

New complex phosphates $\text{Cs}_3\text{M}^{\text{II}}\text{Bi}(\text{P}_2\text{O}_7)_2$ ($\text{M}^{\text{II}} - \text{Ca, Sr, Pb}$): synthesis, characterization, crystal and electronic structure

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SUPPORTING INFORMATION

Table 1S.

The atomic coordinates and their equivalent isotropic thermal parameters of CsCaBiP (I), CsSrBiP (II) and CsPbBiP(III).

Atom		x	y	z	$U_{\text{iso}}/U_{\text{eq}}$
Bi1	I	0.730090(19)	0.146186(18)	0.249723(11)	0.01228(5)
	II	0.73077(2)	0.14783(3)	0.254473(13)	0.01103(5)
	III	0.732104(17)	0.143512(18)	0.257008 (9)	0.01048(4)
Ca1	I	0.06336(10)	0.31751(9)	0.13101(5)	0.00563(14)
Sr1	II	0.06838(6)	0.31685(6)	0.13283(3)	0.00851(11)
Pb1	III	0.063661(19)	0.31885(2)	0.129076 (11)	0.01434(4)
Cs1	I	0.11567(4)	0.48665(3)	0.498757(19)	0.01702(7)
	II	0.11406(5)	0.49088(5)	0.49919(2)	0.01854(10)
	III	0.10796(4)	0.49466(4)	0.498867 (18)	0.01948(7)
Cs2	I	0.27066(4)	0.14483(4)	0.33569(2)	0.02659(8)
	II	0.26460(5)	0.14586(6)	0.33554(3)	0.02746(11)
	III	0.26279(4)	0.15021(4)	0.33278 (2)	0.02978(8)
Cs3	I	0.11909(5)	0.00324(4)	0.56563(3)	0.02840(9)
	II	0.10135(6)	0.00063(6)	0.57290(3)	0.03275(13)
	III	0.09721(4)	0.00268(4)	0.58219 (2)	0.02932(9)
P1	I	0.98245(15)	0.42848(14)	0.29832(7)	0.0111(2)
	II	0.97857(19)	0.42420(18)	0.30136(9)	0.0109(3)
	III	0.97027(14)	0.41774(15)	0.30476 (7)	0.0140(2)
P2	I	0.88579(15)	0.20625(13)	0.41201(7)	0.0121(2)
	II	0.46603(17)	0.3570(2)	0.18494(9)	0.0119(3)
	III	0.87971(14)	0.20448(14)	0.41927 (7)	0.0140(2)
P3	I	0.45687(13)	0.35239(15)	0.18091(7)	0.0109(2)
	II	0.46603(17)	0.3570(2)	0.18494(9)	0.0119(3)
	III	0.47486(12)	0.35913(15)	0.18855 (7)	0.0128(2)
P4	I	0.68042(15)	0.25624(15)	0.07269(8)	0.0126(2)
	II	0.68618(19)	0.2688(2)	0.07489(10)	0.0142(4)
	III	0.69144(13)	0.27470(15)	0.07602 (7)	0.0132(2)
O1	I	0.8729(6)	0.3723(5)	0.2433(3)	0.0275(10)
	II	0.8752(5)	0.3613(5)	0.2444(2)	0.0167(9)
	III	0.8717(4)	0.3510(5)	0.2455 (2)	0.0243(9)
O2	I	1.1294(5)	0.4159(5)	0.2606(3)	0.0226(9)
	II	1.1288(5)	0.4176(5)	0.2692(3)	0.0178(10)
	III	1.1200(4)	0.4217(5)	0.2733 (2)	0.0243(9)
O3	I	0.9548(5)	0.5738(5)	0.3306(3)	0.0236(9)
	II	0.9385(7)	0.5661(6)	0.3309(3)	0.0266(12)
	III	0.9170(6)	0.5501(5)	0.3358 (3)	0.0411(12)
O4	I	0.7382(5)	0.2216(5)	0.3733(2)	0.0238(9)
	II	0.7313(6)	0.2307(6)	0.3781(3)	0.0236(11)
	III	0.7332(4)	0.2187(4)	0.3825 (2)	0.0219(8)

O5	I	0.9520(6)	0.0634(5)	0.3963(3)	0.0315(11)
	II	0.9362(7)	0.0708(6)	0.3952(4)	0.0429(18)
	III	0.9403(6)	0.0662(5)	0.4003 (4)	0.0577(18)
O6	I	0.8813(6)	0.2505(5)	0.4932(3)	0.0256(9)
	II	0.8784(7)	0.2477(7)	0.4969(3)	0.0377(16)
	III	0.8829(6)	0.2433(6)	0.5009 (2)	0.0386(12)
O7	I	0.9921(5)	0.3187(4)	0.3688(2)	0.0170(8)
	II	0.9859(5)	0.3218(5)	0.3736(3)	0.0185(11)
	III	0.9837(4)	0.3108(5)	0.3752 (2)	0.0266(9)
O8	I	0.5296(5)	0.2739(5)	0.2460(3)	0.0249(9)
	II	0.5387(5)	0.2804(6)	0.2492(3)	0.0241(11)
	III	0.5464(4)	0.2797(5)	0.2520 (2)	0.0265(9)
O9	I	0.4353(5)	0.5064(4)	0.2043(3)	0.0262(10)
	II	0.4432(7)	0.5067(6)	0.2098 (4)	0.0352 (15)
	III	0.4495(5)	0.5050(5)	0.2159 (3)	0.0355(11)
O10	I	0.3262(5)	0.2861(5)	0.1490(3)	0.0278(10)
	II	0.3374(6)	0.2900(7)	0.1527 (3)	0.0304 (14)
	III	0.3481(4)	0.2925(6)	0.1538 (3)	0.0385(13)
O11	I	0.6235(5)	0.2412(5)	-0.0066(3)	0.0242(9)
	II	0.6207(6)	0.2422(6)	-0.0009 (3)	0.0284 (13)
	III	0.6161(5)	0.2477(6)	0.0024 (2)	0.0323(10)
O12	I	0.8286(4)	0.3182(5)	0.0788(3)	0.0250(9)
	II	0.8282(5)	0.3378(7)	0.0737 (3)	0.0302 (14)
	III	0.8308(4)	0.3464(6)	0.0680 (2)	0.0303(10)
O13	I	0.6637(5)	0.1199(4)	0.1188(2)	0.0210(8)
	II	0.6829(6)	0.1377(6)	0.1238 (3)	0.0276 (12)
	III	0.6999(5)	0.1462(4)	0.1254 (2)	0.0276(9)
O14	I	0.5767(4)	0.3713(4)	0.1157(2)	0.0177(8)
	II	0.5828(5)	0.3789(5)	0.1197 (3)	0.0169 (10)
	III	0.5928(4)	0.3823(4)	0.1235 (2)	0.0177(7)

Table 2S.

