# Structural Diversity, Photo-physical and Magnetic Properties of Dimeric to 1D Polymeric Coordination Polymers of Lighter Lanthanide(III) Dinitrobenzoates

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## **ELECTRONIC SUPPLEMENTARY INFORMATION**



**Figure S1**. ORTEP showing asymmetric unit of complex **1** with 30 % probability. **Discussion of H-Bonding in Complex 1** Hydrogen atoms of lattice water O1W are H-bonded to coordinated water O2W with a distance O2W-H22W····O1W = 2.009(3) Å. Proton H12W of lattice water O2W is H-bonded to nitro group oxygen O17 with a distance O12W-H12W····O17 = 2.431(3) Å. These strong H-bonding interactions are further supporting the 1D H-bonded chain along *c* axis (Fig 2a). Additionally, aromatic hydrogen atoms of L1 are also showing H-bonding with oxygens of -NO<sub>2</sub> groups in *bc* plane forming 2D, H-bonded network (Fig 2b).



**Fig S2**. Showing for complex **1** (a) 1D, H-bonded chain along *c* axis, (b) 2D, H bonded network between coordinated water O1W, oxygens of  $-NO_2$  groups and aromatic protons of **L1** in *bc* plane with channels along *a* axis.

This creates 1D channels along *a* axis which are filled by lattice water molecules (O1W) whose H-bonding interactions have been discussed earlier. The presence of a pair of coordinated water molecules and one lattice water molecule give rise to extensive hydrogen bonding and form an interesting 3D structure (Fig S2).



Figure S3. ORTEP showing asymmetric unit of complex 2 with 50 % probability.



**Figure S4**. (a) Trigonal bicapped geometry around Eu(III) metal ion in complex 2. (b) Polyhedral representation of 1D coordination polymer along *a* axis. (c) Ball-n-stick representation showing coordination environment around Eu(III) metal ions forming linear chain. (d) [1 0 0] chains with 2-connected uninodal net. (e) Polyhedral representation of 1D polymeric chain down the *a* axis and 3D structure due to H-bonding interactions in *bc* plane where lattice water molecules are shown in blue coloured balls.



Figure S5. ORTEP showing asymmetric unit of complex 3 with 20 % probability.

**Discussion of H-Bonding in Complex 3:** In case of complex **3** there is strong intramolecular H-bonding interactions due to coordinated water molecules with O1W-H11W $\cdots$ O2W<sup>#1</sup>; O1W-H12W $\cdots$ O2W<sup>#1</sup> = 2.87(3) Å (#1: -x+1,-y+2,-z) and intermolecular interactions between protons of water molecules with oxygens of nitro groups are in the range of 1.85(5) to 2.93(4) Å.



Figure S6. ORTEP showing asymmetric unit of complex 4 with 20 % probability.



Figure S7. ORTEP showing asymmetric unit of complex 5 with 20 % probability.



Figure S8. ORTEP showing asymmetric unit of complex 6 with 20 % probability.



Figure S9. ORTEP showing asymmetric unit of complex 7 with 20 % probability.



Figure S10. Intermolecular H-bonding forms 3D network as shown in *bc* plane for Complex 7

**Discussion of H-Bonding in Complex 7:** The intermolecular H-bonding interactions between hydrogen atoms of aromatic ring, coordinated water molecules with oxygens of nitro and carboxylate groups form 3D network in *bc* plane (Fig S10).



Figure S11. ORTEP showing asymmetric unit of complex 8 with 20 % probability.



**Figure S12** (a) and (b) C-H $\cdots \pi$  and H-bonding interactions between two dimeric units forming 1D chain along *b* axis whereas only weak  $\pi \cdots \pi$  and forming 2D network in *bc* plane.

**Discussion of H-Bonding and C-H···** $\pi$  interactions in Complex 8 : Additionally C-H··· $\pi$  interactions with centroid (C2-C7)···H4 distance 3.701 Å forms 1D chain along *b* axis while weak  $\pi$ ··· $\pi$  interactions (centroid (C16-C21)···centroid (C16-C21) 4.150 Å) form a 2D network in *bc* plane (Fig 5(a-b)). Strong H-bonding interactions between water and nitro groups are in the range of 1.870(6) to 2.950(9) Å. The protons H22W and H31W of coordinated water are H-bonded with oxygens O6 and O5 respectively of nitro group.



Fig S13. ORTEP showing asymmetric unit of complex 9 with 30 % probability.



Fig S14. ORTEP showing asymmetric unit of complex 10 with 30 % probability.

**Discussion of H-Bonding in Complex 10 :** Strong intramolecular H-bonding interactions between water molecules and acetate groups are in the range of 1.86(3) to 2.99(2) Å. The intermolecular H-bonding interactions between protons of coordinated water and acetate group with oxygens of –NO2, –COO and acetate groups are forming corrugated chains as shown in *bc* plane (Fig S15)



Figure S15. Intermolecular H-bonding interactions in bc plane in complex 10.

#### **IR Spectroscopy**

Complexes 1-10 are studied by IR spectroscopy. In complexes 1 and 3 of Nd(III) ions, symmetric and anti-symmetric -OH stretching bands appears as a broad bands in the region of 3575-3589 cm<sup>-1</sup>. The C-H vibrations belonging to the aromatic rings found around 3082-3112 cm<sup>-1</sup> and 1404-1412 cm<sup>-1</sup> for -C=C groups. The characteristic peaks of asymmetric and symmetric stretches of COO<sup>-</sup> in the region of 1630-1643 cm<sup>-1</sup> and 1535-1539 cm<sup>-1</sup>, respectively. The complexes contain an aromatic N-O stretch in the region of 1346-1349 cm<sup>-1</sup> and a weak bands around 583-592 cm<sup>-1</sup> that are assigned to M-O vibrations. In complex 2, the symmetric and anti-symmetric OH stretching band appears as a broad band at 3557 cm<sup>-1</sup>. The characteristic peaks of asymmetric and symmetric stretches of COO<sup>-</sup> at 1622 cm<sup>-1</sup> and 1539 cm<sup>-1</sup>, respectively. The complex contains an aromatic N-O stretch at 1342 cm<sup>-1</sup>, a sp<sup>2</sup>C=C strong band at 1415 cm<sup>-1</sup> and a weak band around 525 cm<sup>-1</sup> that is assigned to M-O vibrations. In spectrum of complex 4, a broad band centred at 3380 cm<sup>-1</sup> indicating the symmetric and antisymmetric OH stretch due to H-bonding interactions. The characteristic peaks of asymmetric and symmetric stretches of COO<sup>-</sup> in the region 1621-1542 cm<sup>-1</sup>. The aromatic N-O stretch is observed at 1351 cm<sup>-1</sup>. The weak band around 578 cm<sup>-1</sup> is assigned to M-O vibrations. In complex 5, OH stretching bands appears as broad bands in the region 3456 cm<sup>-1</sup> and characteristic peaks of asymmetric and symmetric stretches of COO<sup>-</sup> at 1640 cm<sup>-1</sup> and

1536 cm<sup>-1</sup>, respectively. The complex contains an aromatic N-O stretch at 1344 cm<sup>-1</sup> and a weak band around 532 cm<sup>-1</sup> and 723 cm<sup>-1</sup> that are assigned to M-O vibrations. The O-H vibrations band appears as a broad band in the region 3453 cm<sup>-1</sup> and characteristic peaks of asymmetric and symmetric stretches of COO<sup>-</sup> at 1680 cm<sup>-1</sup> and 1541 cm<sup>-1</sup>, respectively in complex 6. In the IR spectrum of complex 7, symmetric and anti-symmetric OH stretching bands appears as a broad band at 3352 cm<sup>-1</sup>. The characteristic peaks of asymmetric and symmetric stretches of COO<sup>-</sup> at 1621 cm<sup>-1</sup> and 1538 cm<sup>-1</sup>, respectively. The complex contains an aromatic N-O stretch at 1343 cm<sup>-1</sup>. The weak band around 529 cm<sup>-1</sup> and 723 cm<sup>-1</sup> are assigned to M-O vibrations. The complex contains an aromatic N-O stretch at 1344 cm<sup>-1</sup> and a weak band around 517 cm<sup>-1</sup> and 724 cm<sup>-1</sup> are assigned to M-O vibrations. Complex 8 shows peaks of asymmetric and symmetric stretches of COO<sup>-</sup> at 1630 cm<sup>-1</sup> and 1531 cm<sup>-1</sup>, respectively, an aromatic N-O stretch at 1352 cm<sup>-1</sup> and a weak band around 567 cm<sup>-1</sup> that is assigned to M-O vibrations. In complex 9, O-H vibrations showing band at around 3337 cm<sup>-1</sup>, characteristic peaks of asymmetric and symmetric stretches of COO<sup>-</sup> around 1654 cm<sup>-1</sup> and 1548 cm<sup>-1</sup>, respectively. The complexes contain an aromatic N-O stretch around 1353 cm<sup>-1</sup> and a weak band around 625 cm<sup>-1</sup> that is assigned to M-O vibrations. The IR spectrum of the complex 10 shows a band for O-H group at 3339 cm<sup>-1</sup>, characteristic peaks of asymmetric and symmetric stretches of COO<sup>-</sup> around 1658 cm<sup>-1</sup> and 1546 cm<sup>-1</sup>, respectively. The complexes contain an aromatic N-O stretch around 1352 cm<sup>-1</sup> and a weak band around 622 cm<sup>-1</sup> that is assigned to M-O vibrations.



Figure S16. IR spectra of complexes 1-10.

Powder X-ray Diffraction studies



Fig S17. Showing generated (blue) and experimental (red) PXRD of complex (1)



Fig S18. Showing generated (blue) and experimental (red) PXRD of complex (2)



Fig S19. Showing generated (blue) and experimental (red) PXRD of complex (3)



Fig S20. Showing generated (blue) and experimental (red) PXRD of complex (4)



Fig S21. Showing generated (blue) and experimental (red) PXRD of complex (5)



Fig S22. Showing generated (blue) and experimental (red) PXRD of complex (6)



Fig S23. Showing generated (blue) and experimental (red) PXRD of complex (7)



Fig S24. Showing generated (blue) and experimental (red) PXRD of complex (8)



Fig S25. Showing generated (blue) and experimental (red) PXRD of complex (9)



Fig S26. Showing generated (blue) and experimental (red) PXRD of complex (10)

