# Electronic supplementary information 

## for

# From square core to square opening: Structural diversity and magnetic properties of the oxo-bridged [Cr"IINb ${ }^{\mathrm{V}}$ ] complexes 

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Fig. S1 Final Rietveld refinement for powder sample 1. The experimental data are given in red, the calculated pattern in blue, while the difference between experimental and calculated curve is given below. The purple vertical marks represent the diffraction lines of $\left[\mathrm{Cr}_{2}(\text { phen })_{4}(\mu-\mathrm{O})_{4} \mathrm{Nb}_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{4}\right] \cdot 2 \mathrm{H}_{2} \mathrm{O}$.


c)

Fig. S2 The molecular structure with the atom-numbering scheme of: (a) tetranuclear unit [ $\mathrm{Cr}_{2}$ (phen) $)_{4}(\mu-\mathrm{O})_{4} \mathrm{Nb}_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{4}$ ] in 1; (b) tetranuclear unit [ $\mathrm{Cr}_{2}(\text { terpy })_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}(\mu-\mathrm{O})_{4} \mathrm{Nb}_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{4}$ ] in 2; (c) complex anion $\left.\left[\mathrm{Cr}_{2} \text { (terpy }\right)_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2}(\mu-\mathrm{O})_{2} \mathrm{Nb}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2}\right]$ and cation $\left[\mathrm{Cr}(\right.$ terpy $\left.)\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)\left(\mathrm{H}_{2} \mathrm{O}\right)\right]$ in 3.

Table S1 Selected bond distances ( A ) and angles ( ${ }^{\circ}$ ) for compounds [ $\mathrm{Cr}_{2}(\mathrm{phen})_{4}(\mu$ $\left.\mathrm{O}_{4} \mathrm{Nb}_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{4}\right] \cdot 2 \mathrm{H}_{2} \mathrm{O} \quad$ (1), $\left[\mathrm{Cr}_{2}(\text { terpy })_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}(\mu-\mathrm{O})_{4} \mathrm{Nb}_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)\right] \cdot 4 \mathrm{HO} \quad$ (2) and $\left[\mathrm{Cr}(\right.$ terpy $\left.)\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)\left(\mathrm{H}_{2} \mathrm{O}\right)\right]\left[\mathrm{Cr}_{2}(\text { terpy })_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2}(\mu-\mathrm{O})_{2} \mathrm{Nb}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2}\right] \cdot 3 \mathrm{H}_{2} \mathrm{O}$ (3)