The bond lengths (Å) in the coordination polyhedra of PO₄ and CsO_x for CsCaBiP (I), CsSrBiP (II) and CsPbBiP(III).

	I	II	III		I	II	III
PO₄tetrahedra				Cs(1)–O(12) ⁱⁱⁱ	3.451(5)	3.620(7)	3.662(5)
P(1)–O(1)	1.502(5)	1.524(5)	1.537(4)	Cs(1)–O(9) ⁱⁱ	3.653(5)	3.756(7)	3.843(6)
P(1)–O(3)	1.505(4)	1.510(5)	1.485(5)	Cs(1)–O(5) ^{iv}	3.660(6)	3.605(7)	3.645(6)
P(1)–O(2)	1.522(4)	1.523(5)	1.515(4)	Cs(2)O_x polyhedra			
P(1)–O(7)	1.619(4)	1.614(5)	1.620(4)	Cs(2)–O(14) ^v	3.065(4)	3.047(5)	3.038(4)
P(2)–O(6)	1.490(5)	1.482(6)	1.481(5)	Cs(2)–O(9) ^v	3.108(5)	3.158(6)	3.174(5)
P(2)–O(5)	1.506(5)	1.499(6)	1.499(5)	Cs(2)–O(7) ⁱ	3.118(4)	3.191(5)	3.148(4)
P(2)–O(4)	1.537(5)	1.544(6)	1.530(4)	Cs(2)–O(8)	3.123(5)	3.262(5)	3.276(4)
P(2)–O(7)	1.637(4)	1.641(5)	1.621(4)	Cs(2)–O(2) ⁱ	3.162(4)	3.138(5)	3.142(4)
P(3)–O(10)	1.476(5)	1.483(5)	1.489(4)	Cs(2)–O(1) ^v	3.212(5)	3.350(5)	3.458(4)
P(3)–O(9)	1.523(4)	1.522(6)	1.517(5)	Cs(2)–O(6) ^{iv}	3.335(5)	3.309(6)	3.294(5)
P(3)–O(8)	1.523(5)	1.515(5)	1.512(4)	Cs(2)–O(5) ⁱ	3.239(6)	3.340(7)	3.362(6)
P(3)–O(14)	1.609(4)	1.605(5)	1.608(4)	Cs(2)–O(12) ^v	3.550(5)	3.482(6)	3.541(5)
P(4)–O(12)	1.499(5)	1.491(6)	1.494(4)	Cs(2)–O(10)	3.585(6)	3.579(6)	3.522(5)
P(4)–O(11)	1.500(4)	1.495(5)	1.497(4)	Cs(2)–O(3) ^v	3.662(5)	3.587(6)	3.543(5)
P(4)–O(13)	1.528(4)	1.530(6)	1.522(4)	Cs(3)O_x polyhedra			
P(4)–O(14)	1.636(4)	1.641(5)	1.629(4)	Cs(3)–O(4) ^{iv}	3.019(5)	2.989(6)	3.060(4)
Cs(1)O_x polyhedra				Cs(3)–O(13) ^{vi}	3.020(5)	3.118(6)	3.242(5)
Cs(1)–O(7) ⁱ	3.011(4)	3.003(5)	3.044(4)	Cs(3)–O(12) ^v	3.123(5)	3.097(6)	3.114(4)
Cs(1)–O(14) ⁱⁱ	3.039(4)	3.086(5)	3.128(4)	Cs(3)–O(10) ^{vi}	3.140(5)	3.185(6)	3.176(6)
Cs(1)–O(6) ⁱ	3.115(5)	3.223(6)	3.237(5)	Cs(3)–O(5) ⁱ	3.410(6)	3.564(8)	3.569(7)
Cs(1)–O(13) ⁱⁱⁱ	3.173(4)	3.218(5)	3.193(4)	Cs(3)–O(6) ⁱ	3.456(5)	3.443(7)	3.404(6)
Cs(1)–O(4) ^{iv}	3.198(5)	3.234(5)	3.166(4)	Cs(3)–O(11) ^{vi}	3.465(5)	3.394(6)	3.453(5)
Cs(1)–O(6) ^{iv}	3.333(5)	3.385(6)	3.474(5)	Cs(3)–O(6) ^{iv}	3.521(6)	3.764(7)	3.934(6)
Cs(1)–O(11) ⁱⁱ	3.395(5)	3.387(6)	3.277(5)	Cs(3)–O(11) ^v	3.592(5)	3.825(7)	3.956(6)
Cs(1)–O(11) ⁱⁱⁱ	3.413(5)	3.474(6)	3.581(5)	Cs(3)–O(3) ^{iv}	3.687(5)	3.652(6)	3.378(6)
Cs(1)–O(3) ⁱ	3.418(5)	3.475(6)	3.420(5)	Cs(3)–O(8) ^{iv}	4.015(5)	3.828(7)	3.627(4)
Cs(1)–O(10) ⁱⁱ	3.448(6)	3.465(6)	3.440(6)	Cs(3)–O(9) ^{iv}	-	4.115(8)	3.804(5)

Symmetrycodes: (i) $-1+x, y, z$; (ii) $0.5-x, 1-y, z+0.5$; (iii) $1-x, y+0.5, 0.5-z$; (iv) $-0.5+x, 0.5-y, 1-z$; (v) $1-x, -0.5+y, 0.5-z$; (vi) $0.5-x, -y, z+0.5$; (vii) $2-x, y-0.5, 0.5-z$; (viii) $x+1, y, z$; (ix) $x+0.5, 0.5-y, 1-z$; (x) $0.5-x, 0.5-y, -z$; (xi) $-x, y-0.5, 0.5-z$; (xii) $-x+0.5, 1-y, z-0.5$; (xiii) $-x, y+0.5, 0.5-z$; (xiv) $0.5-x, -y, z-0.5$; (xv) $2-x, y+0.5, 0.5-z$; (xvi) $x+0.5, 0.5-y, -z$.