#### Thermogravimetric analysis

The thermal stability of complexes 1-10 was examined by TGA (Fig. S13). Thermal decomposition curve of 1 shows that at 92 °C, a loss of 2.07 % (calcd 2.16 %) weight due to one lattice water molecule (wt lost 97.93 %, calcd 97.84 %). After that at 180 °C, a loss of two coordinated water molecules took place (*wt lost* 93.48 %, *calcd* 93.51 %). Two endothermic peaks (-1.62 and -0.98 W/g) are observed at 91 °C and at 179 °C, respectively due to a loss of lattice and coordinated water molecules. The complex is stable up to 420 °C and decomposition takes place in single step above that with one sharp exothermic peak (2.15 W/g) due to decomposition of parent complex with explosion. The TGA curve of 2 showed that at 92 °C, there is a loss of 2.07 % weight due to a loss of one lattice water molecule (wt lost 97.93 %, calcd 97.84 %). Then there is a loss of two coordinated water molecules up to 180 °C (wt lost 93.48 %, calcd 93.51 %). The complex is stable up to 420 °C and complete decomposition of parent complex took place in single step above that temperature with explosion. There are two endothermic peaks of -1.62 and -0.98 W/g are found at 91 °C and 179 °C, respectively due to a loss of lattice and coordinated water molecules. After that at 420 °C, there is a sharp exothermic peak of 2.15 W/g was observed due to complete decomposition with explosion. Complex 3 is stable up to 68 °C, after that it loses 5.44 % weight of two coordinated water molecules (wt lost 95.49 %, calcd 95.67 %) and at 215 °C, it loses 8.9 % weight due to one acetate anion (wt lost 84.34 %, calcd 84.37 %), beyond that it is stable up to 244 °C where it finally decomposes with explosion giving a sharp exothermic peak of 0.343 W/g. Thermal decomposition curve of 4 shows the loss of 4.62 % weight at 64 °C due to the removal of four lattice water molecules (wt lost 95.38 %, calcd 95.61 %). The complex is stable up to 306 °C and decomposition took place in single step above that temperature with 2.82 % weight is lost after complete decomposition of parent complex with explosion. There are endothermic peaks of -0.05, 0.046 and 0.087 W/g observed at 64 °C, 174 °C and 236 °C, respectively. One sharp exothermic peak of 0.36 W/g is observed at 306 °C due to decomposition with explosion in complex 5, there is a loss of four coordinated water molecules at 65 °C (wt lost 4.58 %, calcd 4.45 %). After that, a gradual weight loss is observed up to 298 °C resulting metal oxides as residue and a sharp weight loss with explosion. One endothermic peak of 0.165 W/g is observed at 62 °C due to a loss of lattice water molecules and small endothermic peaks of 0.25 W/g and 0.287 W/g are observed at 164 °C and 226 °C, respectively. A sharp exothermic peak of 0.548 W/g is observed at 307 °C due to an explosion of complete residue. In complex 6, there is a loss of four coordinated water molecules in two steps up to 150 °C (wt lost 4.79 %, calcd 4.47 %). After that, the gradual weight loss is observed up to 400 °C and a sharp weight loss with explosion. Two endothermic peaks of -2.80W/g and -2.76W/g are observed at 115 °C and 191 °C, respectively due to a loss of coordinated water molecules. One exothermic peak of 0.67 W/g is observed at 400 °C due to explosion of complete residue. In complex 7, there is a loss of 4.95 % weight due to coordinated solvent molecule DMF at 104 °C (wt lost 95.05 %, calcd 95.63 %). After that at 210 °C, there is a loss of three coordinated water molecules (wt lost 91.83 % calcd, 92.4 %). Then, a gradual weight loss is observed from 240 °C to 370 °C and then sharp decrease to 0 % weight at 400 °C. There are exothermic peaks of 12.89, 13.13 and 24.4 W/g observed at 120 °C, 240 °C and 400 °C, respectively. In complex 8, there is a loss of six coordinated water molecules at 125 °C (wt lost 6.64 %, calcd 6.31 %). After that, gradual decomposition took place in two steps at 204 °C and 360 °C and then sharp decomposition at 361 °C is observed with 2.38 % weight lost as residue. The weak endothermic peaks of -0.048, 0.048 and 0.087 W/g are observed at 58 °C, 158 °C and 217 °C, respectively due to stepwise removal of coordinated water molecules. The sharp exothermic peak of 0.359 W/g is observed at 289 °C due to complete decomposition with explosion.

In case of complex **9**, there is removal of one coordinated water molecule at 44 °C (*wt lost* 2.70 %, *calcd* 2.68 %). After that, a removal of other two coordinated water molecules is observed at 123 °C (*wt lost* 5.37 %, *calcd* 5.32 %). From 210 °C to 414 °C, the decomposition of organic ligand is observed. After that at 435 °C, 41.7 % weight is lost as metal oxide. The endothermic peak at 228 °C is observed due to a removal of organic ligand and a sharp exothermic peak of 0.174W/g is observed at 341 °C due to complete decomposition of complex. Thermal decomposition curve of **10** shows the loss

of four coordinated water molecules at 108 °C (*wt lost* 6.69 %, *calcd* 6.89 %). After that, four acetate groups are decomposed up to 241 °C (*wt lost* 23.28 %, *calcd* 22.6 %). The complex starts decomposition after that and decomposition took place in single step. A sharp exothermic peak of 0.341 W/g is observed at 246 °C due to complete decomposition.



Figure S27. TGA plots of complexes 1-10.



**Figure S28**. Solid-state excitation (black curve) and emission spectra of **3** at room temperature ( $\lambda_{ex} = 581$  nm, green curve;  $\lambda_{ex} = 476$  nm, yellow curve and  $\lambda_{ex} = 330$  nm, purple curve). The intensities have been normalized on the more intense band at 581 nm and at 1060 nm for the excitation and emission spectra, respectively.



**Figure S29**. Solid-state excitation (black curve) and emission spectra (( $\lambda_{ex} = 583$  nm (green curve),  $\lambda_{ex} = 477$  nm (yellow curve) and  $\lambda_{ex} = 330$  nm (purple curve)) of **1** at room temperature. The intensities have been normalized on the more intense band at 583 nm and at 1060 nm for the excitation and emission spectra, respectively.



**Figure S30**. Solid-state excitation (black curve) and emission spectra (( $\lambda_{ex} = 381$  nm (red curve) and  $\lambda_{ex} = 330$  nm (purple curve)) of **6** at room temperature. The intensity has been normalized on the more intense band for the green curve at 381 nm.

Dynamic magnetic measurements



Figure S31. Temperature dependences of  $\chi_M T$  for compounds 1 (black circles) and 3 (white circles). Inset: Magnetic field dependences of the magnetization for compounds 1 (black circles) and 3 (white circles) at 2 K.



Figure S32. Temperature dependences of  $\chi_M T$  for compound 2 (black circles) with the best fitted curve (red line) with the theoretical expression here below.

Magnetism of Eu<sup>III</sup> complexes:

The spin-orbit coupling operator is:

 $\hat{H} = \lambda \hat{L} \cdot \hat{S}$  where  $\lambda$  is the spin-orbit coupling parameter.

The energies of J = L + S states are:

 $E(J) = \lambda J (J+1)/2$  where the energy of  ${}^{7}F_{0}$  state has been taken as the origin.

The magnetic susceptibility considering that excited states ( ${}^{7}F_{J}$  with J = 1 to 5) can be thermally populated is expressed as

$$\chi_{M} = \frac{\sum_{J=0}^{6} (2J+1)\chi_{M}(J) \exp\left[\frac{-\lambda J(J+1)}{2kT}\right]}{\sum_{J=0}^{6} (2J+1) \exp\left[\frac{-\lambda J(J+1)}{2kT}\right]}$$
  
With  $\chi_{M}(J) = \frac{Ng_{J}^{2}\beta^{2}J(J+1)}{3kT} + \frac{2N\beta^{2}(g_{J}-1)(g_{J}-2)}{3\lambda}$  and

$$g_{J} = \frac{3}{2} + \frac{S(S+1) - L(L+1)}{2J(J+1)}$$

The first term is the Curie law and the second term is the temperature Independent Paramagnetism (TIP) which is due to the field induced mixing with close excited states. In this frame  $\chi_M$  can be rewritten:

$$\chi_{M} = \frac{N\beta^{2}}{3kTx} \frac{\left[24 + \left(\frac{27x}{2} - \frac{3}{2}\right)e^{-x} + \left(\frac{135x}{2} - \frac{5}{2}\right)e^{-3x} + \left(189x - \frac{7}{2}\right)e^{-6x} + \left(405x - \frac{9}{2}\right)e^{-10x}\right] + \left(\frac{1485x}{2} - \frac{11}{2}\right)e^{-15x} + \left(\frac{2457x}{2} - \frac{13}{2}\right)e^{-21x}}{1 + 3e^{-x} + 5e^{-3x} + 7e^{-6x} + 9e^{-10x} + 11e^{-15x} + 13e^{-21x}}\right]$$
with  $x = \frac{\lambda}{2}$ 

with  $x = \frac{1}{kT}$ 



Figure S33. Temperature dependences of  $\chi_M T$  for compound 8 (black circles) with the best fitted curve (red line) with the theoretical expression here above adapted for two Eu<sup>III</sup> per chemical unit.



Figure S34. Temperature dependences of  $\chi_M T$  for compound 4 (black circles) with the best fitted curve with the theoretical expression here below.

Magnetism of Sm<sup>III</sup> complexes:

The thermal behaviour of the molar magnetic susceptibility for Sm<sup>III</sup> complexes can be easily derived with the same methodology than for Eu<sup>III</sup> complexes with

$$E(J) = \frac{\lambda}{2} \left( J \left( J + 1 \right) - \frac{35}{4} \right)$$
 with the multiplet ground state <sup>6</sup>H<sub>5/2</sub> taken as the origin.

The magnetic susceptibility considering that excited states ( ${}^{6}\text{H}_{J}$  with J = 7/2 to 15/2) can be thermally populated is expressed as

$$\chi_{M} = \frac{\sum_{J=5/2}^{15/2} (2J+1)\chi_{M} (J) \exp\left[-\frac{E(J)}{kT}\right]}{\sum_{J=5/2}^{15/2} (2J+1) \exp\left[-\frac{E(J)}{kT}\right]}$$
  
With  $\chi_{M} (J) = \frac{Ng_{J}^{2}\beta^{2}J (J+1)}{3kT} + \frac{2N\beta^{2} (g_{J}-1)(g_{J}-2)}{3\lambda}$ 

In this frame  $\chi_M$  (for one Sm<sup>III</sup> site) can be rewritten:

$$\chi_{M} = \frac{N\beta^{2}}{3kT} \underbrace{ \begin{bmatrix} 6\left(\frac{5}{7} + \frac{120}{49x}\right) + 8\left(\frac{2028}{2189} + \frac{4884}{11907x}\right)e^{-\frac{7x}{2}} + 10\left(\frac{8427}{2297} - \frac{3864}{29403x}\right)e^{-8x} \\ + 12\left(\frac{22188}{429} - \frac{6612}{20449x}\right)e^{-\frac{27x}{2}} + 14\left(\frac{9375}{117} - \frac{1848}{4563x}\right)e^{-20x} \\ + 16\left(\frac{1020}{9} - \frac{12}{27x}\right)e^{-\frac{55x}{2}} \\ + 16\left(\frac{1020}{9} - \frac{12}{27x}\right)e^{-\frac{55x}{2}} \\ \end{bmatrix}_{i}$$

<sup>i</sup> The expression given in the book of O. Kahn (Molecular Magnetism, VCH: Weinhem, **1993**) is erroneous.



Figure S35. Temperature dependences of  $\chi_M T$  for compound 5. In inset, the field variation of the magnetization at 2 K.



Figure S36. Temperature dependences of  $\chi_M T$  for compound 6. In inset the  $\chi_M$  vs. T curve at low temperature.



Figure S37. Temperature dependences of  $\chi_M T$  for compounds 9 (white circles) and 10 (black circles). In inset the field variation of the magnetization at 2 K for the same two compounds with the best fitted curves (red lines) with a Brillouin function for two spins S=7/2.