| 1 |  | 2 |  | 3 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Nb1-01 | 1.782(5) | Nb1-01 | 1.787(2) | Nb1-O14 | 1.791(2) |
| Nb1-02 | 2.055(6) | Nb1-02 | 1.794(2) | Nb1-05 | 1.808(2) |
| Nb1-03 | 2.140(6) | Nb1-03 | 2.207(2) | Nb1-06 | 2.218(2) |
| Cr1-01 | 1.885(5) | Nb1-06 | 2.042(2) | Nb1-09 | 2.073(2) |
| Cr1-N1 | 2.069(6) | Nb1-07 | 2.202(2) | Nb1-010 | 2.152(2) |
| Cr1-N2 | 2.044(8) | Nb1-010 | 2.042(2) | Nb1-013 | 2.054(2) |
| O1-Nb1-02 | 100.3(3) | Cr1-01 ${ }^{\text {c }}$ | 1.908(2) | Cr1-N1 | 2.084(3) |
| O1-Nb1-03 | 91.9(3) | Cr1-02 | 1.912(2) | Cr1-N2 | 1.983(3) |
| O1-Nb1-01 ${ }^{\text {a }}$ | 102.2(3) | Cr1-011 | 1.987(2) | Cr1-N3 | 2.104(3) |
| O1-Nb1-02 ${ }^{\text {a }}$ | 87.9(3) | Cr1-N1 | 2.077(3) | Cr1-01 | 1.981(2) |
| O1-Nb1-03 ${ }^{\text {a }}$ | 159.3(3) | Cr1-N2 | 1.993(3) | Cr1-04 | 1.942(2) |
| O2-Nb1-03 | 74.5(2) | Cr1-N3 | 2.052(3) | Cr1-05 | 1.927(2) |
| O2-Nb1-02 ${ }^{\text {a }}$ | 167.1(3) | O1-Nb1-02 | 102.14(10) | Cr2-N4 | 2.090(3) |
| O2-Nb1-03 ${ }^{\text {a }}$ | 95.3(3) | O1-Nb1-010 | 96.85(10) | Cr2-N5 | 1.996(3) |
| O3-Nb3-03 ${ }^{\text {a }}$ | 79.1(3) | O2-Nb1-010 | 100.37(9) | Cr2-N6 | 2.078(3) |
| O1-Cr1-N1 | 88.5(2) | O1-Nb1-06 | 101.17(10) | Cr2-014 | 1.923(2) |
| O1-Cr1-N2 | 90.9(3) | O2-Nb1-06 | 95.29(9) | Cr2-015 | 1.962(3) |
| O1-Cr1-O1 ${ }^{\text {b }}$ | 93.0(3) | O10-Nb1-06 | 153.03(9) | Cr2-018 | 1.941(3) |
| O1-Cr1-N1 ${ }^{\text {b }}$ | 175.4(3) | O1-Nb1-07 | 167.01(9) | Cr3-019 | 1.975(3) |
| O1-Cr1-N2 ${ }^{\text {b }}$ | 95.3(3) | O2-Nb1-07 | 89.64(9) | Cr3-020 | 1.950(3) |
| N1-Cr1-N2 | 80.3(3) | O10-Nb1-07 | 75.39(9) | Cr3-023 | 1.932(3) |
| N1-Cr1-O1 ${ }^{\text {b }}$ | 175.4(3) | O6-Nb1-07 | 82.95(9) | Cr3-N7 | 2.086(3) |
| N1-Cr1-N1 ${ }^{\text {b }}$ | 90.3(2) | O1-Nb1-03 | 87.91(9) | Cr3-N8 | 1.986(3) |
| N1-Cr1-N2 ${ }^{\text {b }}$ | 93.3(3) | O2-Nb1-03 | 167.22(9) | Cr3-N9 | 2.058(4) |
| N2-Cr1-N2 ${ }^{\text {b }}$ | 171.0(3) | O10-Nb1-03 | 86.05(8) | O14-Nb1-05 | 103.86(10) |
| Nb1-O1-Cr1 | 170.4(4) | O6-Nb1-03 | 74.81(8) | O14-Nb1-013 | 102.57(10) |
|  |  | O7-Nb1-03 | 81.25(8) | O5-Nb1-013 | 91.14(10) |
|  |  | O1-Cr1-O2 ${ }^{\text {c }}$ | 91.46(9) | O14-Nb1-09 | 95.50(10) |
|  |  | 01-Cr1-011 ${ }^{\text {c }}$ | 177.37(10) | O5-Nb1-09 | 100.08(10) |
|  |  | O2-Cr1-011 | 90.08(10) | O13-Nb1-09 | 155.81(9) |
|  |  | O1-Cr1-N2 ${ }^{\text {c }}$ | 91.85(10) | O14-Nb1-010 | 90.87(10) |
|  |  | O2-Cr1-N2 | 176.66(10 | O5-Nb1-010 | 161.59(9) |
|  |  | O11-Cr1-N2 | 86.63(10) | O13-Nb1-010 | 74.68(9) |
|  |  | O1-Cr1-N3 ${ }^{\text {c }}$ | 89.39(10) | O9-Nb1-010 | 89.24(9) |
|  |  | O2-Cr1-N3 | 100.59(10) | O14-Nb1-06 | 165.76(10) |
|  |  | O11-Cr1-N3 | 92.42(10) | O5-Nb1-06 | 87.51(9) |
|  |  | N2-Cr1-N3 | 78.97(11) | O13-Nb1-06 | 85.48(9) |
|  |  | $\mathrm{O} 1-\mathrm{Cr} 1-\mathrm{N} 1^{\text {c }}$ | 89.61(10) | O9-Nb1-06 | 73.78(8) |
|  |  | O2-Cr1-N1 | 101.99(10) | O10-Nb1-06 | 79.84(9) |
|  |  | O11-Cr1-N1 | 87.99(10) | O5-Cr1-04 | 91.53(10) |
|  |  | N2-Cr1-N1 | 78.51(11) | O5-Cr1-01 | 173.53(10) |
|  |  | N3-Cr1-N1 | 157.42(11) | O4-Cr1-01 | 82.68(10) |
|  |  | $\mathrm{Nb1-O1-Cr1}{ }^{\text {c }}$ | 167.60(13) | O5-Cr1-N2 | 92.22(10) |
|  |  | Nb1-O2-Cr1 | 164.73(14) | O4-Cr1-N2 | 175.90(11) |
|  |  |  |  | O1-Cr1-N2 | 93.66(10) |
|  |  |  |  | O5-Cr1-N1 | 89.41(10) |
|  |  |  |  | O4-Cr1-N1 | 99.00(11) |