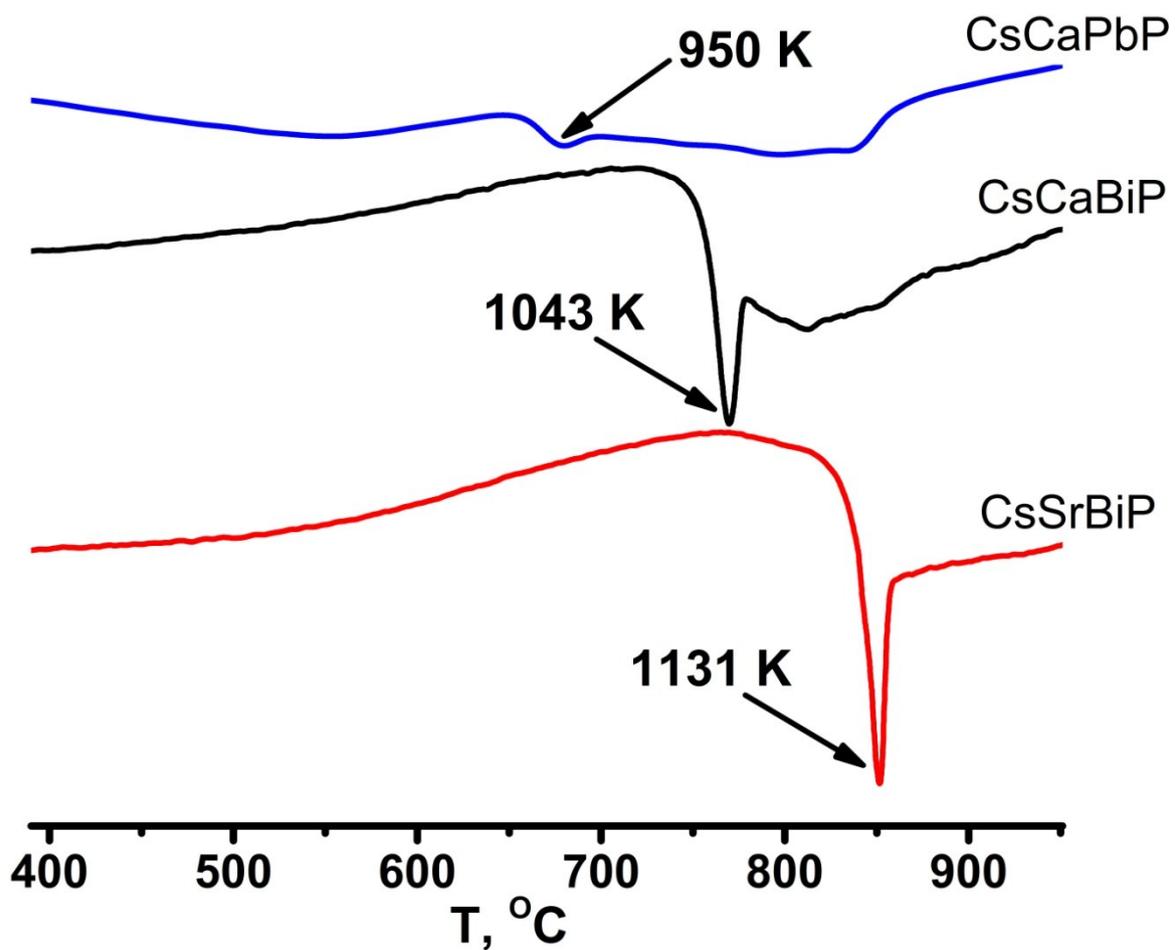


Fig 1S. DTA-curves at heating mode for complex phosphates $\text{Cs}_3\text{M}^{\text{II}}\text{Bi}(\text{P}_2\text{O}_7)_2$ (melting points are indicated by arrows).

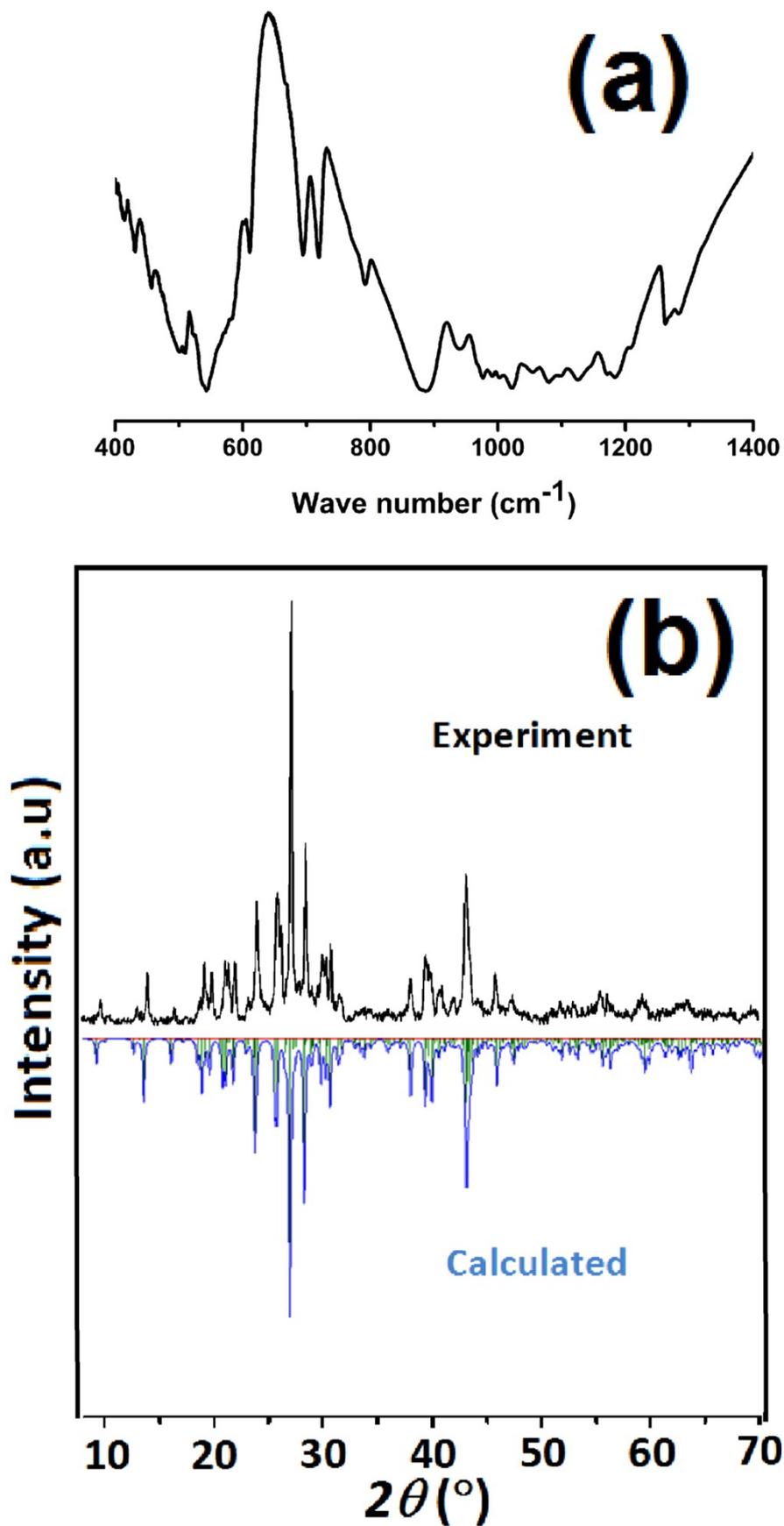


Fig 2S. FTIR-spectra (a) and XRD powder data (b) of glass-ceramic $\text{Cs}_3\text{CaBi}(\text{P}_2\text{O}_7)_2$.