## X-ray crystallography

| Table S1. Crystallographic Data for co | ompounds 1-10. |
|--|----------------|
|--|----------------|

| Identification code                      | 1  | 2   | 3   | 4  | 5  |
|--|--|---|---|--|--|
| Empirical formula                        | $C_{21}H_{15}N_6NdO_{21}$                        | $C_{21}H_{15}N_6O_{21}Eu$                         | $C_{16}H_{13}N_4NdO_{16}$                           | $C_{42}H_{18}N_{12}O_{40}Sm_2$                 | $C_{42}H_{24}N_{12}O_{40}Ce_2$                 |
| Formula weight                           | 831.63   | 839.35  | 661.54  | 1631.41  | 1616.97  |
| Temperature                              | 296(2) K   | 100(2) K  | 296(2) K  | 296(2) K                                       | 296(2) K                                       |
| Wavelength                               | 0.71073 Å  | 0.71073 Å   | 0.71073 Å   | 0.71073 Å                                      | 0.71073 Å                                      |
| Crystal system                           | Triclinic  | Triclinic   | Triclinic   | Monoclinic                                     | Monoclinic                                     |
| Space group                              | Pī   | Pī  | Pī  | Сс   | Сс   |
| Unit cell dimensions                     | $a = 9.2950(6)$ Å, $\alpha = 106.487(3)^{\circ}$ | $a = 9.2090(17)$ Å, $\alpha = 106.024(8)^{\circ}$ | $a = 8.9260(9)$ Å, $a = 75.642(3)^{\circ}$          | $a = 12.8390(14)$ Å, $a = 90^{\circ}$          | $a = 12.7786(18)$ Å, $\alpha = 90^{\circ}$     |
|  | $b = 11.472(8)$ Å, $\beta = 90.356(3)^{\circ}$   | $b = 11.329(2)$ Å, $\beta = 90.136(9)^{\circ}$    | $b = 8.983(8) \text{ Å}, \beta = 77.479(3)^{\circ}$ | $b = 47.454(6)$ Å, $\beta = 92.811(4)^{\circ}$ | $b = 47.775(7)$ Å, $\beta = 92.972(5)^{\circ}$ |
|  | $c = 13.821(10)$ Å, $\gamma = 94.15(3)^{\circ}$  | $c = 13.664(3)$ Å, $\gamma = 94.491(9)^{\circ}$   | $c = 16.6560(16)$ Å, $\gamma = 61.240(3)^{\circ}$   | $c = 9.2030(9)$ Å, $\gamma = 90^{\circ}$       | $c = 9.2651(10)$ Å, $\gamma = 90^{\circ}$      |
| Volume                                   | 1408.91(17) Å <sup>3</sup>                       | 1365.5(5) Å <sup>3</sup>                          | 1126.70(19) Å <sup>3</sup>                          | 5600.3(11) Å <sup>3</sup>                      | 5648.8(13) Å <sup>3</sup>                      |
| Ζ  | 2  | 2   | 2   | 4  | 4  |
| Density (calculated)                     | 1.960 Mg/m <sup>3</sup>                          | 2.041 Mg/m <sup>3</sup>                           | 1.950 Mg/m <sup>3</sup>                             | 1.935 Mg/m <sup>3</sup>                        | 1.901 Mg/m <sup>3</sup>                        |
| Absorption coefficient                   | 1.952 mm <sup>-1</sup>                           | 2.409 mm <sup>-1</sup>                            | 2.395 mm <sup>-1</sup>                              | 2.202 mm <sup>-1</sup>                         | 1.716 mm <sup>-1</sup>                         |
| F(000)                                   | 822  | 828   | 650   | 3192   | 3184   |
| Crystal size                             | 0.22 x 0.18 x 0.17 mm <sup>3</sup>               | 0.16 x 0.13 x 0.10 mm <sup>3</sup>                | 0.24 x 0.21 x 0.18 mm <sup>3</sup>                  | 0.18 x 0.17 x 0.15 mm <sup>3</sup>             | 0.24 x 0.22 x 0.19 mm <sup>3</sup>             |
| Theta range for data collection          | 1.54 to 30.88°.                                  | 1.55 to 31.81°.                                   | 2.54 to 32.61°.                                     | 1.64 to 27.97°.                                | 1.65 to 27.79°.                                |
| Index ranges                             | -13<=h<=13, -15<=k<=16,                          | -13<=h<=12, -16<=k<=16,                           | -13<=h<=13, -13<=k<=13,                             | -14<=h<=16, -60<=k<=62,                        | -16<=h<=16, -55<=k<=62,                        |
|  | -19<=1<=19                                       | -19<=l<=20  | -25<=l<=25  | -7<=l<=12                                      | -8<=l<=12                                      |
| Reflections collected                    | 30525  | 28187   | 30227   | 26340  | 25602  |
| Independent reflections                  | 8562 [R(int) = 0.0491]                           | 8849 [R(int) = 0.1450]                            | 8090 [R(int) = 0.0365]                              | 10017 [R(int) = 0.0798]                        | 11222 [R(int) = 0.0688]                        |
| Completeness to theta = $25.242^{\circ}$ | 98.0 %   | 98.9 %  | 99.5 %  | 100 %  | 99.6 %   |
| Absorption correction                    | Semi-empirical from equivalents                  | Semi-empirical from equivalents                   | Semi-empirical from equivalents                     | Semi-empirical from equivalents                | Semi-empirical from equivalents                |
| Max. and min. transmission               | 0.738 and 0.668                                  | 0.799 and 0.692                                   | 0.677 and 0.592                                     | 0.741 and 0.690                                | 0.742 and 0.681                                |
| Refinement method                        | Full-matrix least-squares on F <sup>2</sup>      | Full-matrix least-squares on F <sup>2</sup>       | Full-matrix least-squares on F <sup>2</sup>         | Full-matrix least-squares on F <sup>2</sup>    | Full-matrix least-squares on F <sup>2</sup>    |
| Data / restraints / parameters           | 8562 / 6 / 460                                   | 8849 / 6 / 460                                    | 8090 / 4 / 346                                      | 10017 / 2 / 885                                | 11222 / 11 / 883                               |
| Goodness-of-fit on F <sup>2</sup>        | 0.954  | 1.084   | 1.091   | 0.878  | 0.901  |
| Final R indices [I>2sigma(I)]            | R1 = 0.0406, wR2 = 0.0784                        | R1 = 0.0685, wR2 = 0.1649                         | R1 = 0.0318, $wR2 = 0.0788$                         | R1 = 0.0522, wR2 = 0.1174                      | R1 = 0.0541, wR2 = 0.1280                      |
| R indices (all data)                     | R1 = 0.0573, wR2 = 0.0851                        | R1 = 0.1269, wR2 = 0.2518                         | R1 = 0.0394, wR2 = 0.0855                           | R1 = 0.0759, wR2 = 0.1343                      | R1 = 0.0723, wR2 = 0.1451                      |
| Largest diff. peak and hole              | 1.225 and -1.142 e.Å <sup>-3</sup>               | 4.489 and -6.413 e.Å <sup>-3</sup>                | 2.594 and -0.930 e.Å <sup>-3</sup>                  | 2.284 and -1.224 e.Å <sup>-3</sup>             | 1.556 and -2.144 e.Å <sup>-3</sup>             |
| CCDC No.                                 | 1584550  | 1584545   | 1584549   | 1584552  | 1584543  |

| Identification code                      | 6   | 7  | 8   | 9   | 10  |
|--|---|--|---|---|---|
| Empirical formula                        | $C_{42}H_{18}N_{12}O_{40}Pr_2$                  | $C_{45}H_{31}N_{13}O_{40}La_2$                     | $C_{42}H_{30}N_{12}O_{42}Eu_2$                        | $C_{42}H_{30}N_{12}O_{42}Gd_2$                    | $C_{22}H_{26}N_4O_{24}Gd_2$                 |
| Formula weight                           | 1612.51   | 1671.65  | 1678.70   | 1689.24   | 1044.95                                     |
| Temperature                              | 296(2) K  | 296(2) K   | 296(2) K  | 296(2) K  | 100(2) K                                    |
| Wavelength                               | 0.71073 Å                                       | 0.71073 Å  | 0.71073 Å   | 0.71073 Å   | 0.71073 Å                                   |
| Crystal system                           | Monoclinic                                      | Triclinic  | Triclinic   | Triclinic   | Orthorhombic                                |
| Space group                              | Cc  | Pī   | Pī  | $P\overline{1}$                                   | Pbca  |
| Unit cell dimensions                     | $a = 12.771(3)$ Å, $\alpha = 90^{\circ}$ .      | $a = 8.9791(13)$ Å, $\alpha = 81.559(8)^{\circ}$ . | $a = 8.893(3)$ Å, $\alpha = 63.296(11)^{\circ}$       | $a = 8.9350(7)$ Å, $\alpha = 63.305(3)^{\circ}$ . | $a = 14.1321(4)$ Å, $\alpha = 90^{\circ}$ . |
|  | $b = 47.712(9)$ Å, $\beta = 92.452(11)^{\circ}$ | $b = 14.499(2)$ Å, $\beta = 89.492(7)^{\circ}$ .   | $b = 13.631(4) \text{ Å}, \beta = 79.353(13)^{\circ}$ | $b = 13.6750(12)$ Å, $\beta = 79.447(4)^{\circ}$  | $b = 8.8970(3)$ Å, $\beta = 90^{\circ}$ .   |
|  | $c = 9.221(2)$ Å, $\gamma = 90^{\circ}$ .       | $c = 23.157(4)$ Å, $\gamma = 81.411(7)^{\circ}$ .  | $c = 14.316(4)$ Å, $\gamma = 72.448(11)^{\circ}$      | $c = 14.3180(13)$ Å, $\gamma = 72.332(3)^{\circ}$ | $c = 25.7568(7)$ Å, $\gamma = 90^{\circ}$ . |
| Volume                                   | 5614(2) Å <sup>3</sup>                          | 2948.5(8) Å <sup>3</sup>                           | 1475.7(8) Å <sup>3</sup>                              | 1487.0(2) Å <sup>3</sup>                          | 3238.49(17) Å <sup>3</sup>                  |
| Ζ  | 4   | 2  | 1   | 1   | 4   |
| Density (calculated)                     | 1.908 Mg/m <sup>3</sup>                         | 1.883 Mg/m <sup>3</sup>                            | 1.889 Mg/m <sup>3</sup>                               | 1.886 Mg/m <sup>3</sup>                           | 2.143 Mg/m <sup>3</sup>                     |
| Absorption coefficient                   | 1.841 mm <sup>-1</sup>                          | 1.553 mm <sup>-1</sup>                             | 2.230 mm <sup>-1</sup>                                | 2.334 mm <sup>-1</sup>                            | 4.166 mm <sup>-1</sup>                      |
| F(000)                                   | 3168  | 1652   | 828   | 830   | 2024  |
| Crystal size                             | 0.16 x 0.14 x 0.12 mm <sup>3</sup>              | 0.19 x 0.17 x 0.16 mm <sup>3</sup>                 | 0.19 x 0.16 x 0.12 mm <sup>3</sup>                    | 0.18 x 0.15 x 0.12 mm <sup>3</sup>                | 0.17 x 0.15 x 0.13 mm <sup>3</sup>          |
| Theta range for data collection          | 1.65 to 27.26°.                                 | 1.57 to 30.25°.                                    | 1.59 to 33.22°.                                       | 1.59 to 28.04°.                                   | 1.58 to 35.44°.                             |
| Index ranges                             | -16<=h<=12, -54<=k<=60,                         | -12<=h<=12, -20<=k<=20,                            | -8<=h<=13, -20<=k<=20,                                | -11<=h<=11, -18<=k<=16,                           | -17<=h<=22, -8<=k<=14,                      |
|  | -11<=1<=11                                      | -32<=1<=32   | -20<=l<=21  | -18<=l<=18  | -41<=1<=33                                  |
| Reflections collected                    | 24423   | 68102  | 25104   | 26132   | 30138                                       |
| Independent reflections                  | 9624 [R(int) = 0.0547]                          | 17467 [R(int) = 0.0530]                            | 9806 [R(int) = 0.0330]                                | 7111 [R(int) = 0.0213]                            | 7216 [R(int) = 0.0249]                      |
| Completeness to theta = $25.242^{\circ}$ | 100 %   | 100 %  | 93.5 %  | 100 %   | 99.9 %                                      |
| Absorption correction                    | Semi-empirical from equivalents                 | Semi-empirical from equivalents                    | Semi-empirical from equivalents                       | Semi-empirical from equivalents                   | Semi-empirical from equivalents             |
| Max. and min. transmission               | 0.814 and 0.751                                 | 0.795 and 0.751                                    | 0.781 and 0.672                                       | 0.772 and 0.671                                   | 0.619 and 0. 531                            |
| Refinement method                        | Full-matrix least-squares on F <sup>2</sup>     | Full-matrix least-squares on F <sup>2</sup>        | Full-matrix least-squares on F <sup>2</sup>           | Full-matrix least-squares on F <sup>2</sup>       | Full-matrix least-squares on F <sup>2</sup> |
| Data / restraints / parameters           | 9624 / 2 / 865                                  | 17467 / 9 / 921                                    | 9806 / 6 / 470  | 7111 / 9 / 470                                    | 7216 / 4 / 249                              |
| Goodness-of-fit on F <sup>2</sup>        | 0.973   | 1.001  | 1.077   | 0.971   | 1.279                                       |
| Final R indices [I>2sigma(I)]            | R1 = 0.0390, wR2 = 0.0732                       | R1 = 0.0381, $wR2 = 0.0810$                        | R1 = 0.0473, WR2 = 0.0972                             | R1 = 0.0176, wR2 = 0.0439                         | R1 = 0.0270, wR2 = 0.0603                   |
| R indices (all data)                     | R1 = 0.0532, $wR2 = 0.0786$                     | R1 = 0.0595, wR2 = 0.0902                          | R1 = 0.0729, WR2 = 0.1279                             | R1 = 0.0190, wR2 = 0.0449                         | R1 = 0.0325, $wR2 = 0.0626$                 |
| Largest diff. peak and hole              | 1.235 and -1.041 e.Å <sup>-3</sup>              | 1.075 and -0.739 e.Å <sup>-3</sup>                 | 4.066 and -4.056 e.Å <sup>-3</sup>                    | 0.630 and -0.511 e.Å <sup>-3</sup>                | 2.483 and -1.556 e.Å <sup>-3</sup>          |
| CCDC No.                                 | 1584551   | 1584548  | 1584544   | 1584547   | 1584546                                     |