|  |  | O1-Cr1-N1 | 94.31(11) |
| :---: | :---: | :---: | :---: |
|  |  | N2-Cr1-N1 | 79.38(12) |
|  |  | O5-Cr1-N3 | 89.75(11) |
|  |  | O4-Cr1-N3 | 88.91(11) |
|  |  | O1-Cr1-N3 | 104.21(11) |
|  |  | N2-Cr1-N3 | 77.48(11) |
|  |  | N1-Cr1-N3 | 156.79(11) |
|  |  | O14-Cr2-018 | 93.97(11) |
|  |  | O14-Cr2-015 | 177.98(11) |
|  |  | O18-Cr2-015 | 84.02(12) |
|  |  | O14-Cr2-N5 | 94.53(11) |
|  |  | O18-Cr2-N5 | 71.41(12) |
|  |  | O15-Cr2-N5 | 87.49(12) |
|  |  | O14-Cr2-N6 | 90.62(11) |
|  |  | O18-Cr2-N6 | 102.28(13) |
|  |  | O15-Cr2-N6 | 89.58(11) |
|  |  | N5-Cr2-N6 | 78.83(14) |
|  |  | O14-Cr2-N4 | 89.97(10) |
|  |  | O18-Cr2-N4 | 100.60(12) |
|  |  | O15-Cr2-N4 | 90.63(11) |
|  |  | N5-Cr2-N4 | 78.22(13) |
|  |  | N6-Cr2-N4 | 157.02(13) |
|  |  | O23-Cr3-020 | 81.52(13) |
|  |  | O23-Cr3-019 | 175.08(13) |
|  |  | O20-Cr3-019 | 94.04(14) |
|  |  | O23-Cr3-N8 | 94.09(12) |
|  |  | O20-Cr3-N8 | 175.59(13) |
|  |  | O19-Cr3-N8 | 90.36(13) |
|  |  | O23-Cr3-N9 | 90.12(13) |
|  |  | O20-Cr3-N9 | 101.24(15) |
|  |  | O19-Cr3-N9 | 88.66(12) |
|  |  | N8-Cr3-N9 | 79.18(15) |
|  |  | O23-Cr3-N7 | 93.09(12) |
|  |  | O20-Cr3-N7 | 101.06(14) |
|  |  | O19-Cr3-N7 | 89.83(12) |
|  |  | N8-Cr3-N7 | 78.58(15) |
|  |  | N9-Cr3-N7 | 157.69(15) |
|  |  | Nb1-O5-Cr1 | 156.80(13) |
|  |  | Nb1-O14-Cr2 | 163.81(15) |

${ }^{a}$ Symmetry operator: (i) $y, x, 2-z$
${ }^{\text {b }}$ Symmetry operator: (ii) $1-y, 1-x, 2-z$
${ }^{c}$ Symmetry operator: (ii) $1-x,-y, 1-z$


Fig. S3 The one-dimensional hydrogen-bonding pattern in the crystal packing of $\left[\mathrm{Cr}_{2}(\mathrm{phen})_{4}(\mu-\right.$ $\left.\mathrm{O})_{4} \mathrm{Nb}_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{4}\right] \cdot 2 \mathrm{H}_{2} \mathrm{O}(1)$.


Fig. S4 Full interaction map showing interaction preferences of the tetranuclear $\left[\mathrm{Cr}_{2}(\mathrm{phen})_{4}(\mu-\right.$ $\left.\mathrm{O})_{4} \mathrm{Nb}_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{4}\right]$ unit in 1.

Table S2 Hydrogen-bonding geometry in compounds 1-3. Interatomic distances involving the water molecules without located hydrogen atoms are given.