Details of calculations of Voronoi-Dirichlet polyhedron (VDP)

CN – Coordination number

Rsd– Radius of spherical domain

D(CP) – The shift of an atom from the centroid of its coordination polyhedron and coordinates of the centroid

D(VDP)– The shift of an atom from the centroid of its Voronoi-Dirichlet polyhedron and coordinates of the centroid

Atom, Top – The values of division coefficients used for bonds between central atom and atoms, forming Voronoi-Dirichlet polyhedron, if they differ from 0.5

CN(m:l:n) – Total coordination number of the atom, written as $n:m:l$, where n , m and l are the numbers of 'direct', 'half-direct' and 'indirect' neighbours

NV – The number of vertices of Voronoi-Dirichlet polyhedron

V – Volume of Voronoi-Dirichlet polyhedron/coordination polyhedron

S – Surface area of Voronoi-Dirichlet polyhedron

Cpac – Packing coefficient

Ccov – Covering coefficient

G3 – Dimensionless second moment of inertia of Voronoi-Dirichlet polyhedron

Face distribution – Combinatorial properties of VDP faces written as the number of vertices (edges) of a face/the number of such faces

Vertex distribution – Combinatorial properties of VDP vertices written as the number of edges(faces), that meet in a vertex/the number of such vertices

Dist – The distance between central atom and X_i atom

S_{Seg} – The area of the face

V_{Seg} – The volume of a pyramid with the face in a bottom and the central atom in the top

S_{Ang} – The solid angle of the face

NV – The number of vertices (edges) of the face

Phi – The angle (X_i –central atom–VDP centroid)

Table 3S.

Calculations VDP for atoms Bi and Cs in $\text{Cs}_3\text{CaBi}(\text{P}_2\text{O}_7)_2$.

Central atom: Bi1 0.230 0.354 0.750

Rsd: 1.483; **D(CP):** 0.655 (0.2961 0.3320 0.7562); **D(VDP):** 0.225 (0.2534 0.3560 0.7537);

Atom: 2.180<r<3.601, <r> = 2.927; **Top:** 1.675<R<2.224, <R> = 1.930; **CN** = 8:0:5;

NV =22; **V** = 13.668/44.203; **S** = 32.856; **Cpac** = 0.397; **Ccov** = 3.371; **G3** = 0.085805893;

Face distribution: {3/1 4/4 5/3 6/3 7/2}; **Vertex distribution:** {3/22}

N	Atom	x	y	z	Dist. Å	SSeg.	VSeg.	SAng.	NV	Phi
1	O9	0.065	0.494	0.704	2.180	14.48	12.65	16.33	5	136.05
2	O8	0.030	0.226	0.754	2.218	12.69	11.28	15.00	5	147.86
3	O4	0.238	0.278	0.627	2.291	13.43	12.33	14.95	6	104.57
4	O13	0.164	0.380	0.881	2.400	15.85	15.25	15.62	7	88.82
5	O1	0.373	0.128	0.757	2.513	15.57	15.67	14.53	7	63.87
6	O2	0.371	0.584	0.761	2.540	15.09	15.36	14.20	4	53.82
7	O3	0.545	0.426	0.831	3.322	6.31	8.40	4.69	6	12.04
8	O5	0.452	0.437	0.604	3.395	3.87	5.27	2.77	6	66.46
9	O14	0.077	0.129	0.884	3.480	0.47	0.65	0.35	4	105.47
10	O12	0.329	0.182	0.921	3.540	1.24	1.75	0.91	4	64.29
11	O7	0.492	0.181	0.631	3.601	0.63	0.91	0.39	5	63.22

Central atom:Cs1 0.116 0.487 0.499

Rsd: 1.842; **D(CP):** 0.220 (0.1206 0.5070 0.5043); **D(VDP):** 0.028 (0.1177 0.4844 0.4987);

Atom: 3.011<r< 4.750, <r> = 3.591; **Top:** 1.771<R<2.446, <R> = 2.159; **CN** = 15:0:5;

NV = 36; **V** = 26.174/102.730; **S** = 48.047; **Cpac** = 0.546; **Ccov** = 2.343; **G3** = 0.080441684 ;

Face distribution: {3/7 5/1 6/7 7/2 8/1 9/2}; **Vertex distribution:** {3/36}

N	Atom	x	y	z	Dist. Å	SSeg.	VSeg.	SAng.	NV	Phi
1	O7	-0.008	0.319	0.369	3.011	11.15	10.27	11.45	5	79.89
2	O14	-0.077	0.629	0.616	3.038	9.88	9.18	10.71	6	139.32
3	O6	-0.119	0.250	0.493	3.115	12.35	11.77	11.68	9	86.48
4	O13	0.336	0.620	0.381	3.173	9.97	9.67	9.91	8	79.81
5	O4	0.238	0.278	0.627	3.199	8.77	8.58	9.09	6	49.20
6	O6	0.381	0.250	0.507	3.333	9.55	9.74	8.79	7	7.93
7	O11	-0.123	0.759	0.493	3.395	7.01	7.28	6.80	6	175.03
8	O11	0.377	0.741	0.507	3.413	5.32	5.56	5.49	6	92.64
9	O3	-0.045	0.574	0.331	3.418	6.28	6.57	6.27	6	115.01
10	O10	0.174	0.714	0.649	3.448	5.79	6.11	5.81	9	113.40
11	O12	0.171	0.818	0.421	3.451	4.64	4.90	4.80	6	123.17
12	O9	0.065	0.494	0.704	3.652	2.95	3.30	2.81	6	98.94
13	O5	0.452	0.437	0.604	3.660	3.76	4.21	3.53	7	50.22