 Table S2. Possible important hydrogen bonding interactions for complexes 1-10.

Complex 1

| Х-Н…Ү                     | Χ…Υ            | $H{\cdots}Y$ | ∠Х-Н…Ү        |                |             |
|---------------------------|----------------|--------------|---------------|----------------|-------------|
| O1W-H11W…O15              | 3.647(7)       | 2.84         | 166           |                |             |
| O2W-H21W…O1               | 2.810(3)       | 2.50         | 103           |                |             |
| O2W-H22W…O1W              | 2.766(5)       | 2.01         | 158           |                |             |
| O3W-H31WO1W1              | 3.242(5)       | 2.77         | 118           |                |             |
| O3W-H32WO1W1              | 3.242 (5)      | 2.94         | 105           |                |             |
| O3W-H32W…O2W <sup>1</sup> | 2.790 (3)      | 2.00         | 170           |                |             |
| $O3W-H32W\cdots O8^{1}$   | 3.186 (3)      | 2.78         | 114           |                |             |
| O1W-H12W…N6 <sup>2</sup>  | 3.622(6)       | 2.93         | 143           |                |             |
| O1W-H12WO17 <sup>2</sup>  | 3.156(6)       | 2.44         | 148           |                |             |
| O1W-H12WO18 <sup>2</sup>  | 3.307(7)       | 2.74         | 128           |                |             |
| O1W-H12WO16 <sup>3</sup>  | 3.253(7)       | 2.86         | 112           |                |             |
| O2W-H21WO54               | 2.993(4)       | 2.25         | 151           |                |             |
| O3W-H31WO3 <sup>5</sup>   | 3.167(4)       | 2.64         | 124           |                |             |
| O3W-H31WO45               | 3.112(4)       | 2.39         | 148           |                |             |
| O3W-H31WN15               | 3.308 (4)      | 2.69         | 133           |                |             |
| (1) -x+1, -y, -z+1        | (2) -x, -y, -z | (3) -x+      | l, -y, -z (4) | -x, -y+1, -z+1 | (5) x, +y-1 |

| Х-Н…Ү                             | X···Y   | Н…Ү  | ∠Х-Н…Ү |  |  |  |  |
|-----------------------------------|---|------|--------|--|--|--|--|
| O2W-H22W…O1                       | 2.790(9)  | 2.50 | 101    |  |  |  |  |
| O3W-H31W…O5                       | 3.263(14)   | 2.72 | 126    |  |  |  |  |
| O3W-H31W…O6                       | 3.571(11)   | 2.91 | 138    |  |  |  |  |
| O3W-H31W…O161                     | 3.168(15)   | 2.43 | 152    |  |  |  |  |
| O1W-H12W…O4 <sup>2</sup>          | 3.569(10)   | 2.99 | 130    |  |  |  |  |
| O1W-H12W…O8 <sup>3</sup>          | 3.143(10)   | 2.65 | 120    |  |  |  |  |
| O1W-H12W…O2W <sup>3</sup>         | 2.775(9)  | 2.15 | 132    |  |  |  |  |
| O2W-H22W…O3 <sup>4</sup>          | 2.936 (12)  | 2.17 | 154    |  |  |  |  |
| O3W-H32W…O18 <sup>4</sup>         | 3.340 (11)  | 2.73 | 132    |  |  |  |  |
| O1W-H11W…O6 <sup>5</sup>          | 3.049 (11)  | 2.50 | 123    |  |  |  |  |
| O1W-H11W…N2 <sup>5</sup>          | 3.250 (12)  | 2.79 | 117    |  |  |  |  |
| O1W-H11W···O3W <sup>5</sup>       | 3.207 (11)  | 2.50 | 144    |  |  |  |  |
| O1W-H11W…O5 <sup>5</sup>          | 3.128(12)   | 2.64 | 119    |  |  |  |  |
| O3W-H32W…O15 <sup>6</sup>         | 3.636(14)   | 2.91 | 149    |  |  |  |  |
| O2W-H21W···O3W <sup>6</sup>       | 2.722(11)   | 2.16 | 126    |  |  |  |  |
| (1) x, $+y-1$ , $+z-1$ (2) $-x+2$ | 1) x, +y-1, +z-1 (2) -x+2, -y+2, -z+2 (3) -x+1, -y+2, -z+2 (4) -x+2, -y+1, -z+2 (5) x, +y+1, +z |      |        |  |  |  |  |
| (6) -x+1, -y+1, -z+2              |   |      |        |  |  |  |  |
| Complex <b>3</b>                  |   |      |        |  |  |  |  |

| Х-Н…Ү                    | X···Y          | Н…Ү          | ∠Х-Н…Ү |
|--------------------------|----------------|--------------|--------|
| O1W-H12W…O1              | 2.994(4)       | 2.65         | 108    |
| O1W-H12WO2               | 3.294(3)       | 2.68         | 134    |
| O2W-H21WO141             | 2.668(4)       | 1.85         | 170    |
| O1W-H12WO1 <sup>2</sup>  | 2.774(3)       | 2.13         | 136    |
| O1W-H12WO2 <sup>2</sup>  | 2.864(3)       | 2.60         | 101    |
| O1W-H12WO2W <sup>2</sup> | 3.375(3)       | 2.87         | 123    |
| O1W-H11WO2W <sup>2</sup> | 3.375(3)       | 2.87         | 125    |
| O1W-H11WO1 <sup>2</sup>  | 2.774(3)       | 2.11         | 144    |
| O2W-H22WN1 <sup>2</sup>  | 3.510(4)       | 2.77         | 154    |
| O2W-H22WO3 <sup>2</sup>  | 2.961(4)       | 2.25         | 147    |
| O2W-H22WO4 <sup>2</sup>  | 3.684(5)       | 2.93         | 155    |
| (1) -x+2, -y+2, -z (     | 2) -x+1, -y+2, | , <b>-</b> Z |        |
|                          |                |              |        |

| Х-Н…Ү                     | X···Y         | Н…Ү        | ∠Х-Н…Ү          |     |
|---------------------------|---------------|------------|-----------------|-----|
| O2W-H21W…O2               | 2.746(9)      | 1.98       | 154             |     |
| O2W-H21W…O3               | 3.368(12)     | 2.83       | 124             |     |
| O3W-H31W…N11              | 3.617(12)     | 2.97       | 137             |     |
| O3W-H31W…O27              | 3.463(12)     | 2.79       | 140             |     |
| O3W-H31W…O33              | 3.205(12)     | 2.49       | 147             |     |
| O4W-H42W…O14              | 2.804(10)     | 2.51       | 102             |     |
| $O4W-H42W\cdots O36^{1}$  | 3.182(12)     | 2.41       | 156             |     |
| O3W-H31W…O29 <sup>2</sup> | 2.994(13)     | 2.56       | 115             |     |
| O2W-H22W…O9 <sup>3</sup>  | 3.077(11)     | 2.32       | 152             |     |
| O2W-H22W…O10 <sup>3</sup> | 3.406(13)     | 2.91       | 121             |     |
| O3W-H32W…O20 <sup>3</sup> | 2.941(10)     | 2.62       | 105             |     |
| $O3W-H32W\cdots O1W^3$    | 2.944(10)     | 2.21       | 148             |     |
| O4W-H41W…O1 <sup>3</sup>  | 2.728(9)      | 2.03       | 145             |     |
| $O2W-H22W\cdots N3^3$     | 3.440(12)     | 2.82       | 133             |     |
| O4W-H42W…O21 <sup>3</sup> | 2.917(11)     | 2.39       | 123             |     |
| (1) $x+1, +y, +z$ (2)     | x-1/2, -y+1/2 | +1, +z+1/2 | (3) $x, +y, +z$ | z+1 |