| Compound | $D-\mathrm{H} \cdots \mathrm{A}$ | D-H/Å | H $\cdots$ / $/ \AA$ | $D \cdots A / \AA$ | $D-H \cdots A /{ }^{\circ}$ | Symm. op. on $A$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | O6-H6A…04 | 0.8(2) | 2.4(6) | 2.938(14) | 123(1) | $x, y,-1+z$ |
| 2 | O11-H11A $\cdots$ O4 | 0.851(18) | 1.809(18) | 2.659(3) | 178(4) | $3 / 2-x,-1 / 2+y, 1 / 2-z$ |
|  | 011-H11B $\cdots 08$ | 0.84(3) | 1.89(2) | 2.688(3) | 158(2) | $2-x,-y, 1-z$ |
|  | O12-H12A…05 | 0.87(2) | 2.17(2) | 3.022(4) | 167(3) | $x, y, z$ |
|  | O12-H12B..O13 | 0.87(2) | 1.95(2) | 2.789(5) | 163(2) | $x, y, z$ |
|  | O13-H13A...07 | 0.86(2) | 2.29(2) | 3.108(4) | 159(3) | $x, y, z$ |
|  | O13-H13B $\cdots$. ${ }^{\text {a }}$ | 0.857(11) | 2.196(15) | 3.025(4) | 163(3) | $3 / 2-x,-1 / 2+y, 1 / 2-z$ |
| 3 | O19-H19A $\cdots$ - ${ }^{\text {O }}$ | 0.84(3) | 1.92(4) | 2.754(4) | 179(5) | $1+x, y, z$ |
|  | O19-H19B $\cdots$ O7 | 0.84(3) | 1.91(2) | 2.740(4) | 166(4) | $1-x,-y, 1-z$ |
|  | 024...022 |  |  | 2.789(16) |  | $x,-1+y, z$ |
|  | 024...011 |  |  | 2.906(17) |  | $x, y, z$ |
|  | 025..03 |  |  | 2.819(11) |  | $x, y, z$ |
|  | 025..015 |  |  | 2.957(10) |  | $-1+x, y, z$ |
|  | 026..02 |  |  | 2.847(8) |  | $-x, 1+y,-z$ |
|  | 026..025 |  |  | 2.904(14) |  | $-x, 1+y,-z$ |



Fig. S5 Final Rietveld refinement for powder sample of 2. The experimental data are given in red, the calculated pattern in blue, while the difference between experimental and calculated curve is given below. The green vertical marks represent the diffraction position of $\left[\mathrm{Cr}_{2}(\text { terpy })_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}(\mu-\right.$ $\left.\mathrm{O})_{4} \mathrm{Nb}_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{4}\right] \cdot 4 \mathrm{H}_{2} \mathrm{O}$.


Fig. S6 The three-dimensional hydrogen-bonding pattern in the crystal packing of $\left.\left[\mathrm{Cr}_{2} \text { (terpy }\right)_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}(\mu-\mathrm{O})_{4} \mathrm{Nb}_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)\right] \cdot 4 \mathrm{H}_{2} \mathrm{O}(2)$.


Fig. S7 The hydrogen bonding pattern in the crystal packing of $\left[\mathrm{Cr}(\right.$ terpy $\left.)\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)\left(\mathrm{H}_{2} \mathrm{O}\right)\right]\left[\mathrm{Cr}_{2}(\text { terpy })_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2}(\mu-\mathrm{O})_{2} \mathrm{Nb}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2}\right] \cdot 3 \mathrm{H}_{2} \mathrm{O}$ (3).


Fig. S8 The $\pi$-stacked tetramers in $\left[\mathrm{Cr}(\right.$ terpy $\left.)\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)\left(\mathrm{H}_{2} \mathrm{O}\right)\right]\left[\mathrm{Cr}_{2}(\text { terpy })_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2}(\mu-\mathrm{O})_{2} \mathrm{Nb}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2}\right] \cdot 3 \mathrm{H}_{2} \mathrm{O}$ (3).

Table S3 Geometric parameters of the aromatic stacking interactions in compound $\mathbf{3}$

| Compound | $\mathrm{Cg}(i) \cdots \mathrm{Cg}(\mathrm{j})$ | $\operatorname{Cg}(i) \cdots \operatorname{Cg}(j) / \AA^{a}$ | $\alpha /^{\circ}$ | $B /{ }^{\circ} \mathrm{C}$ | $\mathrm{Cg}(i) \cdots$ plane $[\mathrm{Cg}(\mathrm{j})] / \AA^{d}$ | Symmetry operator |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | $(\mathrm{N} 2 \rightarrow \mathrm{C} 10) \cdots(\mathrm{N} 3 \rightarrow \mathrm{C} 15)$ | 3.647(3) | 0.9(2) | 22.0 | $3.3748(16)$ | $-x,-y,-z$ |
|  | $(\mathrm{N} 6 \rightarrow \mathrm{C} 30) \cdots(\mathrm{N} 7 \rightarrow$ C35 $)$ | 3.695(4) | 5.8(3) | 20.9 | 3.501(2) | $1-x, 1-y, 1-z$ |