Central atom:Cs2 0.771 0.355 0.664

Rsd: 1.879; **D(CP):** 0.281 (0.7888 0.3315 0.6626); **D(VDP):** 0.104 (0.7745 0.3467 0.6611);
Atom: 3.065<r<5.063, <r> = 3.838; **Top:** 1.946<R<2.579, <R> = 2.302; **CN** = 13:0:7;
NV = 36; **V** = 27.770/120.452; **S** = 50.527; **Cpac** = 0.543; **Ccov** = 2.587; **G3** = 0.082202137;
Face distribution: {3/8 5/2 6/5 7/1 8/2 9/1 12/1}; **Vertex distribution:** {3/36}

N	Atom	x	y	z	Dist. Å	SSEG.	VSeg.	SAng.	NV	Phi
1	O14	0.923	0.629	0.616	3.065	8.83	8.20	9.99	6	109.86
2	O9	1.065	0.494	0.704	3.108	9.25	8.72	9.63	9	98.33
3	O7	0.492	0.181	0.631	3.118	9.16	8.66	9.72	6	77.19
4	O8	1.030	0.226	0.754	3.124	11.11	10.53	11.16	8	73.06
5	O2	0.629	0.084	0.739	3.163	9.36	8.98	9.90	6	75.19
6	O1	0.627	0.628	0.743	3.212	9.48	9.23	9.96	8	172.49
7	O5	0.452	0.437	0.604	3.239	8.25	8.10	8.72	6	108.54
8	O6	0.881	0.250	0.493	3.334	16.09	16.27	13.92	12	34.93
9	O12	0.671	0.682	0.579	3.550	4.25	4.57	4.30	5	121.93
10	O10	0.826	0.214	0.851	3.586	5.13	5.58	4.88	7	99.09
11	O3	0.545	0.426	0.831	3.663	5.20	5.77	5.02	5	140.07
12	O8	0.970	0.726	0.746	4.212	0.01	0.01	0.01	3	132.28
13	O4	1.238	0.278	0.627	4.452	0.51	0.69	0.38	3	57.38
14	O13	0.836	-0.120	0.619	4.591	2.19	3.05	1.53	6	27.00

Central atom: Cs3 0.619 0.497 0.434

Rsd: 1.913; **D(CP):** 0.454 (0.6421 0.4924 0.4118); **D(VDP):** 0.111 (0.6239 0.4881 0.4309);
Atom: 3.019<r<5.063, <r> = 3.891; **Top:** 1.950<R<2.579, <R> = 2.295; **CN** = 13:0:9;
NV = 40; **V** = 29.346/130.936; **S** = 51.967; **Cpac** = 0.491; **Ccov** = 2.448; **G3** = 0.081912637 ;
Face distribution: {3/8 4/1 5/1 6/6 7/3 9/1 10/1 11/1}; **Vertex distribution:** {3/40}

N	Atom	x	y	z	Dist. Å	SSEG.	VSeg.	SAng.	NV	Phi
1	O4	0.738	0.222	0.373	3.019	12.15	10.83	13.28	7	12.96
2	O13	0.336	0.620	0.381	3.020	12.57	11.20	13.33	9	117.81
3	O12	0.671	0.682	0.579	3.123	9.90	9.13	10.95	7	142.22
4	O10	0.674	0.786	0.351	3.140	11.26	10.44	11.90	10	108.74
5	O5	0.452	0.437	0.604	3.410	7.34	7.39	7.59	6	122.37
6	O6	0.381	0.250	0.507	3.456	9.80	10.00	9.25	6	87.78
7	O11	0.377	0.741	0.507	3.465	4.46	4.56	4.97	5	162.15
8	O6	0.881	0.250	0.493	3.521	9.03	9.39	8.06	11	52.71
9	O11	0.877	0.759	0.493	3.592	5.30	5.61	5.18	6	113.26
10	O3	0.955	0.574	0.331	3.687	6.73	7.32	6.41	7	62.27
11	O8	0.530	0.274	0.246	4.015	5.53	6.56	4.48	6	41.41
12	O7	0.992	0.319	0.369	4.019	0.79	0.94	0.74	4	35.72
13	O1	0.873	0.372	0.243	4.274	1.64	2.07	1.22	6	31.56
14	O8	0.470	0.774	0.254	4.340	0.05	0.06	0.04	3	100.10
15	O9	0.435	0.506	0.204	4.399	2.03	2.64	1.53	6	70.89
16	O14	0.923	0.629	0.616	4.442	0.25	0.33	0.18	3	109.82

Table 4S.

Calculations VDP for atoms Bi and Cs in $\text{Cs}_3\text{SrBi}(\text{P}_2\text{O}_7)_2$.

Central atom: Bi1 0.231 0.352 0.746 Rsd:1.487

D(CP): 0.529 (0.2821 0.3661 0.7359); **D(VDP):** 0.232 (0.2544 0.3589 0.7464);

Atom: 2.213 < r < 3.869 <r>=2.933; **Top:** 1.719 < R < 2.257 <R>=1.958; **CN** = 8:0:4;

NV = 20; **V** = 13.771/39.842; **S** = 33.242; **Cpac** = 0.412; **Ccov** = 3.495; **G3** = 0.085976891;

Face distribution: {3/3 4/2 5/2 6/3 7/1 8/1}; **Vertex distribution:** {3/20}

N	Atom	x	y	z	Dist. Å	SSEG.	VSEG.	SANG.	NV	Phi
1	O8	0.039	0.220	0.751	2.213	12.38	11.02	14.98	5	160.08
2	O9	0.057	0.493	0.710	2.218	15.50	13.83	16.75	6	123.57
3	O4	0.231	0.269	0.622	2.324	12.88	12.04	14.50	6	98.83
4	O13	0.183	0.362	0.876	2.353	16.27	15.40	16.28	6	96.29
5	O1	0.375	0.139	0.756	2.470	16.38	16.28	15.33	7	72.65
6	O2	0.371	0.582	0.769	2.613	14.99	15.76	13.77	5	43.02
7	O5	0.436	0.429	0.605	3.233	6.71	8.72	4.99	8	54.01
8	O14	0.083	0.121	0.880	3.542	0.09	0.13	0.06	3	120.62
9	O3	0.562	0.434	0.831	3.543	4.37	6.23	3.04	4	21.64
10	O7	0.486	0.178	0.626	3.603	0.21	0.31	0.15	4	61.93
11	O10	0.163	0.710	0.653	3.869	0.00	0.00	0.00	3	86.35