| Х-Н…Ү        | X····Y   | $\mathbf{H} \cdots \mathbf{Y}$ | ∠Х-Н…Ү |
|--------------|----------|--------------------------------|--------|
| O1W-H11W…O25 | 2.759(3) | 2.45                           | 104    |
| O2W-H21W…O26 | 2.879(3) | 2.59                           | 103    |

| O2W-H21W…O37              | 2.826(3)        | 2.04        | 166     |                   |
|---------------------------|-----------------|-------------|---------|-------------------|
| O3W-H32W…O2               | 2.836(4)        | 2.52        | 104     |                   |
| O3W-H32W…O3               | 3.036 (3)       | 2.22        | 171     |                   |
| O2W-H22W…O21 <sup>1</sup> | 3.078 (4)       | 2.73        | 109     |                   |
| O2W-H22W…O311             | 2.868(4)        | 2.55        | 105     |                   |
| O2W-H22W…O331             | 3.158(4)        | 2.36        | 173     |                   |
| O1W-H12WO6 <sup>2</sup>   | 3.339(4)        | 2.67        | 142     |                   |
| $O1W-H12W\cdots N2^2$     | 3.500(4)        | 2.71        | 166     |                   |
| O1W-H12W…O5 <sup>2</sup>  | 2.884(4)        | 2.10        | 164     |                   |
| O1W-H11W…N12 <sup>3</sup> | 3.537(4)        | 2.86        | 143     |                   |
| O1W-H11W…O35 <sup>3</sup> | 3.033(4)        | 2.24        | 166     |                   |
| O1W-H11W…O36 <sup>3</sup> | 3.289(4)        | 2.82        | 119     |                   |
| O3W-H31W…O1W <sup>4</sup> | 2.734(3)        | 1.94        | 163     |                   |
| (1) x+1, +y, +z (2) -x+   | 1, -y+1, -z+2 ( | (3) x+1, +y | ∕-1, +z | (4) $x-1, +y, +z$ |

| X-H···Y                        | X···Y           | $H \cdots Y$ | ∠Х-Н…Ү      |                      |
|--------------------------------|-----------------|--------------|-------------|----------------------|
| O1W-H12W…O13                   | 2.623(8)        | 1.87         | 153         |                      |
| O2W-H22W…O4                    | 3.303(6)        | 2.98         | 106         |                      |
| $O1W\text{-}H11W^{\dots}N1^1$  | 3.451(10)       | 2.75         | 145         |                      |
| O1W-H11W…O3 <sup>2</sup>       | 2.978(9)        | 2.42         | 127         |                      |
| O2W-H21W…O7 <sup>2</sup>       | 2.686(8)        | 1.87         | 174         |                      |
| O1W-H11W…O4 <sup>2</sup>       | 3.194(10)       | 2.46         | 152         |                      |
| O1W-H11 $W$ ···N1 <sup>2</sup> | 3.451(10)       | 2.75         | 147         |                      |
| O3W-H31W…O12 <sup>3</sup>      | 3.329(13)       | 2.95         | 111         |                      |
| $O3W-H32W\cdots N4^3$          | 3.475(12)       | 2.81         | 139         |                      |
| O3W-H32W…O11 <sup>3</sup>      | 2.898(10)       | 2.12         | 159         |                      |
| O3W-H32W…O12 <sup>3</sup>      | 3.329(13)       | 2.88         | 116         |                      |
| $O2W-H22W\cdots O5^4$          | 3.489(10)       | 2.85         | 136         |                      |
| O2W-H22W…O6 <sup>4</sup>       | 2.980(8)        | 2.17         | 173         |                      |
| O2W-H22 $W$ ···N2 <sup>4</sup> | 3.575(9)        | 2.80         | 158         |                      |
| $O3W-H31W\cdots N2^4$          | 3.740(7)        | 2.96         | 160         |                      |
| O3W-H31W…O5 <sup>4</sup>       | 2.865(6)        | 2.06         | 167         |                      |
| (1) -x+1, -y, -z+2             | (2) $x, +y, +z$ | -1 (3)       | x, +y, +z+1 | (4) -x+1, -y+1, -z+2 |
|                                |                 |              |             |                      |

| Х-Н…Ү       | X····Y    | Н…Ү  | ∠Х-Н…Ү |
|-------------|-----------|------|--------|
| O1W-H12W…O4 | 3.298(2)  | 2.90 | 113    |
| O2W-H22W…O7 | 2.830 (3) | 2.56 | 101    |
| O2W-H22W…O8 | 2.619(3)  | 1.86 | 158    |

| O3W-H32W…O7               | 2.652 (2)            | 2.38             | 101 |
|---------------------------|----------------------|------------------|-----|
| O3W-H31WO181              | 3.351(5)             | 2.99             | 110 |
| $O3W-H32W\cdots N6^{1}$   | 3.496 (4)            | 2.98             | 125 |
| O3W-H32W…O17 <sup>1</sup> | 2.903 (4)            | 2.26             | 138 |
| O1W-H11W…O13 <sup>2</sup> | 2.696 (3)            | 1.89             | 173 |
| $O2W-H21W\cdots N1^2$     | 3.464 (3)            | 2.75             | 150 |
| O2W-H21W…O3 <sup>2</sup>  | 2.994 (3)            | 2.41             | 131 |
| O2W-H21W…O4 <sup>2</sup>  | 3.199 (4)            | 2.46             | 154 |
| O3W-H31W⋯O5 <sup>3</sup>  | 2.868 (2)            | 2.06             | 170 |
| $O1W-H12W\cdots N2^3$     | 3.587 (3)            | 2.80             | 165 |
| O1₩-H12W…O5 <sup>3</sup>  | 3.497 (4)            | 2.84             | 140 |
| O1₩-H12W…O6 <sup>3</sup>  | 2.997 (3)            | 2.20             | 171 |
| O3W-H31W…N2 <sup>3</sup>  | 3.752 (2)            | 2.99             | 157 |
| (1) $x, +y, +z-1$ (2)     | -x+1, -y+2, -z+1 (3) | -x+1, -y+1, -z+1 |     |

| Х-Н⋯Ү                          | $\mathbf{X}\cdots\mathbf{Y}$ | $H \cdots Y$ | ∠Х-Н…Ү                 |     |
|--------------------------------|------------------------------|--------------|------------------------|-----|
| $O1W-H12W\cdots O8^{1}$        | 2.689 (2)                    | 1.88         | 176                    |     |
| O2W-H21WO101                   | 2.693(2)                     | 1.897        | 169                    |     |
| O2W-H22W…O7 <sup>2</sup>       | 2.696(2)                     | 1.94         | 154                    |     |
| O1W-H11W…O2 <sup>3</sup>       | 2.841(2)                     | 2.03         | 172                    |     |
| (1) $-x+1/2$ , $+y+1/2$ , $+z$ | (2) $x-1/2, +y$              | r-1, -z+1/2  | (3) $-x+1/2, -y, +z-1$ | 1/2 |

| Table S3. Important bond distances ( | Å | ) and bond angles | (°) ( | of complexes | 1-10. |
|--------------------------------------|---|-------------------|-------|--------------|-------|
|--------------------------------------|---|-------------------|-------|--------------|-------|

| Complex 1  |   |
|--|---|
| O(1)-Nd(1)   | 2.478(2)  |
| O(2W)-Nd(1)  | 2.579(2)  |
| O(3W)-Nd(1)  | 2.513(2)  |
| O(7)-Nd(1)   | 2.440(2)  |
| O(8)-Nd(1)   | 2.392(2)  |
| O(13)-Nd(1)  | 2.385(2)  |
| O(14)-Nd(1)  | 2.470(2)  |
| O(13)-Nd(1)-O(8)   | 143.06(8)   |
| O(12) Nd(1) $O(7)$   |   |
| O(13)-Nu(1)-O(7)   | 75.45(8)  |
| O(13)-Nd(1)-O(7)<br>O(8)-Nd(1)-O(7)  | 75.45(8)<br>101.28(7)   |
| O(13)-Nd(1)-O(7)<br>O(13)-Nd(1)-O(14)  | 75.45(8)<br>101.28(7)<br>128.84(7)                                      |
| O(13)-Nd(1)-O(7)<br>O(8)-Nd(1)-O(14)<br>O(8)-Nd(1)-O(14)   | 75.45(8)<br>101.28(7)<br>128.84(7)<br>77.16(7)                          |
| O(13)-Nd(1)-O(7)<br>O(8)-Nd(1)-O(14)<br>O(8)-Nd(1)-O(14)<br>O(7)-Nd(1)-O(14)                     | 75.45(8)<br>101.28(7)<br>128.84(7)<br>77.16(7)<br>140.09(8)             |
| O(13)-Nd(1)-O(7)<br>O(8)-Nd(1)-O(14)<br>O(8)-Nd(1)-O(14)<br>O(7)-Nd(1)-O(14)<br>O(13)-Nd(1)-O(1) | 75.45(8)<br>101.28(7)<br>128.84(7)<br>77.16(7)<br>140.09(8)<br>81.55(8) |

| O(7)-Nd(1)-O(1)   | 139.04(8) |
|-------------------|-----------|
| O(14)-Nd(1)-O(1)  | 80.31(8)  |
| O(13)-Nd(1)-O(3W) | 136.78(8) |
| O(8)-Nd(1)-O(3W)  | 72.65(8)  |
| O(7)-Nd(1)-O(3W)  | 73.00(8)  |
| O(14)-Nd(1)-O(3W) | 68.51(8)  |
| O(1)-Nd(1)-O(3W)  | 140.74(8) |
| O(13)-Nd(1)-O(2W) | 72.18(8)  |
| O(8)-Nd(1)-O(2W)  | 71.71(8)  |
| O(7)-Nd(1)-O(2W)  | 73.38(8)  |
| O(14)-Nd(1)-O(2W) | 138.86(8) |
| O(1)-Nd(1)-O(2W)  | 67.46(8)  |
| O(3W)-Nd(1)-O(2W) | 124.00(8) |

| O(1)-Eu(1)        | 2.430(8) |
|-------------------|----------|
| O(2)-Eu(1)        | 2.948(5) |
| O(7)-Eu(1)        | 2.402(4) |
| O(8)-Eu(1)        | 2.352(7) |
| O(13)-Eu(1)       | 2.339(4) |
| O(14)-Eu(1)       | 2.430(4) |
| O(1W)-Eu(1)       | 2.456(2) |
| O(2W)-Eu(1)       | 2.530(1) |
| O(13)-Eu(1)-O(8)  | 142.7(2) |
| O(13)-Eu(1)-O(7)  | 76.2(2)  |
| O(8)-Eu(1)-O(7)   | 101.4(1) |
| O(13)-Eu(1)-O(14) | 128.7(1) |
| O(8)-Eu(1)-O(14)  | 76.6(2)  |
| O(7)-Eu(1)-O(14)  | 140.3(2) |
| O(13)-Eu(1)-O(1)  | 81.0(2)  |
| O(8)-Eu(1)-O(1)   | 77.7(2)  |
| O(7)-Eu(1)-O(1)   | 139.6(2) |
| O(14)-Eu(1)-O(1)  | 79.5(2)  |
| O(13)-Eu(1)-O(1W) | 137.6(2) |
| O(8)-Eu(1)-O(1W)  | 72.7(2)  |
| O(7)-Eu(1)-O(1W)  | 73.1(2)  |
| O(14)-Eu(1)-O(1W) | 68.5(2)  |
| O(1)-Eu(1)-O(1W)  | 140.3(2) |
| O(13)-Eu(1)-O(2W) | 72.4(2)  |
| O(8)-Eu(1)-O(2W)  | 71.4(2)  |

