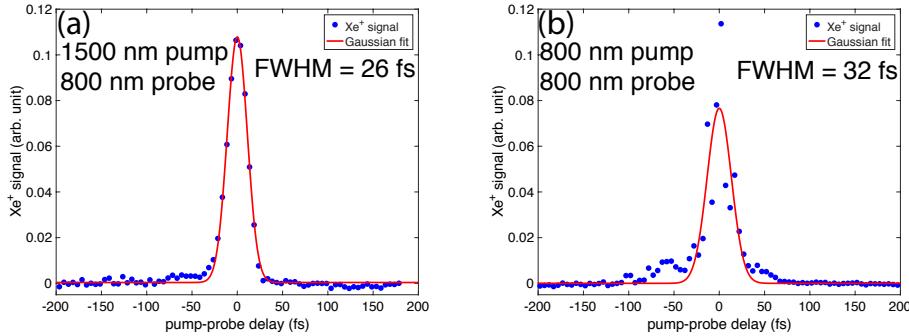


Figure S2: Cross-correlation measurements of Xe⁺ signal taken with (a) 1500 nm pump - 800 nm probe, and (b) 800 nm pump - 800 nm probe. Gaussian fits to the experimental data and extracted FWHM values are shown.

SIII Additional pump-probe measurements

A 1600 nm pump pulse was also tested to assess the hypothesis that adiabatic ionization is needed to effectively prepare the coherent state in DMMP⁺ because the pulse duration of the 1600 nm pulse from the OPA increases to 28 fs due to the limited phase matching bandwidth (Figure S3(a)-(b)). Large oscillation amplitudes in the yields of DMMP⁺ and its dissociation products are observed (Figure S3(c)). Additional pump and probe energies were tested with the 800 nm pump setup in order to determine the combination of pump and probe energies that produces the largest amplitude oscillations. Decreasing the energy of either pump or probe only decreased the oscillation amplitude (Figure S4).

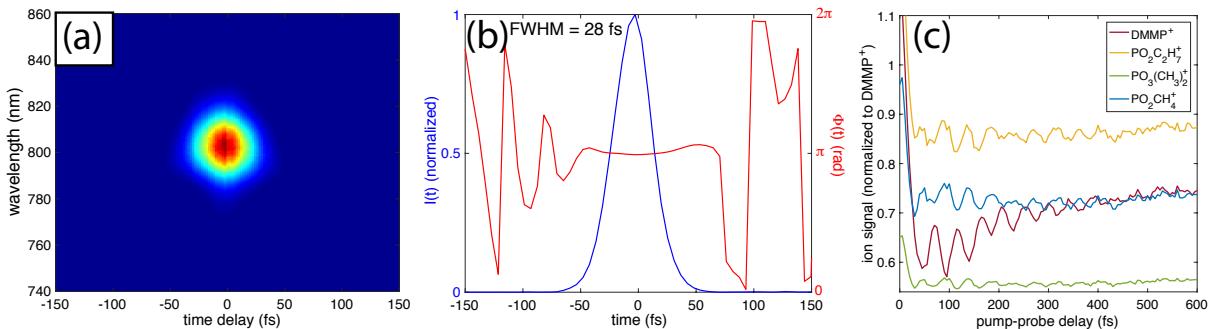


Figure S3: (a) FROG spectrogram of 1600 nm pump. (b) Retrieved electric field. (c) Transient ion signals of DMMP⁺ and dissociation products with 1600 nm pump.

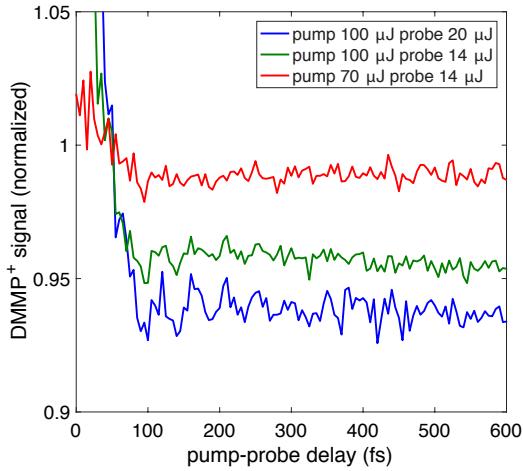


Figure S4: Transient ion signals of DMMP^+ at various pump and probe energies for 800 nm pump. Signals are normalized to the yield at negative time delays.