Central atom: Cs1 0.114 0.491 0.499

Rsd: 1.869; **D(CP):** 0.216 (0.1116 0.5091 0.4922); **D(VDP):** 0.027 (0.1167 0.4900 0.4988);

Atom: 3.003<r<4.984, <r> = 3.705; **Top:** 1.791<R<2.523, <R> = 2.197; **CN** = 16:0:7;

NV = 42; **V** = 27.358/117.390; **S** = 49.459; **Cpac** = 0.518; **Ccov** = 2.459; **G3** = 0.080492504;

Face distribution: {3/8 4/1 5/1 6/5 7/4 8/1 9/3}; **Vertex distribution:** {3/42}

N	Atom	x	y	z	Dist. Å	SSEG.	VSEG.	SANG.	NV	Phi
1	O7	-0.014	0.322	0.374	3.003	11.32	10.24	11.94	6	90.19
2	O14	-0.083	0.621	0.620	3.086	9.68	9.00	10.50	6	148.88
3	O13	0.317	0.638	0.376	3.218	10.20	9.89	10.15	8	54.11
4	O6	-0.122	0.248	0.497	3.223	11.10	10.78	10.48	9	113.65
5	O4	0.231	0.269	0.622	3.234	8.64	8.42	9.03	6	70.37
6	O6	0.378	0.252	0.503	3.384	9.41	9.59	8.61	7	29.08
7	O11	-0.121	0.758	0.499	3.387	7.74	7.89	7.56	7	145.92
8	O10	0.163	0.710	0.653	3.465	6.25	6.52	6.28	9	105.96
9	O11	0.379	0.742	0.501	3.474	5.62	5.88	5.71	6	63.96
10	O3	-0.062	0.566	0.331	3.475	6.24	6.54	6.15	9	105.69
11	O5	0.436	0.429	0.605	3.605	4.62	5.02	4.46	7	47.13
12	O12	0.172	0.838	0.426	3.621	3.91	4.27	3.88	7	92.99
13	O9	0.057	0.493	0.710	3.757	2.61	2.95	2.44	6	113.33
14	O2	0.129	0.418	0.269	4.124	0.56	0.69	0.43	5	69.80

Central atom: Cs2 0.765 0.354 0.664

Rsd: 1.895; **D(CP):** 0.284 (0.7835 0.3315 0.6671); **D(VDP):** 0.088 (0.7673 0.3466 0.6620);**Atom:** 3.048<r<5.008, <r> = 3.885; **Top:** 1.961<R<2.584, <R> = 2.333; **CN** = 11:0:9;**NV** = 36; **V** = 28.497/128.215; **S** = 51.515; **Cpac** = 0.520; **Ccov** = 2.537; **G3** = 0.081924722;**Face distribution:** {3/6 4/2 5/3 6/4 7/2 8/1 9/1 12/1}; **Vertex distribution:** {3/36}

N	Atom	x	y	z	Dist. Å	SSeg.	VSeg.	SAng.	NV	Phi
1	O14	0.917	0.621	0.620	3.048	8.83	8.11	10.23	6	115.10
2	O2	0.629	0.082	0.731	3.138	10.57	9.99	10.97	7	67.76
3	O9	1.057	0.493	0.710	3.159	9.14	8.70	9.47	9	102.70
4	O7	0.486	0.178	0.626	3.191	8.64	8.31	9.13	5	72.55
5	O8	1.039	0.220	0.751	3.261	10.09	9.92	9.93	8	71.17
6	O6	0.878	0.248	0.497	3.308	16.76	16.70	14.56	12	37.70
7	O5	0.436	0.429	0.605	3.340	8.07	8.12	8.28	6	106.82
8	O1	0.625	0.639	0.744	3.350	8.01	8.08	8.42	7	172.78
9	O12	0.672	0.662	0.574	3.482	5.49	5.76	5.58	5	122.76
10	O10	0.837	0.210	0.847	3.580	5.37	5.79	5.32	6	94.29
11	O3	0.562	0.434	0.831	3.587	6.84	7.39	6.62	6	137.43
12	O8	0.961	0.720	0.749	4.247	0.01	0.01	0.01	3	136.54
13	O4	1.231	0.269	0.622	4.524	0.42	0.57	0.31	3	59.19
14	O13	0.817	-0.138	0.624	4.815	0.96	1.39	0.62	5	24.74

Central atom: Cs3 0.601 0.499 0.427 Rsd:1.930

D(CP): 0.487 (0.6327 0.4933 0.4054); **D(VDP):** 0.095 (0.6053 0.4914 0.4246);**Atom:** 2.989<r<5.008, <r> = 3.900; **Top:** 2.022<R<2.584, <R> = 2.324; **CN** = 12:0:9;**NV** = 38; **V** = 30.104/133.938; **S** = 52.948; **Cpac** = 0.464; **Ccov** = 2.402; **G3** = 0.081806697;**Face distribution:** {3/6 4/2 5/3 6/5 7/1 8/1 9/2 10/1}; **Vertex distribution:** {3/38}

N	Atom	x	y	z	Dist. Å	SSeg.	VSeg.	SAng.	NV	Phi
1	O4	0.731	0.231	0.378	2.989	12.35	10.82	13.87	7	10.23
2	O12	0.672	0.662	0.574	3.098	11.25	10.21	12.24	6	134.58
3	O13	0.317	0.638	0.376	3.117	11.68	10.67	12.24	9	123.04
4	O10	0.663	0.790	0.347	3.185	11.09	10.36	11.83	9	115.60
5	O11	0.379	0.742	0.501	3.394	5.48	5.45	6.20	5	164.99
6	O6	0.378	0.252	0.503	3.442	10.69	10.78	10.09	6	82.00
7	O5	0.436	0.429	0.605	3.565	6.30	6.59	6.29	6	114.70
8	O3	0.938	0.566	0.331	3.652	7.88	8.44	7.46	8	65.88
9	O6	0.878	0.248	0.497	3.764	7.12	7.85	5.93	10	50.48
10	O11	0.879	0.758	0.499	3.825	3.82	4.28	3.48	5	113.95
11	O8	0.539	0.280	0.249	3.828	6.44	7.22	5.56	6	41.06
12	O7	0.986	0.322	0.374	4.108	0.56	0.67	0.49	4	38.67
13	O9	0.443	0.507	0.210	4.115	3.67	4.43	3.10	6	74.38
14	O8	0.461	0.780	0.251	4.329	0.03	0.04	0.03	3	107.00
15	O1	0.875	0.361	0.244	4.335	0.93	1.18	0.70	5	35.40

Table 5S.