| O(7)-Eu(1)-O(2W)  | 73.1(2)   |
|-------------------|-----------|
| O(14)-Eu(1)-O(2W) | 138.4(2)  |
| O(1)-Eu(1)-O(2W)  | 68.4(2)   |
| O(1W)-Eu(1)-O(2W) | 123.6(2)  |
| O(13)-Eu(1)-O(2)  | 66.1(2)   |
| O(7)-Eu(1)-O(2)   | 140.0(2)  |
| O(14)-Eu(1)-O(2)  | 65.9(2)   |
| O(1)-Eu(1)-O(2)   | 47.22(1)  |
| O(1W)-Eu(1)-O(2)  | 128.80(1) |
| O(2W)-Eu(1)-O(2)  | 105.9(2)  |
| O(8)-Eu(1)-O(2)   | 116.3(2)  |
|                   |           |

| 2.4404(18) |
|------------|
| 2.536(2)   |
| 2.488(2)   |
| 2.4837(19) |
| 2.453(2)   |
| 2.5221(18) |
| 2.5732(19) |
| 142.39(7)  |
| 78.44(6)   |
| 136.93(6)  |
| 71.97(7)   |
| 71.34(7)   |
| 138.03(7)  |
| 124.76(6)  |
| 72.38(7)   |
| 70.17(6)   |
| 103.47(7)  |
| 73.95(7)   |
| 125.50(8)  |
| 66.79(7)   |
| 128.82(8)  |
| 127.31(6)  |
| 77.52(7)   |
| 98.62(8)   |
| 73.12(7)   |
| 71.93(7)   |
| 50.68(6)   |
|            |

| O(1W)-Nd(1)-O(14) | 134.34(8) |
|-------------------|-----------|
|-------------------|-----------|

| O(1)-Sm(2)        | 2.513(10) |
|-------------------|-----------|
| O(2)-Sm(2)        | 2.588(9)  |
| O(1W)-Sm(1)       | 2.514(9)  |
| O(2W)-Sm(2)       | 2.539(11) |
| O(3W)-Sm(1)       | 2.528(10) |
| O(4W)-Sm(1)       | 2.503(10) |
| O(7)-Sm(2)        | 2.391(9)  |
| O(8)-Sm(1)        | 2.419(9)  |
| O(13)-Sm(1)       | 2.347(9)  |
| O(14)-Sm(2)       | 2.457(9)  |
| O(19)-Sm(2)       | 2.388(10) |
| O(19)-Sm(1)       | 2.662(10) |
| O(20)-Sm(1)       | 2.481(11) |
| O(25)-Sm(1)       | 2.408(9)  |
| O(25)-Sm(2)       | 2.658(9)  |
| O(26)-Sm(2)       | 2.576(11) |
| O(31)-Sm(2)       | 2.341(9)  |
| O(32)-Sm(1)       | 2.405(10) |
| O(13)-Sm(1)-O(32) | 92.9(3)   |
| O(13)-Sm(1)-O(25) | 150.8(3)  |
| O(32)-Sm(1)-O(25) | 84.9(3)   |
| O(13)-Sm(1)-O(8)  | 82.2(3)   |
| O(32)-Sm(1)-O(8)  | 140.5(4)  |
| O(25)-Sm(1)-O(8)  | 81.2(3)   |
| O(13)-Sm(1)-O(20) | 83.9(3)   |
| O(32)-Sm(1)-O(20) | 138.2(4)  |
| O(25)-Sm(1)-O(20) | 116.6(3)  |
| O(8)-Sm(1)-O(20)  | 80.5(4)   |
| O(13)-Sm(1)-O(4W) | 73.3(3)   |
| O(32)-Sm(1)-O(4W) | 72.6(3)   |
| O(25)-Sm(1)-O(4W) | 78.3(3)   |
| O(8)-Sm(1)-O(4W)  | 68.5(4)   |
| O(20)-Sm(1)-O(4W) | 143.3(4)  |
| O(13)-Sm(1)-O(1W) | 70.6(3)   |
| O(32)-Sm(1)-O(1W) | 73.2(3)   |
| O(25)-Sm(1)-O(1W) | 135.2(3)  |
| O(8)-Sm(1)-O(1W)  | 138.6(3)  |

| O(20)-Sm(1)-O(1W) | 66.4(3)  |
|-------------------|----------|
| O(4W)-Sm(1)-O(1W) | 128.0(3) |
| O(13)-Sm(1)-O(3W) | 134.9(3) |
| O(32)-Sm(1)-O(3W) | 74.1(3)  |
| O(25)-Sm(1)-O(3W) | 72.4(3)  |
| O(8)-Sm(1)-O(3W)  | 134.3(3) |
| O(20)-Sm(1)-O(3W) | 79.0(3)  |
| O(4W)-Sm(1)-O(3W) | 137.0(3) |
| O(1W)-Sm(1)-O(3W) | 64.3(3)  |
| O(13)-Sm(1)-O(19) | 128.3(3) |
| O(32)-Sm(1)-O(19) | 136.0(3) |
| O(25)-Sm(1)-O(19) | 66.5(3)  |
| O(8)-Sm(1)-O(19)  | 69.5(3)  |
| O(20)-Sm(1)-O(19) | 50.2(3)  |
| O(4W)-Sm(1)-O(19) | 128.2(3) |
| O(1W)-Sm(1)-O(19) | 103.5(3) |
| O(3W)-Sm(1)-O(19) | 65.9(3)  |
| O(13)-Sm(1)-C(36) | 107.5(4) |
| O(32)-Sm(1)-C(36) | 140.5(4) |
| O(25)-Sm(1)-C(36) | 92.0(4)  |
| O(8)-Sm(1)-C(36)  | 77.0(4)  |
| O(20)-Sm(1)-C(36) | 24.7(3)  |
| O(4W)-Sm(1)-C(36) | 145.1(4) |
| O(1W)-Sm(1)-C(36) | 82.0(4)  |
| O(3W)-Sm(1)-C(36) | 67.5(4)  |
| O(19)-Sm(1)-C(36) | 25.9(3)  |
| O(31)-Sm(2)-O(19) | 147.0(3) |
| O(31)-Sm(2)-O(7)  | 139.9(3) |
| O(19)-Sm(2)-O(7)  | 72.8(3)  |
| O(31)-Sm(2)-O(14) | 108.3(3) |
| O(19)-Sm(2)-O(14) | 81.7(3)  |
| O(7)-Sm(2)-O(14)  | 74.0(3)  |
| O(31)-Sm(2)-O(1)  | 73.6(4)  |
| O(19)-Sm(2)-O(1)  | 79.5(3)  |
| O(7)-Sm(2)-O(1)   | 140.2(3) |
| O(14)-Sm(2)-O(1)  | 74.2(3)  |
| O(31)-Sm(2)-O(2W) | 71.0(4)  |
| O(19)-Sm(2)-O(2W) | 141.8(3) |
| O(7)-Sm(2)-O(2W)  | 70.2(3)  |
| O(14)-Sm(2)-O(2W) | 79.3(4)  |

| O(1)-Sm(2)-O(2W)  | 125.5(3) |
|-------------------|----------|
| O(31)-Sm(2)-O(26) | 74.0(4)  |
| O(19)-Sm(2)-O(26) | 116.2(4) |
| O(7)-Sm(2)-O(26)  | 82.4(4)  |
| O(14)-Sm(2)-O(26) | 144.6(4) |
| O(1)-Sm(2)-O(26)  | 136.4(4) |
| O(2W)-Sm(2)-O(26) | 68.0(4)  |
| O(31)-Sm(2)-O(2)  | 74.4(3)  |
| O(19)-Sm(2)-O(2)  | 73.8(3)  |
| O(7)-Sm(2)-O(2)   | 139.7(3) |
| O(14)-Sm(2)-O(2)  | 122.4(3) |
| O(1)-Sm(2)-O(2)   | 50.8(3)  |
| O(2W)-Sm(2)-O(2)  | 143.8(3) |
| O(26)-Sm(2)-O(2)  | 92.6(3)  |
| O(31)-Sm(2)-O(25) | 112.1(3) |
| O(19)-Sm(2)-O(25) | 66.9(3)  |
| O(7)-Sm(2)-O(25)  | 72.6(3)  |
| O(14)-Sm(2)-O(25) | 139.4(3) |
| O(1)-Sm(2)-O(25)  | 121.4(3) |
| O(2W)-Sm(2)-O(25) | 109.7(3) |
| O(26)-Sm(2)-O(25) | 49.7(3)  |
| O(2)-Sm(2)-O(25)  | 73.9(3)  |

| 2.592(9)  |
|-----------|
| 2.646(8)  |
| 2.390(8)  |
| 2.459(9)  |
| 2.456(9)  |
| 2.698(9)  |
| 2.566(10) |
| 2.530(8)  |
| 2.448(8)  |
| 2.457(8)  |
| 2.479(8)  |
| 2.489(8)  |
| 2.675(9)  |
| 2.663(11) |
| 2.632(8)  |
|           |

| O(2W)-Ce(2)       | 2.572(9)  |
|-------------------|-----------|
| O(3W)-Ce(2)       | 2.524(10) |
| O(4W)-Ce(2)       | 2.555(8)  |
| O(7)-Ce(1)-O(13)  | 147.4(3)  |
| O(7)-Ce(1)-O(25)  | 140.1(3)  |
| O(13)-Ce(1)-O(25) | 71.9(3)   |
| O(7)-Ce(1)-O(19)  | 111.7(3)  |
| O(13)-Ce(1)-O(19) | 79.4(3)   |
| O(25)-Ce(1)-O(19) | 72.8(3)   |
| O(7)-Ce(1)-O(1)   | 74.6(3)   |
| O(13)-Ce(1)-O(1)  | 79.3(3)   |
| O(25)-Ce(1)-O(1)  | 140.1(3)  |
| O(19)-Ce(1)-O(1)  | 75.3(3)   |
| O(7)-Ce(1)-O(1W)  | 70.7(3)   |
| O(13)-Ce(1)-O(1W) | 141.9(3)  |
| O(25)-Ce(1)-O(1W) | 70.6(3)   |
| O(19)-Ce(1)-O(1W) | 83.9(3)   |
| O(1)-Ce(1)-O(1W)  | 128.8(3)  |
| O(7)-Ce(1)-O(2)   | 74.6(3)   |
| O(13)-Ce(1)-O(2)  | 73.7(3)   |
| O(25)-Ce(1)-O(2)  | 138.7(3)  |
| O(19)-Ce(1)-O(2)  | 121.9(3)  |
| O(1)-Ce(1)-O(2)   | 49.8(3)   |
| O(1W)-Ce(1)-O(2)  | 142.8(3)  |
| O(7)-Ce(1)-O(32)  | 74.3(3)   |
| O(13)-Ce(1)-O(32) | 114.8(3)  |
| O(25)-Ce(1)-O(32) | 81.4(3)   |
| O(19)-Ce(1)-O(32) | 145.1(4)  |
| O(1)-Ce(1)-O(32)  | 136.7(3)  |
| O(1W)-Ce(1)-O(32) | 65.2(4)   |
| O(2)-Ce(1)-O(32)  | 93.1(3)   |
| O(7)-Ce(1)-O(31)  | 110.8(3)  |
| O(13)-Ce(1)-O(31) | 67.2(3)   |
| O(25)-Ce(1)-O(31) | 72.1(3)   |
| O(19)-Ce(1)-O(31) | 137.3(3)  |
| O(1)-Ce(1)-O(31)  | 120.8(3)  |
| O(1W)-Ce(1)-O(31) | 106.3(3)  |
| O(2)-Ce(1)-O(31)  | 74.1(3)   |
| O(32)-Ce(1)-O(31) | 48.1(3)   |
| O(26)-Ce(2)-O(31) | 80.7(2)   |