SIV Results of calculations

Table S1 reports the calculated normal modes of DMMP^+ at the BPW91 and B3LYP levels. Both the harmonic and anharmonic frequencies are shown. The coherently excited normal mode is highlighted in red. Table S2 reports the differences in bond lengths and bond angles between the optimized neutral and cation geometries of DMMP. The atom labels are given in Figure S5. All radii $R(x,y)$ are given in Angstroms and all angles $A(x,y,z)$ are given in degrees. The two coordinates contributing to the coherently excited normal mode are highlighted in red.

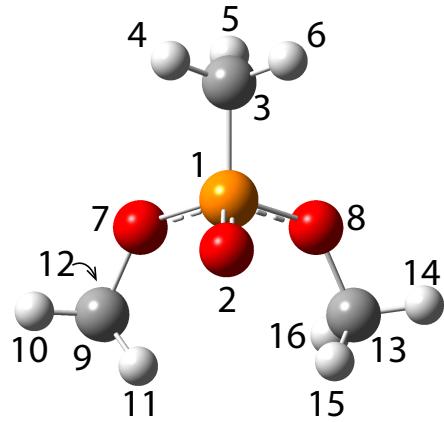


Figure S5: DMMP structure with atoms labeled according to the labels in Table S2.

| BPW91 | ν_{harm} | ν_{anharm} | I_{harm} | I_{anharm} | B3LYP | ν_{harm} | ν_{anharm} | I_{harm} | I_{anharm} |
|--------------|---------------------|-----------------------|-------------------|---------------------|--------------|---------------------|-----------------------|-------------------|---------------------|
| mode | (cm $^{-1}$) | (cm $^{-1}$) | km/mol | km/mol | | (cm $^{-1}$) | (cm $^{-1}$) | km/mol | km/mol |
| 1 | 40.91 | 61.33 | 1.69 | 1.58 | | 19.27 | -467.96 | 0.001 | 221.11 |
| 2 | 80.87 | 43.91 | 1.70 | 1.16 | | 69.54 | -119.57 | 0.23 | 3.69 |
| 3 | 97.04 | 63.32 | 1.23 | 0.58 | | 84.03 | 74.78 | 2.96 | 2.19 |
| 4 | 120.73 | 94.20 | 1.48 | 2.73 | | 99.72 | 83.09 | 2.46 | 4.50 |
| 5 | 151.96 | 121.67 | 2.03 | 6.14 | | 133.60 | 160.11 | 4.54 | 9.09 |
| 6 | 161.71 | 147.04 | 6.31 | 27.54 | | 154.69 | 135.60 | 0.77 | 11.28 |
| 7 | 166.71 | 152.59 | 14.69 | 13.58 | | 166.52 | 159.89 | 15.15 | 16.07 |
| 8 | 232.45 | 230.90 | 7.77 | 13.63 | | 204.71 | 218.16 | 10.28 | 4.58 |
| 9 | 236.88 | 217.98 | 4.38 | 11.21 | | 253.09 | 245.36 | 3.46 | 2.54 |
| 10 | 270.05 | 257.44 | 1.63 | 34.61 | | 271.82 | 268.02 | 8.01 | 6.20 |
| 11 | 270.43 | 260.17 | 4.85 | 5.21 | | 346.10 | 331.31 | 10.01 | 3.79 |
| 12 | 456.72 | 444.07 | 33.44 | 34.79 | | 471.50 | 462.55 | 26.80 | 25.72 |
| 13 | 610.71 | 583.28 | 4.86 | 2.59 | | 659.12 | 641.83 | 24.98 | 23.41 |
| 14 | 686.55 | 649.17 | 0.41 | 0.85 | | 760.83 | 715.42 | 0.64 | 0.92 |