Calculations VDP for atoms Bi and Cs in $\text{Cs}_3\text{PbBi}(\text{P}_2\text{O}_7)_2$.

Central atom: Bi1 0.232 0.356 0.743

Rsd: 1.486; **D(CP):** 0.570 (0.2882 0.3724 0.7348); **D(VDP):** 0.247 (0.2559 0.3669 0.7421);

Atom: 2.197<r<3.830, <r> = 2.944; **Top:** 1.738<R<2.343, <R> = 1.978; **CN** = 7:0:5;

NV = 20; **V** = 13.732/40.181; **S** = 33.424; **Cpac** = 0.404; **Ccov** = 3.922; **G3** = 0.087098949;

Face distribution: {3/3 4/2 5/2 6/3 7/1 8/1}; **Vertex distribution:** {3/20}

N	Atom	x	y	z	Dist. Å	SSeg.	VSeg.	SAng.	NV	Phi
1	O8	0.046	0.220	0.748	2.197	12.07	10.75	14.97	5	167.19
2	O9	0.051	0.495	0.716	2.229	16.06	14.53	16.99	6	115.84
3	O4	0.233	0.281	0.618	2.318	13.48	12.68	14.94	6	93.79
4	O13	0.200	0.354	0.875	2.327	15.75	14.87	16.23	6	100.70
5	O1	0.372	0.149	0.755	2.417	16.34	16.02	15.58	7	81.61
6	O2	0.380	0.578	0.773	2.623	16.53	17.59	14.53	5	36.00
7	O5	0.440	0.434	0.600	3.275	6.57	8.73	4.74	8	46.57
8	O7	0.484	0.189	0.625	3.544	0.47	0.67	0.32	4	62.87
9	O14	0.093	0.118	0.877	3.549	0.00	0.00	0.00	3	130.33
10	O3	0.583	0.450	0.836	3.796	2.28	3.52	1.42	4	30.27
11	O10	0.152	0.708	0.654	3.830	0.26	0.41	0.15	3	77.69

Central atom: Cs1 0.108 0.495 0.499

Rsd: 1.873; **D(CP):**0.180 (0.1055 0.5121 0.4957); **D(VDP):** 0.041 (0.1121 0.4937 0.4984);

Atom: 3.044<r<5.019, <r> = 3.712; **Top:** 1.804<R<2.538, <R> = 2.196; **CN** = 14:0:9;

NV = 42; **V** = 27.511/115.607; **S** = 49.603; **Cpac** = 0.537; **Ccov** = 2.489; **G3** = 0.080544502;

Face distribution: {3/9 6/6 7/4 8/1 9/3}; **Vertex distribution:** {3/42}

N	Atom	x	y	z	Dist. Å	SSeg.	VSeg.	SAng.	NV	Phi
1	O7	-0.016	0.311	0.375	3.044	10.38	9.49	11.08	6	95.97
2	O14	-0.093	0.618	0.623	3.128	9.22	8.67	9.87	6	142.47
3	O4	0.233	0.281	0.618	3.166	9.59	9.12	10.14	6	67.25
4	O13	0.300	0.646	0.375	3.193	10.71	10.28	10.74	7	55.87
5	O6	-0.117	0.243	0.501	3.237	10.86	10.56	10.29	9	117.13
6	O11	-0.116	0.752	0.502	3.277	8.46	8.33	8.60	7	142.59
7	O3	-0.083	0.550	0.336	3.421	6.85	7.05	6.82	9	112.77
8	O10	0.152	0.708	0.654	3.440	6.90	7.14	6.93	9	99.57
9	O6	0.383	0.257	0.499	3.474	8.58	8.95	7.65	8	30.08
10	O11	0.384	0.748	0.498	3.581	4.99	5.37	4.91	6	57.41
11	O5	0.440	0.434	0.600	3.645	4.51	4.94	4.26	7	39.59
12	O12	0.169	0.846	0.432	3.662	3.51	3.86	3.46	7	90.26
13	O9	0.051	0.495	0.716	3.843	2.04	2.36	1.88	6	108.38
14	O2	0.120	0.422	0.273	4.019	1.19	1.43	0.95	6	75.73

Central atom: Cs2 0.763 0.350 0.667

Rsd: 1.895; **D(CP):** 0.314 (0.7834 0.3245 0.6673); **D(VDP):** 0.074 (0.7644 0.3435 0.6650);**Atom:** 3.038<r<4.892, <r> = 3.902; **Top:** 1.962<R<2.604, <R> = 2.346; **CN** = 11:0:10;**NV** = 38; **V** = 28.504/120.469; **S** = 51.653; **Cpac** = 0.515; **Ccov** = 2.594; **G3** = 0.081728861;**Face distribution:** {3/9 5/4 6/2 7/1 8/1 9/3 13/1}; **Vertex distribution:** {3/38}

N	Atom	x	y	z	Dist. Å	SSEG.	VSEG.	SANG.	NV	Phi
1	O14	0.907	0.618	0.623	3.038	9.07	8.32	10.52	5	119.33
2	O2	0.620	0.078	0.727	3.142	11.09	10.52	11.21	9	63.99
3	O7	0.484	0.189	0.625	3.148	9.07	8.62	9.67	5	68.86
4	O9	1.051	0.495	0.716	3.174	8.85	8.49	9.24	9	109.33
5	O8	1.046	0.220	0.748	3.276	9.78	9.67	9.65	9	74.56
6	O6	0.883	0.243	0.501	3.295	16.86	16.78	14.70	13	37.91
7	O5	0.440	0.434	0.600	3.362	8.02	8.14	8.09	7	102.02
8	O1	0.628	0.649	0.745	3.458	6.78	7.08	7.10	6	168.60
9	O10	0.848	0.208	0.846	3.522	5.76	6.13	5.94	6	94.89
10	O12	0.669	0.654	0.568	3.540	5.20	5.56	5.16	5	119.49
11	O3	0.583	0.450	0.836	3.543	8.11	8.67	7.76	8	139.28
12	O9	0.949	-0.005	0.784	4.382	0.02	0.02	0.01	3	60.20
13	O4	1.233	0.281	0.618	4.567	0.26	0.36	0.20	3	65.08
14	O13	0.800	-0.146	0.625	4.892	0.52	0.77	0.32	5	24.23