| O(26)-Ce(2)-O(3W) | 68.3(2)   |
|-------------------|-----------|
| O(31)-Ce(2)-O(3W) | 79.0(2)   |
| O(26)-Ce(2)-O(4W) | 139.7(2)  |
| O(31)-Ce(2)-O(4W) | 134.1(2)  |
| O(3W)-Ce(2)-O(4W) | 128.5(2)  |
| O(26)-Ce(2)-O(14) | 81.0(3)   |
| O(31)-Ce(2)-O(14) | 115.8(2)  |
| O(3W)-Ce(2)-O(14) | 143.5(3)  |
| O(4W)-Ce(2)-O(14) | 66.4(2)   |
| O(26)-Ce(2)-O(2W) | 133.9(2)  |
| O(31)-Ce(2)-O(2W) | 72.0(2)   |
| O(3W)-Ce(2)-O(2W) | 137.3(2)  |
| O(4W)-Ce(2)-O(2W) | 63.4(2)   |
| O(14)-Ce(2)-O(2W) | 78.6(2)   |
| O(26)-Ce(2)-O(13) | 69.4(2)   |
| O(31)-Ce(2)-O(13) | 66.36(19) |
| O(3W)-Ce(2)-O(13) | 128.5(2)  |
| O(4W)-Ce(2)-O(13) | 102.8(2)  |
| O(14)-Ce(2)-O(13) | 49.6(2)   |
| O(2W)-Ce(2)-O(13) | 65.9(3)   |

| O(1)-Pr(1)  | 2.575(6) |
|-------------|----------|
| O(2)-Pr(1)  | 2.642(5) |
| O(1W)-Pr(1) | 2.581(6) |
| O(2W)-Pr(2) | 2.571(6) |
| O(3W)-Pr(2) | 2.557(5) |
| O(4W)-Pr(2) | 2.526(6) |
| O(7)-Pr(1)  | 2.378(6) |
| O(8)-Pr(2)  | 2.438(6) |
| O(13)-Pr(1) | 2.492(6) |
| O(14)-Pr(2) | 2.424(6) |
| O(19)-Pr(1) | 2.435(6) |
| O(20)-Pr(2) | 2.455(5) |
| O(25)-Pr(2) | 2.477(6) |
| O(25)-Pr(1) | 2.662(6) |
| O(26)-Pr(1) | 2.620(8) |
| O(31)-Pr(1) | 2.441(6) |
| O(31)-Pr(2) | 2.653(6) |
|             |          |

| O(32)-Pr(2)            | 2.532(7)   |
|------------------------|------------|
| O(7)-Pr(1)-O(19)       | 140.1(2)   |
| O(7)-Pr(1)-O(31)       | 147.03(19) |
| O(19)-Pr(1)-O(31)      | 72.06(19)  |
| O(7)-Pr(1)-O(13)       | 111.5(2)   |
| O(19)-Pr(1)-O(13)      | 73.5(2)    |
| O(31)-Pr(1)-O(13)      | 80.19(19)  |
| O(7)-Pr(1)-O(1)        | 74.3(2)    |
| O(19)-Pr(1)-O(1)       | 140.5(2)   |
| O(31)-Pr(1)-O(1)       | 79.7(2)    |
| O(13)-Pr(1)-O(1)       | 75.0(2)    |
| O(7)-Pr(1)-O(1W)       | 71.8(2)    |
| O(19)-Pr(1)-O(1W)      | 70.0(2)    |
| O(31)-Pr(1)-O(1W)      | 141.15(19) |
| O(13)-Pr(1)-O(1W)      | 81.4(2)    |
| O(1)-Pr(1)-O(1W)       | 127.3(2)   |
| O(7)-Pr(1)-O(26)       | 73.4(2)    |
| O(19)-Pr(1)-O(26)      | 81.7(2)    |
| O(31)-Pr(1)-O(26)      | 115.2(2)   |
| O(13)-Pr(1)-O(26)      | 145.0(2)   |
| O(1)-Pr(1)-O(26)       | 136.4(2)   |
| O(1W)-Pr(1)-O(26)      | 67.0(2)    |
| O(7)-Pr(1)-O(2)        | 73.87(18)  |
| O(19)-Pr(1)-O(2)       | 139.25(18) |
| O(31)-Pr(1)-O(2)       | 73.88(17)  |
| O(13)-Pr(1)-O(2)       | 121.6(2)   |
| O(1)- $Pr(1)$ - $O(2)$ | 49.53(18)  |
| O(1W)-Pr(1)-O(2)       | 144.1(2)   |
| O(26)-Pr(1)-O(2)       | 93.3(2)    |
| O(7)-Pr(1)-O(25)       | 109.7(2)   |
| O(19)-Pr(1)-O(25)      | 73.08(19)  |
| O(31)-Pr(1)-O(25)      | 66.80(18)  |
| O(13)-Pr(1)-O(25)      | 138.60(18) |
| O(1)-Pr(1)-O(25)       | 119.99(18) |
| O(1W)-Pr(1)-O(25)      | 108.9(2)   |
| O(26)-Pr(1)-O(25)      | 49.00(19)  |
| O(2)-Pr(1)-O(25)       | 73.38(18)  |
| O(20)-Pr(2)-O(25)      | 81.3(2)    |
| O(20)-Pr(2)-O(4W)      | 68.3(2)    |
| O(25)-Pr(2)-O(4W)      | 78.89(19)  |

| O(20)-Pr(2)-O(32) | 80.4(2)    |
|-------------------|------------|
| O(25)-Pr(2)-O(32) | 116.2(2)   |
| O(4W)-Pr(2)-O(32) | 143.0(2)   |
| O(20)-Pr(2)-O(3W) | 139.0(2)   |
| O(25)-Pr(2)-O(3W) | 134.35(19) |
| O(4W)-Pr(2)-O(3W) | 128.4(2)   |
| O(32)-Pr(2)-O(3W) | 66.5(2)    |
| O(20)-Pr(2)-O(2W) | 134.3(2)   |
| O(25)-Pr(2)-O(2W) | 71.37(19)  |
| O(4W)-Pr(2)-O(2W) | 136.4(2)   |
| O(32)-Pr(2)-O(2W) | 79.9(2)    |
| O(3W)-Pr(2)-O(2W) | 64.23(18)  |
| O(20)-Pr(2)-O(31) | 68.8(2)    |
| O(25)-Pr(2)-O(31) | 66.46(18)  |
| O(4W)-Pr(2)-O(31) | 127.79(18) |
| O(32)-Pr(2)-O(31) | 49.90(18)  |
| O(3W)-Pr(2)-O(31) | 103.51(19) |
| O(2W)-Pr(2)-O(31) | 66.87(18)  |

| O(1)-La(1)      | 2.514(2) |
|-----------------|----------|
| O(2)-La(2)      | 2.573(2) |
| O(7)-La(1)      | 2.492(2) |
| O(7)-La(2)      | 2.865(2) |
| O(8)-La(2)      | 2.595(2) |
| O(13)-La(1)     | 2.805(2) |
| O(14)-La(1)     | 2.615(2) |
| O(19)-La(2)     | 2.640(2) |
| O(20)-La(2)     | 2.840(2) |
| O(25)-La(1)     | 2.602(2) |
| O(26)-La(2)     | 2.492(2) |
| O(26)-La(1)     | 2.881(2) |
| O(31)-La(1)#2   | 2.568(2) |
| O(32)-La(2)     | 2.478(2) |
| O(37)-La(2)     | 2.611(2) |
| O(1W)-La(1)     | 2.689(2) |
| O(2W)-La(1)     | 2.573(2) |
| O(3W)-La(2)     | 2.587(2) |
| O(7)-La(1)-O(1) | 72.69(7) |

| O(7)-La(1)-O(2W)  | 77.19(8)  |
|-------------------|-----------|
| O(1)-La(1)-O(2W)  | 128.95(7) |
| O(7)-La(1)-O(25)  | 111.69(7) |
| O(1)-La(1)-O(25)  | 77.90(8)  |
| O(2W)-La(1)-O(25) | 76.28(8)  |
| O(7)-La(1)-O(14)  | 80.66(7)  |
| O(1)-La(1)-O(14)  | 71.15(7)  |
| O(2W)-La(1)-O(14) | 141.82(9) |
| O(25)-La(1)-O(14) | 141.42(8) |
| O(7)-La(1)-O(1W)  | 138.08(7) |
| O(1)-La(1)-O(1W)  | 65.50(7)  |
| O(2W)-La(1)-O(1W) | 132.92(8) |
| O(25)-La(1)-O(1W) | 62.83(7)  |
| O(14)-La(1)-O(1W) | 83.33(8)  |
| O(7)-La(1)-O(13)  | 123.66(7) |
| O(1)-La(1)-O(13)  | 103.21(7) |
| O(2W)-La(1)-O(13) | 127.81(7) |
| O(25)-La(1)-O(13) | 122.45(6) |
| O(14)-La(1)-O(13) | 47.63(6)  |
| O(1W)-La(1)-O(13) | 65.94(7)  |
| O(7)-La(1)-O(26)  | 64.73(7)  |
| O(1)-La(1)-O(26)  | 66.66(7)  |
| O(2W)-La(1)-O(26) | 63.43(7)  |
| O(25)-La(1)-O(26) | 47.05(6)  |
| O(14)-La(1)-O(26) | 131.33(6) |
| O(1W)-La(1)-O(26) | 99.84(7)  |
| O(13)-La(1)-O(26) | 165.53(6) |
| O(32)-La(2)-O(26) | 139.11(8) |
| O(2)-La(2)-O(20)  | 122.81(7) |
| O(3W)-La(2)-O(20) | 63.03(7)  |
| O(8)-La(2)-O(20)  | 130.02(6) |
| O(37)-La(2)-O(20) | 102.50(7) |
| O(19)-La(2)-O(20) | 47.10(6)  |
| O(32)-La(2)-O(7)  | 105.13(7) |
| O(26)-La(2)-O(7)  | 64.98(7)  |
| O(2)-La(2)-O(7)   | 66.99(7)  |
| O(3W)-La(2)-O(7)  | 126.20(7) |
| O(8)-La(2)-O(7)   | 47.24(6)  |
| O(37)-La(2)-O(7)  | 68.43(7)  |
| O(19)-La(2)-O(7)  | 128.85(6) |