| 15 | 772.79 | 754.66 | 17.55 | 15.98 | | 766.97 | 742.20 | 4.70 | 8.98 |
| 16 | 863.04 | 827.65 | 6.71 | 49.04 | | 864.02 | 834.09 | 13.13 | 6.70 |
| 17 | 863.82 | 832.65 | 9.71 | 97.59 | | 934.66 | 910.52 | 15.19 | 8.37 |
| 18 | 913.70 | 898.08 | 22.36 | 16.42 | | 952.94 | 935.45 | 34.93 | 28.81 |
| 19 | 946.88 | 916.91 | 5.08 | 11.09 | | 1044.26 | 1005.66 | 180.21 | 88.76 |
| 20 | 1036.50 | 1009.49 | 249.38 | 65.55 | | 1065.54 | 1026.02 | 371.47 | 310.84 |
| 21 | 1105.33 | 1075.83 | 14.25 | 0.97 | | 1165.06 | 1136.55 | 2.74 | 1.53 |
| 22 | 1112.65 | 1079.99 | 2.44 | 4.54 | | 1168.16 | 1137.93 | 0.20 | 0.72 |
| 23 | 1138.09 | 1112.54 | 3.31 | 20.37 | | 1193.50 | 1156.89 | 31.98 | 6.54 |
| 24 | 1138.17 | 1114.13 | 7.49 | 6.20 | | 1193.89 | 1159.18 | 17.05 | 6.04 |
| 25 | 1325.94 | 1293.71 | 32.06 | 26.55 | | 1375.94 | 1345.20 | 32.59 | 28.91 |
| 26 | 1400.74 | 1353.62 | 7.30 | 11.82 | | 1454.26 | 1417.39 | 17.40 | 18.97 |
| 27 | 1403.29 | 1359.26 | 2.28 | 55.20 | | 1454.42 | 1417.39 | 10.49 | 11.43 |
| 28 | 1409.46 | 1365.70 | 24.75 | 35.02 | | 1476.73 | 1440.99 | 3.58 | 1145.53 |
| 29 | 1411.58 | 1371.51 | 32.34 | 22.24 | | 1478.22 | 1442.73 | 4.47 | 5.19 |
| 30 | 1414.79 | 1376.17 | 12.53 | 6.19 | | 1481.76 | 1433.39 | 13.10 | 198.80 |
| 31 | 1415.36 | 1375.39 | 9.75 | 12.14 | | 1491.56 | 1443.71 | 0.64 | 6.07 |
| 32 | 1443.52 | 1402.71 | 106.92 | 90.26 | | 1502.53 | 1450.00 | 7.20 | 6.83 |
| 33 | 1460.52 | 1411.80 | 72.77 | 51.57 | | 1507.95 | 1455.68 | 59.09 | 28.08 |
| 34 | 2978.86 | 2854.75 | 74.53 | 354.81 | | 3059.30 | 2942.92 | 16.93 | 19.38 |
| 35 | 2981.99 | 2850.16 | 21.29 | 671.12 | | 3078.34 | 2980.18 | 0.53 | 5.50 |
| 36 | 3002.87 | 2880.43 | 16.53 | 18.41 | | 3079.80 | 2976.54 | 7.36 | 4.70 |
| 37 | 3073.87 | 2899.24 | 5.61 | 27.73 | | 3149.72 | 3005.34 | 6.74 | 5.21 |
| 38 | 3074.81 | 2909.01 | 6.22 | 19.48 | | 3150.15 | 3005.92 | 5.39 | 4.33 |
| 39 | 3096.35 | 2947.64 | 6.79 | 5.58 | | 3176.98 | 3036.45 | 2.61 | 2.40 |
| 40 | 3099.79 | 2952.78 | 6.10 | 4.72 | | 3177.53 | 3034.16 | 2.66 | 3.88 |
| 41 | 3113.58 | 2937.77 | 17.65 | 26.30 | | 3201.86 | 3056.59 | 1.45 | 1.31 |
| 42 | 3114.85 | 2941.32 | 13.77 | 20.43 | | 3202.33 | 3057.00 | 0.65 | 0.26 |