Central atom: Cs3 0.597 0.497 0.418

Rsd: 1.922; **D(CP):** 0.314 (0.6262 0.4880 0.4106); **D(VDP):** 0.073 (0.5979 0.4899 0.4171);**Atom:** 3.061<r<5.019, <r> = 3.890; **Top:** 2.040<R<2.604, <R> = 2.330; **CN** = 13:0:7;**NV** = 36; **V** = 29.729/127.466; **S** = 52.495; **Cpac** = 0.505; **Ccov** = 2.487; **G3** = 0.081318453;**Face distribution:** {3/6 4/3 5/1 6/4 7/2 8/2 9/1 10/1}; **Vertex distribution:** {3/36}

N	Atom	x	y	z	Dist. Å	SSEG.	VSEG.	SANG.	NV	Phi
1	O4	0.733	0.219	0.382	3.061	11.36	10.24	12.69	7	19.68
2	O12	0.669	0.654	0.568	3.115	11.60	10.63	12.31	6	126.70
3	O10	0.652	0.792	0.346	3.175	10.72	10.02	11.62	8	143.89
4	O13	0.300	0.646	0.375	3.242	10.69	10.20	10.87	8	118.73
5	O3	0.917	0.550	0.336	3.378	10.35	10.29	10.24	9	89.79
6	O6	0.383	0.257	0.499	3.404	11.07	11.09	10.45	6	56.55
7	O11	0.384	0.748	0.498	3.454	5.23	5.32	5.81	4	144.40
8	O5	0.440	0.434	0.600	3.568	6.20	6.51	6.08	6	90.87
9	O8	0.546	0.280	0.252	3.627	7.22	7.71	6.69	6	46.19
10	O9	0.449	0.505	0.216	3.804	5.76	6.45	5.27	7	84.30
11	O6	0.883	0.243	0.501	3.934	5.84	6.76	4.62	10	51.70
12	O11	0.884	0.752	0.502	3.956	2.57	2.99	2.28	5	127.85
13	O7	0.984	0.311	0.375	4.137	0.17	0.21	0.15	4	57.16
14	O1	0.872	0.351	0.245	4.224	0.71	0.88	0.58	4	59.65
15	O8	0.454	0.780	0.248	4.270	0.05	0.06	0.05	3	123.14

Table 6S.

Experimental (obtained by X-ray structural analysis) and calculated (obtained after geometry optimization) lattice parameters of $\text{Cs}_3\text{M}^{\text{II}}\text{Bi}(\text{P}_2\text{O}_7)_2$ crystals.

Lattice constant/ UC volume	$\text{Cs}_3\text{CaBi}(\text{P}_2\text{O}_7)_2$		$\text{Cs}_3\text{SrBi}(\text{P}_2\text{O}_7)_2$		$\text{Cs}_3\text{PbBi}(\text{P}_2\text{O}_7)_2$	
	Exp.	Calc.	Exp.	Calc.	Exp.	Calc.
a, Å	9.28730	9.46027	9.39780	9.60073	9.42430	9.72855
b, Å	9.42920	9.53013	9.62840	9.73125	9.72610	9.77751
c, Å	17.6162	18.0394	17.6552	18.0551	17.5291	18.1647
V, Å ³	1542.68	1626.39	1597.54	1686.83	1606.75	1727.85
ΔV^* , %	5.4		5.6		7.5	

$$*\Delta V = ((V^{\text{calc.}} - V^{\text{exp.}}) / V^{\text{exp.}}) \times 100\%$$

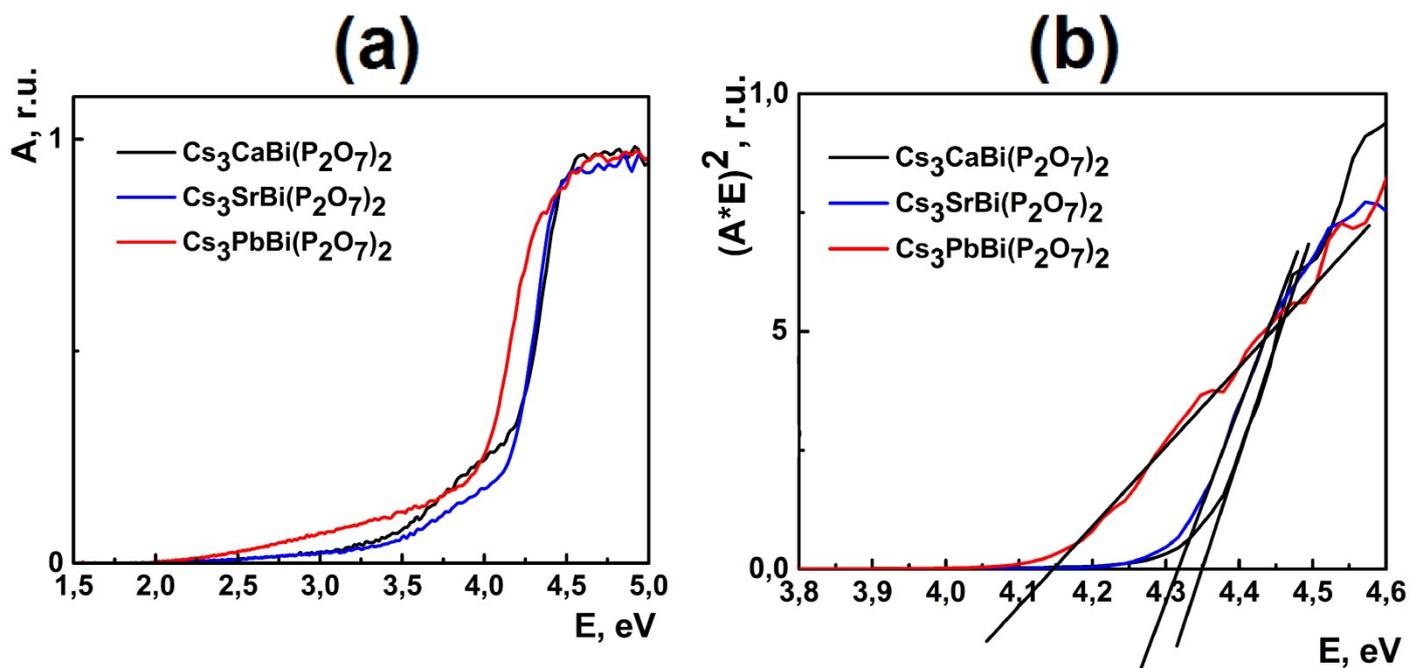


Fig 3S. UV-VIS absorbance spectra of $\text{Cs}_3\text{M}^{\text{II}}\text{Bi}(\text{P}_2\text{O}_7)_2$ crystals (a), and corresponding Tauc plots calculated for direct allowed transitions (b).