${ }^{\mathrm{a}} \mathrm{Cg}=$ centre of gravity of the aromatic ring. ${ }^{\mathrm{b}} \alpha=$ angle between the planes of two aromatic rings. ${ }^{\mathrm{c}} 8=$ angle between the $\mathrm{Cg} \cdots \mathrm{Cg}$ line and the normal to the plane of the first aromatic ring

Table S4 Intra and shortest intermolecular distances ( $\AA$ ) between metal centres in compounds 1-3

| Compound | $[\mathrm{Cr} \cdots \mathrm{Cr}]_{\text {intra }}$ | $\mathrm{Cr}-\mathrm{O}-\mathrm{Nb}-\mathrm{O}-\mathrm{Cr}$ | $\mathrm{Cr} \cdots \mathrm{Cr}$ | $\mathrm{Cr} \cdots \mathrm{Nb}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 5.359 | 7.332 | 10.346 | 8.214 |
| $\mathbf{2}$ | 5.411 | 7.400 | 9.121 | 7.369 |
| $\mathbf{3}$ | 6.089 | 7.407 | 6.936 | 8.025 |



Fig. $\mathbf{S 9}$ Temperature dependence of the molar magnetic susceptibility for compound 3. The red solid line represents the best-fitted model curve.



Fig. S10 Overlayered relaxed structures of 1-3 calculated with three different density functionals: PBE, ${ }^{1} \mathrm{GGA}+\mathrm{U},{ }^{2}$ and vdW-DF-cx. ${ }^{3}$ All three functionals predict very similar geometries with only subtle differences showing that it is not very important to account for vdW forces for these compounds.


Fig. S11 Isosurface plots (iso value is 0.003 electrons/a.u. ${ }^{3}$ ) of magnetic polarization density (difference of spin up and spin down electron density) for compound 1: (a) antiferromagnetic solution obtained with GGA+U; ${ }^{2}$ (b) ferromagnetic solution obtained with $G G A+U ;{ }^{2}$ (c) antiferromagnetic solution obtained with PBE; ${ }^{14}$ (d) ferromagnetic solution obtained with PBE; ${ }^{1}$ (e) antiferromagnetic solution obtained with vdW-DF-cx; ${ }^{3}$ f) ferromagnetic solution obtained with vdW-DF-cx. ${ }^{3}$


Fig. S12 Isosurface plots (iso value is 0.01 electrons/a.u. ${ }^{3}$ ) of magnetic polarization density (difference of spin up and spin down electron density) for compound 1: (a) antiferromagnetic solution obtained with $G G A+U ;^{2}$ (b) ferromagnetic solution obtained with GGA+U; ${ }^{2}$ (c) antiferromagnetic solution obtained with PBE; ${ }^{1}(\mathrm{~d})$ antiferromagnetic solution obtained with vdW-DF-cx. ${ }^{3}$

Table S6 Magnetic and structural properties obtained from DFT calculations

| Compound | 1 |  |  | 2 |  |  | 3 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | PBE | $U=3.5 \mathrm{eV}$ | vdW-DF-cx | PBE | $U=3.5 \mathrm{eV}$ | vdW-DF-cx | PBE | $U=3.5 \mathrm{eV}$ | vdW-DF-cx |
| $\Delta E(\mathrm{mV})$ | -52.11 | -11.02 | -65.75 | -53.09 | -12.73 | -61.26 | -33.86 | -11.06 | -40.09 |
| $J\left(\mathrm{~cm}^{-1}\right)$ | -5.79 | -1.22 | -7.31 | -5.90 | -1.41 | -6.81 | -3.76 | -1.23 | -4.45 |
| $\mathrm{Cr}-\mathrm{O}-\mathrm{Nb}-\mathrm{O}-\mathrm{Cr}(\mathrm{Å})$ | 7.41 | 7.47 | 7.38 | 7.41 | 7.48 | 7.40 | 7.43 | 7.50 | 7.41 |
| $\mathrm{Cr} \cdots \mathrm{Cr}(\mathrm{A})$ | 5.42 | 5.45 | 5.37 | 5.44 | 5.48 | 5.41 | 6.20 | 6.23 | 6.20 |
| $\mathrm{Cr}-\mathrm{O}-\mathrm{Nb}$ (deg) | 171.4 | 170.7 | 171.5 | 168.5 | 167.1 | 168.7 | 155.7 | 155.3 | 155.3 |
| $\mathrm{Cr}-\mathrm{O}-\mathrm{Nb} 2$ (deg) | 171.8 | 171.2 | 172.0 | 165.0 | 163.6 | 165.7 | 168.1 | 169.0 | 168.2 |

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