

## Supplementary Information

*Details make the difference: A family of heterometallic complexes with cube-like {Cu<sub>3</sub>Mn(μ<sub>3</sub>-O)<sub>4</sub>} and double open cube-like {Cu<sub>3</sub>Mn(μ-O)<sub>2</sub>(μ<sub>3</sub>-O)<sub>2</sub>} tetrานuclear cores*

O. Stetsiuk, O. V. Nesterova, V. N. Kokozay, K. V. Domasevitch, I. V. Omelchenko, O. V. Shishkin, B. Vranovičová, R. Boča, A. J. L. Pombeiro, S. R. Petrusenko

**Table S1.** Calculated magnetic parameters for **1–5**.<sup>a</sup>

Complex	<i>M<sub>r</sub></i>	<i>g<sub>Mn</sub></i>	<i>g<sub>Cu</sub></i>	<i>J<sub>2</sub>/hc</i>	<i>J<sub>4</sub>/hc</i>	<i>D<sub>Mn</sub>/hc</i>	<i>(zj)/hc</i>	<i>χ<sub>TIM</sub></i> <sup>b</sup>	<i>R(χ)</i>	<i>R(M)</i>						
-fit								/%								
1-a	1375.07	1.859	2.313	-54.8	-27.0	-13.6	-0.075	+0.2	4.0	3.4						
1-b		1.850	2.087	-21.8	-39.5	-28.7	~0	+0.9	4.8	4.4						
2-a	1088.49	1.869	2.349	-54.8	-27.0	-14.4	-0.013	+14.4	3.5	4.3						
2-b		1.851	2.065	-21.7	-39.5	-28.7	0.028	+2.6	4.0	5.6						
3-a	1064.25	1.988	2.009	-45.0	-37.5	-2.8	-0.079	+12.2	2.2	0.7						
3-b		1.976	2.004	-35.0	-45.9	-0.3	-0.050	+14.1	1.5	0.8						
4-a	1057.12	2.000	2.000	-52.5	-39.1	-2.5	~0	+15.0	1.9	1.0						
4-b		2.000	2.004	-35.0	-46.9	-0.3	-0.047	+14.7	1.3	1.0						
5-a	2340.09	1.851 <sup>c</sup>	2.178	-22.7	-11.6	-23.4	0.268	+40.0	2.5	3.3						
5-b		1.889 <sup>c</sup>	2.336	-14.9	-28.3	-19.7	-0.063	+40.0	0.6	3.1						

<sup>a</sup> Coupling constants conforming the definition  $\hat{H}_{ij} = -J(\vec{S}_i \cdot \vec{S}_j)$  in cm<sup>-1</sup>. *J<sub>2</sub>* – in two bases, *J<sub>4</sub>* – within four walls.

<sup>b</sup> Temperature independent magnetism *χ<sub>TIM</sub>* in units of 10<sup>-9</sup> m<sup>3</sup> mol<sup>-1</sup> (SI).

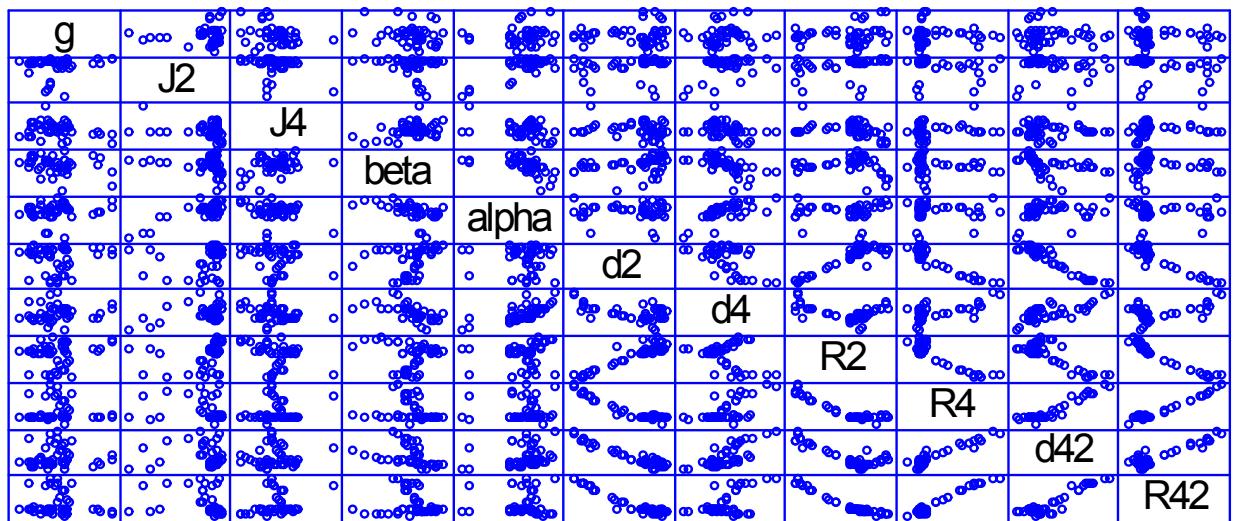
<sup>c</sup> *g(Mn<sup>II</sup>)* = 1.950 and 1.956.