| O(20)-La(2)-O(7)  | 170.06(6)  |
|-------------------|------------|
| O(32)-La(2)-O(2)  | 138.50(8)  |
| O(26)-La(2)-O(2)  | 76.84(7)   |
| O(32)-La(2)-O(3W) | 127.66(7)  |
| O(26)-La(2)-O(3W) | 79.20(7)   |
| O(2)-La(2)-O(3W)  | 66.67(8)   |
| O(32)-La(2)-O(8)  | 70.82(8)   |
| O(26)-La(2)-O(8)  | 112.19(7)  |
| O(2)-La(2)-O(8)   | 76.17(8)   |
| O(3W)-La(2)-O(8)  | 137.56(8)  |
| O(32)-La(2)-O(37) | 68.28(8)   |
| O(26)-La(2)-O(37) | 71.42(8)   |
| O(2)-La(2)-O(37)  | 132.94(7)  |
| O(3W)-La(2)-O(37) | 136.09(8)  |
| O(8)-La(2)-O(37)  | 84.63(8)   |
| O(32)-La(2)-O(19) | 85.06(8)   |
| O(26)-La(2)-O(19) | 74.80(7)   |
| O(2)-La(2)-O(19)  | 132.85(8)  |
| O(3W)-La(2)-O(19) | 71.55(8)   |
| O(8)-La(2)-O(19)  | 150.05(8)  |
| O(37)-La(2)-O(19) | 69.74(8)   |
| O(32)-La(2)-O(20) | 66.70(7)   |
| O(26)-La(2)-O(20) | 116.98(7)  |
| Complex 8         |            |
| O(1)-Eu(1)        | 2.393(3)   |
| O(7)-Eu(1)        | 2.522(4)   |
| O(8)-Eu(1)        | 2.755(4)   |
| O(14)-Eu(1)       | 2.359(4)   |
| O(1W)-Eu(1)       | 2.393(4)   |
| O(2W)-Eu(1)       | 2.396(4)   |
| O(3W)-Eu(1)       | 2.461(4)   |
| O(14)-Eu(1)-O(1W) | 73.27(17)  |
| O(14)-Eu(1)-O(1)  | 135.03(14) |
| O(1W)-Eu(1)-O(1)  | 139.94(15) |
| O(14)-Eu(1)-O(2W) | 104.1(2)   |
| O(1W)-Eu(1)-O(2W) | 71.49(16)  |
| O(1)-Eu(1)-O(2W)  | 73.58(15)  |
| O(14)-Eu(1)-O(3W) | 66.64(15)  |
| O(1W)-Eu(1)-O(3W) | 116.23(19) |
| O(1)-Eu(1)-O(3W)  | 70.10(14)  |

| O(2W)-Eu(1)-O(3W) | 72.86(17)  |
|-------------------|------------|
| O(14)-Eu(1)-O(7)  | 142.64(15) |
| O(1W)-Eu(1)-O(7)  | 70.73(16)  |
| O(1)-Eu(1)-O(7)   | 81.13(14)  |
| O(2W)-Eu(1)-O(7)  | 73.56(16)  |
| O(3W)-Eu(1)-O(7)  | 140.60(15) |
| O(14)-Eu(1)-O(8)  | 141.50(15) |
| O(1W)-Eu(1)-O(8)  | 108.61(15) |
| O(1)-Eu(1)-O(8)   | 68.36(12)  |
| O(2W)-Eu(1)-O(8)  | 112.97(16) |
| O(3W)-Eu(1)-O(8)  | 133.68(14) |
| O(7)-Eu(1)-O(8)   | 48.12(12)  |

| O(2)-Gd(1)        | 2.3888(13) |
|-------------------|------------|
| O(7)-Gd(1)        | 2.3520(15) |
| O(13)-Gd(1)       | 2.5139(14) |
| O(14)-Gd(1)       | 2.7702(15) |
| O(1W)-Gd(1)       | 2.4008(14) |
| O(2W)-Gd(1)       | 2.3959(15) |
| O(3W)-Gd(1)       | 2.4489(15) |
| O(7)-Gd(1)-O(2)   | 135.15(5)  |
| O(7)-Gd(1)-O(2W)  | 73.18(6)   |
| O(2)-Gd(1)-O(2W)  | 140.11(5)  |
| O(7)-Gd(1)-O(1W)  | 104.25(7)  |
| O(2)-Gd(1)-O(1W)  | 73.88(5)   |
| O(2W)-Gd(1)-O(1W) | 71.33(6)   |
| O(7)-Gd(1)-O(3W)  | 67.03(5)   |
| O(2)-Gd(1)-O(3W)  | 69.95(5)   |
| O(2W)-Gd(1)-O(3W) | 116.17(7)  |
| O(1W)-Gd(1)-O(3W) | 72.73(6)   |
| O(7)-Gd(1)-O(13)  | 142.33(5)  |
| O(2)-Gd(1)-O(13)  | 81.45(5)   |
| O(2W)-Gd(1)-O(13) | 70.65(6)   |
| O(1W)-Gd(1)-O(13) | 73.77(6)   |
| O(3W)-Gd(1)-O(13) | 140.66(5)  |
| O(7)-Gd(1)-O(14)  | 141.22(5)  |
| O(2)-Gd(1)-O(14)  | 68.13(4)   |
| O(2W)-Gd(1)-O(14) | 108.96(5)  |
| O(1W)-Gd(1)-O(14) | 113.16(6)  |
|                   |            |

| O(3W)-Gd(1)-O(14) | 133.35(5) |
|-------------------|-----------|
| O(13)-Gd(1)-O(14) | 48.33(4)  |

| O(1)-Gd(1)        | 2.5093(18) |
|-------------------|------------|
| O(2)-Gd(1)        | 2.4839(16) |
| O(7)-Gd(1)        | 2.4280(17) |
| O(8)-Gd(1)        | 2.4847(17) |
| O(9)-Gd(1)        | 2.5850(17) |
| O(10)-Gd(1)       | 2.4664(17) |
| O(1W)-Gd(1)       | 2.3678(16) |
| O(2W)-Gd(1)       | 2.3629(17) |
| O(2W)-Gd(1)-O(1W) | 86.27(6)   |
| O(2W)-Gd(1)-O(7)  | 145.09(6)  |
| O(1W)-Gd(1)-O(7)  | 126.65(6)  |
| O(2W)-Gd(1)-O(10) | 78.62(7)   |
| O(1W)-Gd(1)-O(10) | 72.88(6)   |
| O(7)-Gd(1)-O(10)  | 98.69(6)   |
| O(2W)-Gd(1)-O(2)  | 74.30(6)   |
| O(1W)-Gd(1)-O(2)  | 72.40(6)   |
| O(7)-Gd(1)-O(2)   | 122.58(6)  |
| O(10)-Gd(1)-O(2)  | 136.83(6)  |
| O(2W)-Gd(1)-O(8)  | 147.94(6)  |
| O(1W)-Gd(1)-O(8)  | 75.36(6)   |
| O(7)-Gd(1)-O(8)   | 52.95(5)   |
| O(10)-Gd(1)-O(8)  | 71.01(6)   |
| O(2)-Gd(1)-O(8)   | 122.58(6)  |
| O(2W)-Gd(1)-O(1)  | 126.68(6)  |
| O(1W)-Gd(1)-O(1)  | 80.91(6)   |
| O(7)-Gd(1)-O(1)   | 75.74(6)   |
| O(10)-Gd(1)-O(1)  | 142.37(6)  |
| O(2)-Gd(1)-O(1)   | 52.46(5)   |
| O(8)-Gd(1)-O(1)   | 76.62(6)   |
| O(2W)-Gd(1)-O(9)  | 77.43(6)   |
| O(1W)-Gd(1)-O(9)  | 123.61(6)  |
| O(7)-Gd(1)-O(9)   | 74.31(6)   |
| O(10)-Gd(1)-O(9)  | 51.17(5)   |
| O(2)-Gd(1)-O(9)   | 146.37(5)  |
| O(8)-Gd(1)-O(9)   | 91.00(5)   |
| O(1)-Gd (1)-O(9)  | 149.17(5)  |

| T / K | $\chi_{\rm T}$ / cm <sup>3</sup> mol <sup>-1</sup> | $\chi_{\rm S}$ / cm <sup>3</sup> mol <sup>-1</sup> | α        | τ/s      | R <sup>2</sup> |
|-------|--|--|----------|----------|----------------|
| 2     | 0.27946  | 0.02985  | 0.21233  | 0.01715  | 0.9994         |
| 2.2   | 0.25665  | 0.02781  | 0.20627  | 0.01386  | 0.99938        |
| 2.4   | 0.23876  | 0.02584  | 0.20874  | 0.01111  | 0.99595        |
| 2.6   | 0.21821  | 0.02545  | 0.20394  | 0.00859  | 0.99688        |
| 2.8   | 0.20312  | 0.02188  | 0.19521  | 0.00638  | 0.99604        |
| 3     | 0.18624  | 0.02421  | 0.15463  | 0.00488  | 0.99641        |
| 3.5   | 0.15928  | 0.02416  | 0.09371  | 0.00226  | 0.99648        |
| 4     | 0.14029  | 0.02336  | 0.06349  | 9.30E-04 | 0.99806        |
| 4.5   | 0.12639  | 0.00519  | 0.06569  | 3.37E-04 | 0.99874        |
| 5     | 0.11431  | 0.03046  | -0.03036 | 2.00E-04 | 0.99958        |
| 5.5   | 0.10465  | 0.03335  | -0.04992 | 9.95E-05 | 0.99936        |

**Table S4.** Best fitted parameters ( $\chi_T$ ,  $\chi_S$ ,  $\tau$  and  $\alpha$ ) with the extended Debye model for 1 at 2 kOe in the temperature range 2-5.5 K.

**Table S5.** Best fitted parameters ( $\chi_T$ ,  $\chi_S$ ,  $\tau$  and  $\alpha$ ) with the extended Debye model for **3** at 3.5 kOe in the temperature range 2-5 K.

| T / K | $\chi_{\rm T}$ / cm <sup>3</sup> mol <sup>-1</sup> | $\chi_{\rm S}$ / cm <sup>3</sup> mol <sup>-1</sup> | α       | τ / s    | R <sup>2</sup> |
|-------|--|--|---------|----------|----------------|
| 2     | 0.33078  | 0.01304  | 0.33891 | 0.00281  | 0.99901        |
| 2.2   | 0.30505  | 0.01184  | 0.33875 | 0.00242  | 0.99883        |
| 2.4   | 0.28053  | 0.01204  | 0.3256  | 0.00202  | 0.99914        |
| 2.6   | 0.26119  | 0.01275  | 0.30918 | 0.00169  | 0.99925        |
| 2.8   | 0.2436   | 0.01251  | 0.2885  | 0.00141  | 0.99948        |
| 3     | 0.22902  | 0.01247  | 0.28341 | 0.0012   | 0.99947        |
| 3.5   | 0.19918  | 0.01363  | 0.24809 | 7.79E-04 | 0.9998         |
| 4     | 0.17606  | 0.01614  | 0.19368 | 4.58E-04 | 0.9999         |
| 4.5   | 0.15816  | 0.01417  | 0.13373 | 2.46E-04 | 0.99989        |
| 5     | 0.14309  | 0.02573  | 0.06158 | 1.44E-04 | 0.99991        |