

Electronic Supplementary Information for:

Multicomponent diffusion coefficients from microfluidics using Raman microspectroscopy

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S1 Pure component data

Table S1 Used chemicals with supplier and purity

	supplier	description	purity in %
cyclohexane	VWR	Spectronorm	99.7
toluene	VWR	Spectronorm	99.8
methanol	VWR	Spectronorm	99.9
acetone	Merck Millipore	Uvasol	99.9
1-propanol	Merck	LiChrosolv	99.8
1-chlorobutane	Merck	LiChrosolv	99.8
heptane	Bernd Kraft	p.a.	99

Table S2 Molar volumes of pure components

	V_i^0 in $\text{m}^3 \text{mol}^{-1}$	reference
cyclohexane	108.8×10^{-6}	1
toluene	106.9×10^{-6}	2
1-propanol	75.17×10^{-6}	3
1-chlorobutane	105.2×10^{-6}	4
heptane	147.4×10^{-6}	5

S2 Reparameterization for the estimation procedure of ternary diffusion coefficients

For ternary mixtures, the following constraints impose positive definiteness of the diffusion coefficient \mathbf{D}^V :⁶

$$D_{11} + D_{22} > 0 \quad (\text{S1})$$

$$D_{11}D_{22} - D_{12}D_{21} > 0 \quad (\text{S2})$$

$$(D_{11} - D_{22})^2 + 4D_{12}D_{21} > 0 \quad (\text{S3})$$

In practice, many solvers employ infeasible path strategies and allow violations of constraints during the iterations. We employed the reparameterization proposed by Bardow *et al.*:⁷

$$\theta_1 = D_1^\dagger, \theta_2 = D_2^\dagger, \theta_3 = D_{11} - D_{22}, \text{ and } \theta_4 = D_{12}. \quad (\text{S4})$$

The inverse transformation is performed according to

$$D_{11} = \frac{\theta_1 + \theta_2 + \theta_3}{2}, D_{22} = \frac{\theta_1 + \theta_2 - \theta_3}{2}, D_{21} = \frac{(\theta_1 - \theta_2)^2 - \theta_3^2}{4\theta_4}, \text{ and } D_{12} = \theta_4. \quad (\text{S5})$$

With simple constraints on θ_1 and θ_2 , the constraints (S1) - (S3) are trivially satisfied.⁷ In practical applications, division by the unknown parameter θ_4 to compute D_{21} does not lead to numerical difficulties in our experience.

S3 Cyclohexane + toluene

The influence of the temperature inaccuracy on the diffusion coefficient is expected to be in the same order of magnitude as the standard deviation $\sigma(D)$ based on the correlation

$$D(T) = D(T_0) \frac{T}{T_0} \frac{\eta_{AB}(x, T_0)}{\eta_{AB}(x, T)} \quad (\text{S6})$$

between the diffusion coefficient D , absolute temperature T and viscosity η .⁸ The index 0 indicates the reference conditions. For a temperature accuracy of ± 0.5 K, a relative error of the diffusion coefficient of 0.8 % is expected according to the temperature correlation (S6) and the viscosities of cyclohexane + toluene listed in Table S3.

Table S3 Expected influence of temperature on the diffusion coefficient and the viscosity of cyclohexane + toluene at $x_{\text{cyclohexane}} = 0.6$. Viscosities were interpolated based on the data published by Silva *et al.*⁹ The diffusion coefficient at 25 °C was published by Sanni *et al.*¹⁰

T in °C	η in mPas	D in $10^{-9} \text{ m}^2 \text{ s}^{-1}$	comment on D
24.5	0.635	1.753	eq. S6
25	0.631	1.767	Reference ¹⁰
25.5	0.627	1.781	eq. S6

S4 1-Propanol + 1-chlorobutane + heptane

Table S4 Composition of the experiments with 1-propanol + 1-chlorobutane + heptane in mol%

	\bar{x}	series A		series B	
		x_{left}	x_{right}	x_{left}	x_{right}
1-propanol	33.3	35.8	30.8	35.8	30.8
1-chlorobutane	33.3	35.8	30.8	30.8	35.8
heptane	33.3	28.4	38.4	33.4	33.4

Table S5 Measured diffusion coefficient for 1-propanol + 1-chlorobutane + heptane at $x_{1\text{-propanol}} = x_{1\text{-chlorobutane}} = 33.3 \text{ mol\%}$ and $25 \text{ }^\circ\text{C}$ by microfluidic experiment in this work with standard deviation $\sigma(\mathbf{D}^V)$ from repeated experiments in comparison to K ashammer *et al.*¹¹. The quality of fit for the diffusion coefficient is given as RMSE_{fit} .

	D_{11}	D_{12}	D_{21}	D_{22}	RMSE_{fit}
	in $1 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$				in mol%
$n_{\text{exp}} = 1^{\text{a}}$	0.746 ± 0.202	-0.552 ± 0.474	0.423 ± 0.120	2.571 ± 0.263	0.29
$n_{\text{exp}} = 2^{\text{b}}$	0.998 ± 0.025	-0.279 ± 0.044	0.311 ± 0.027	2.521 ± 0.050	0.29
$n_{\text{exp}} = 9^{\text{c}}$	1.017	-0.236	0.310	2.516	0.29
literature	1.033 ± 0.016	-0.174 ± 0.025	0.255 ± 0.012	2.463 ± 0.017	

^a estimated from nine separate experiments

^b estimated from all combinations of two experiments, one from series A and series B each

^c estimated from all experiments simultaneously, four from series A and five from series B each. No standard deviations from repeated experiments are available, but standard deviations are expected to be less than for $n_{\text{exp}} = 2$ as more data was used.

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