Table S1: Calculated normal modes of DMMP $^{+}$.

| coordinate | BPW91 | | | B3LYP | | |
|-------------|---------|--------|---------|---------|--------|---------|
| | neutral | cation | % diff. | neutral | cation | % diff. |
| R(1,2) | 1.497 | 1.540 | 2.811 | 1.484 | 1.582 | 6.555 |
| R(1,3) | 1.813 | 1.783 | 1.622 | 1.804 | 1.775 | 1.591 |
| R(1,7) | 1.646 | 1.614 | 1.950 | 1.627 | 1.565 | 3.836 |
| R(1,8) | 1.630 | 1.615 | 0.932 | 1.611 | 1.570 | 2.551 |
| R(3,4) | 1.097 | 1.097 | 0.073 | 1.090 | 1.091 | 0.110 |
| R(3,5) | 1.098 | 1.097 | 0.073 | 1.091 | 1.091 | 0.046 |
| R(3,6) | 1.098 | 1.098 | 0.027 | 1.091 | 1.092 | 0.018 |
| R(7,9) | 1.445 | 1.457 | 0.851 | 1.438 | 1.471 | 2.274 |
| R(8,13) | 1.446 | 1.457 | 0.754 | 1.438 | 1.469 | 2.148 |
| R(9,10) | 1.097 | 1.095 | 0.246 | 1.090 | 1.088 | 0.183 |
| R(9,11) | 1.096 | 1.100 | 0.347 | 1.089 | 1.088 | 0.046 |
| R(9,12) | 1.101 | 1.096 | 0.427 | 1.093 | 1.085 | 0.741 |
| R(13,14) | 1.099 | 1.100 | 0.091 | 1.092 | 1.088 | 0.339 |
| R(13,15) | 1.099 | 1.095 | 0.346 | 1.091 | 1.088 | 0.312 |
| R(13,16) | 1.095 | 1.096 | 0.064 | 1.088 | 1.086 | 0.211 |
| A(2,1,3) | 116.55 | 119.49 | 2.527 | 116.46 | 116.31 | 0.132 |
| A(2,1,7) | 113.69 | 108.27 | 4.766 | 113.29 | 106.83 | 5.697 |
| A(2,1,8) | 117.33 | 108.11 | 7.858 | 116.85 | 103.78 | 11.189 |
| A(3,1,7) | 106.01 | 104.50 | 1.431 | 106.09 | 106.80 | 0.666 |
| A(3,1,8) | 100.04 | 104.49 | 4.442 | 100.71 | 106.90 | 6.143 |
| A(7,1,8) | 101.16 | 111.98 | 10.701 | 101.57 | 116.65 | 14.851 |
| A(1,3,4) | 110.75 | 110.51 | 0.215 | 110.71 | 109.84 | 0.791 |
| A(1,3,5) | 109.25 | 108.64 | 0.551 | 109.31 | 109.01 | 0.271 |
| A(1,3,6) | 108.83 | 108.63 | 0.183 | 109.02 | 109.02 | 0.003 |
| A(4,3,5) | 109.66 | 109.80 | 0.129 | 109.56 | 109.74 | 0.163 |
| A(4,3,6) | 109.58 | 109.79 | 0.193 | 109.52 | 109.53 | 0.005 |
| A(5,3,6) | 108.74 | 109.44 | 0.638 | 108.69 | 109.69 | 0.922 |
| A(1,7,9) | 120.04 | 129.32 | 7.732 | 121.29 | 131.30 | 8.249 |
| A(1,8,13) | 119.42 | 129.34 | 8.307 | 120.70 | 131.79 | 9.192 |
| A(7,9,10) | 110.97 | 111.81 | 0.757 | 110.81 | 110.24 | 0.508 |
| A(7,9,11) | 106.27 | 106.32 | 0.757 | 106.41 | 17.60 | 1.112 |
| A(7,9,12) | 110.38 | 106.12 | 3.860 | 110.30 | 105.20 | 4.624 |
| A(10,9,11) | 110.20 | 111.46 | 1.646 | 110.28 | 111.85 | 1.429 |
| A(10,9,12) | 109.66 | 111.46 | 1.646 | 109.64 | 110.90 | 1.150 |
| A(11,9,12) | 109.31 | 109.18 | 0.118 | 109.35 | 110.78 | 1.312 |
| A(8,13,14) | 110.36 | 106.25 | 3.721 | 110.25 | 106.35 | 3.536 |
| A(8,13,15) | 110.73 | 111.85 | 1.006 | 110.57 | 110.84 | 0.247 |
| A(8,13,16) | 105.97 | 106.16 | 0.174 | 106.20 | 105.90 | 0.283 |
| A(14,13,16) | 110.13 | 111.68 | 1.407 | 110.12 | 111.69 | 0.990 |
| A(14,13,16) | 109.69 | 109.14 | 0.499 | 109.70 | 110.79 | 0.990 |
| A(15,13,16) | 109.87 | 111.47 | 1.455 | 109.93 | 111.02 | 0.928 |