**Table S2.** Data selected for the correlations for 6 new hits.

↓Complex	<i>g<sub>Cu</sub></i>	<i>J<sub>2</sub></i>	<i>J<sub>4</sub></i>	<i>β<sub>M-O-M</sub></i>	<i>α<sub>M-O-M</sub></i>	<i>R<sub>M-M</sub></i>	<i>R<sub>M-M</sub></i>	<i>R<sub>M-O</sub></i>	<i>R<sub>M-O</sub></i>	<i>d<sub>4-d<sub>2</sub></sub></i>	<i>R<sub>4-R<sub>2</sub></sub></i>
Abbrev. →	<i>g</i>	<i>J2</i>	<i>J4</i>	beta	alpha	<i>d2</i>	<i>d4</i>	<i>R2</i>	<i>R4</i>	<i>d42</i>	<i>R42</i>
<b>1</b>	2.313	-54.8	-27.0	102.53	97.47	3.510	3.144	2.239	1.959	-0.366	-0.280
<b>2</b>	2.349	-54.8	-27.0	101.96	97.81	3.501	3.177	2.253	1.957	-0.324	-0.296
<b>3</b>	2.009	-45.0	-37.5	102.81	97.82	3.496	3.136	2.226	1.950	-0.360	-0.276
<b>4</b>	2.000	-52.5	-39.1	99.55	98.61	3.407	3.158	2.220	1.961	-0.249	-0.259
<b>5 unit A</b>	2.178	-22.7	-11.6	100.64	99.27	3.542	3.210	2.292	1.953	-0.332	-0.339
<b>5 unit B</b>	2.178	-22.7	-11.6	98.32	99.88	3.509	3.235	2.307	1.854	-0.274	-0.453

**Table S3.** Pair correlation coefficients for 41 + 6 hits.

	g	J2	J4	beta	alpha	d2	d4	R2	R4	d42	R42
g		0.114	-0.287	-0.253	0.155	0.043	0.176	0.155	-0.026	0.029	-0.081
J2	0.114		-0.195	-0.210	0.754	0.223	0.344	0.307	-0.221	-0.050	-0.253
J4	-0.287	-0.195		0.385	-0.330	-0.169	-0.294	-0.323	0.117	0.026	0.205
beta	-0.253	-0.210	0.385		-0.501	0.275	-0.603	-0.097	-0.180	-0.421	-0.070
alpha	0.155	0.754	-0.330	-0.501		-0.009	0.677	0.177	-0.005	0.243	-0.071
d2	0.043	0.223	-0.169	0.275	-0.009		-0.545	0.929	-0.942	-0.956	-0.959
d4	0.176	0.344	-0.294	-0.603	0.677	-0.545		-0.337	0.642	0.767	0.534
R2	0.155	0.307	-0.323	-0.097	0.177	0.929	-0.337		-0.906	-0.830	-0.966
R4	-0.026	-0.221	0.117	-0.180	-0.005	-0.942	0.642	-0.906		0.945	0.984
d42	0.029	-0.050	0.026	-0.421	0.243	-0.956	0.767	-0.830	0.945		0.921
R42	-0.081	-0.253	0.205	-0.070	-0.071	-0.959	0.534	-0.966	0.984	0.921	

**Figure S1.** Brief view to the pair correlations for 41+6 hits.