Table S2: Coordinate differences.

SV Curve fitting results

Table S3 presents the fitting coefficients to Eq. S.1

$$S(\tau) = ae^{-\tau/T} \left[\sin \left(\frac{2\pi}{t} \tau + \phi \right) + b \right] + c, \quad (\text{S.1})$$

where the curves are reported in the main text, Figure 3. The reported errors in the table denote 95% confidence intervals. The R^2 values for each fit are also given.

| ion | λ (nm) | a | T (fs) | t (fs) | ϕ (rad) | b | c | R^2 |
|-------------------------------------|----------------|-------------------|--------------|----------------|---------------|----------------|-------------------|-------|
| DMMP ⁺ | 800 | 0.019 ± 0.008 | 180 ± 10 | 45.8 ± 0.8 | 4.2 ± 0.5 | 0.3 ± 0.2 | 0.937 ± 0.002 | 0.51 |
| | 1200 | 0.072 ± 0.007 | 150 ± 10 | 45.3 ± 0.3 | 4.1 ± 0.2 | -2.5 ± 0.2 | 0.780 ± 0.002 | 0.98 |
| | 1500 | 0.100 ± 0.009 | 150 ± 10 | 45.0 ± 0.6 | 4.1 ± 0.1 | -1.8 ± 0.1 | 0.805 ± 0.002 | 0.98 |
| $\text{PO}_2\text{C}_2\text{H}_7^+$ | 1200 | 0.033 ± 0.009 | 130 ± 30 | 45.7 ± 0.9 | 1.4 ± 0.4 | -1.3 ± 0.3 | 1.113 ± 0.001 | 0.81 |
| | 1500 | 0.043 ± 0.009 | 150 ± 30 | 45.1 ± 0.4 | 1.4 ± 0.2 | -0.2 ± 0.1 | 1.06 ± 0.001 | 0.81 |
| $\text{PO}_3(\text{CH}_3)_2^+$ | 1200 | 0.007 ± 0.002 | 230 ± 60 | 45.9 ± 0.9 | 1.3 ± 0.5 | -4 ± 1 | 0.374 ± 0.002 | 0.86 |
| | 1500 | 0.014 ± 0.004 | 170 ± 50 | 45.5 ± 0.6 | 1.1 ± 0.3 | -0.5 ± 0.2 | 0.329 ± 0.001 | 0.72 |
| PO_2CH_4^+ | 1200 | 0.018 ± 0.006 | 230 ± 70 | 45.0 ± 0.7 | 0.6 ± 0.4 | -1.9 ± 0.6 | 0.931 ± 0.003 | 0.77 |
| | 1500 | 0.04 ± 0.01 | 140 ± 40 | 45.2 ± 0.7 | 0.9 ± 0.3 | 0.4 ± 0.2 | 0.823 ± 0.001 | 0.70 |

Table S3: Curve fitting coefficients for all transient ions.

References

- [1] S. Byrnes and A. Wyatt, *Frequency Resolved Optical Gating*, MATLAB File Exchange. Last accessed October 13, 2017.
- [2] D. J. Kane, *IEEE J. Quant. Electron.*, 1999, **35**, 421–431.