## Supporting Information

## Mapping of Bernal and non-Bernal

## Stacking Domains in Bilayer Graphene

## Using Infrared Nanoscopy

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## A. Examples of IR-sSNOM images of bilayer graphene (BLG)



Figure S1. Examples of sSNOM intensity $\left(\left|s_{2}\right|^{2}\right)$ and phase ( $\phi_{2}$ ) images of BLG obtained with IR light at $\omega_{1}=0.366 \mathrm{eV}$ and $\omega_{2}=0.124 \mathrm{eV}$. The scale bars correspond to $2 \mu \mathrm{~m}$. Last column shows the stacking angles $(\theta)$ of AA'-BLG in each image, estimated from the Raman spectra (see Supporting Information-B).
B. Raman spectroscopy on AB and AA'-stacked bilayer graphene


Figure S2. (a) The Raman spectra of a BLG on $\mathrm{SiO}_{2} / \mathrm{Si}$ substrate (excitation wavelength of $\lambda_{\mathrm{ex}}=$ 514.5 nm ) obtained from the D1 $(\beta)$ and $\mathrm{D} 2(\alpha)$ regions of BLG shown in Figure 2c of main text). (b) Lineshape analysis of 2D peak of $\beta$ (D1), showing characteristic lineshape for AB-BLG.

We have correlated the sSNOM contrasts to the Raman spectroscopic analysis results. Spectra (around G and 2D peaks) of BLG obtained from the b (D1 region) and a (D2 region) in Figure 2c.

The peak intensity ratios of G and 2D peaks of BLG $\left(I_{G} / I_{2 D}\right)$, and the lineshapes of 2Dpeaks are used to assess the stacking orders in BLG. We estimated the stacking angle and stacking order in BLG from the peak height ratio $\left(I_{\mathrm{G}} / I_{2 \mathrm{D}}\right)$, based on Chen et al's report, in which they correlated the stacking angle and the $I_{\mathrm{G}} / I_{2 \mathrm{D}}$. In particular, the AB-BLG has the fixed ratio of $I_{\mathrm{G}} / I_{2 \mathrm{D}} \approx 1^{1-3}$. For AB-BLG, the 2D peaks show characteristic shoulders in 2D peaks, which can be decomposed into four peaks, representing four-step Stokes-Stokes double-resonance Raman (DRR) scattering ${ }^{4}$.

Detailed 2D-lineshapes of AB-BLG show significant differences among reported results ${ }^{1,}$ ${ }^{3,5,6}$ possibly due to the differences in the doping levels of BLG. The most evident feature that distinguishes AB and $\mathrm{AA}^{\prime}$ '-BLG is simply the width of 2D peak. For a $\mathrm{AA}^{\prime}$ '-BLG with stackingangle $\theta=0 \sim 10^{\circ}$, additional peak at $1625 \mathrm{~cm}^{-1}$ (called R'-peak) appears, which provides additional information on stacking angle. For the particular BLG shown in Figure 2 in main text, the $I_{\mathrm{G}} / I_{2 \mathrm{D}}$, 2D-peak lineshape, and presence / absence of R'-peak (see Figure S2) indicates the existence of AB-BLG and AA'-BLG with $\theta=8 \pm 1^{\circ}$. In the last column of Figure S 1 , we have provided stacking angles of several other AA'-BLG domains we have examined with sSNOM.

## C. Point-dipole modeling for IR s-SNOM

The details of point-dipole sSNOM model can be found in the reports by Aizpurua et $\mathrm{al}^{7}$ and Kim et al ${ }^{8}$. Briefly, the tip-end, which is modeled as a nanosphere has a polarizability of:

$$
\begin{equation*}
\alpha=4 \pi a^{3}\left(\varepsilon_{t i p}-\varepsilon_{1}\right) /\left(\varepsilon_{t i p}+2 \varepsilon_{1}\right), \tag{1}
\end{equation*}
$$

where the $\varepsilon_{t i p}$, and $\varepsilon_{1}$ are dielectric constants of tip-end, and vacuum, respectively. For the calculation of sSNOM amplitude, we evaluate the Fresnel coefficient of graphene $/ \mathrm{SiO}_{2} / \mathrm{Si}$ sample:

$$
\begin{equation*}
r_{p}=\frac{Z_{1} C-Z_{2} S-\sigma_{r} \pi \alpha C}{Z_{1} C+Z_{2} S+\sigma_{r} \pi \alpha C}, \tag{2}
\end{equation*}
$$

where $C=\cos \varphi-i \frac{Z_{2}}{Z_{1}} \sin \varphi, S=-i \sin \varphi+\frac{Z_{2}}{Z_{1}} \cos \varphi$ and $\varphi=k_{2 z} d$. The $Z_{i}=\frac{2 \pi}{\lambda} \cdot \frac{\varepsilon_{i}}{k_{i z}}$ are the admittance of $i=1$ (vacuum), $2\left(\mathrm{SiO}_{2}\right)$, and $3(\mathrm{Si})$ media, and the $k_{i z}$ are the out-of-plane wave-
vectors in $i^{\prime}$ 'h media: $k_{i z}(q)=\sqrt{\varepsilon_{i}(\omega / c)^{2}-q^{2}}\left(\operatorname{Im}\left[k_{i z}\right]>0\right.$ and $\left.\operatorname{Re}\left[k_{i z}\right]>0\right)$ where $q$ and $\omega$ are the in-plane photon momentum vector and angular frequency of light, respectively. The $\sigma_{r}$ is the inplane optical conductivity of graphene, $\sigma$, normalized by unit conductivity, $\sigma_{0}=c \alpha / 4$. The $\alpha$ is the fine-structure constant. Overall far-field scattering amplitude is calculated as:

$$
\begin{equation*}
\vec{E}_{\text {scat }} \propto \vec{\alpha} \cdot \vec{E}_{\text {inc }}\left(1-\ddot{\alpha} \cdot \vec{G}\left(\left\{\sigma, \varepsilon_{i}\right\}\right)\right)^{-1}, \tag{3}
\end{equation*}
$$

where $\vec{E}_{\text {inc }}$ is the incident electric field. The $\vec{G}$ is the Green dyadic operator, which is a function of optical conductivities of graphene $(\sigma)$, and dielectric constants of substrate materials $\left(\varepsilon_{i}\right)$. In the s-SNOM measurement, the signal is processed through a lock-in amplifier. The transferfunction between the $E_{\text {scat }}$ and the demodulated signal $s_{n}$ is:

$$
\begin{equation*}
s_{n}=\left|s_{n}\right| e^{i \phi_{n}}=\frac{1}{2 \pi} \int_{0}^{2 \pi} E_{\text {scat }, p}(z+\delta z \cos \psi) e^{i n \psi} d \psi, \tag{4}
\end{equation*}
$$

where z and $\delta z$ are average tip-sample distance, and the amplitude of vertical tip-oscillation, respectively.

In the numerical sSNOM modeling, dielectric constant of $\mathrm{SiO}_{2}$ and Si is obtained by Sellmeier equations. ${ }^{9}$. The tip (PtIr) is made of an alloy of Pt: $\mathrm{Ir}=70: 30$. In the model, the tip is assumed to be a nanosphere with pure Pt with $\varepsilon=-144+75 \mathrm{i}$ at 0.366 eV and $-1324+916 \mathrm{i}$ at 0.124 $\mathrm{eV}^{10,11}$. In the model, the tip is assumed to be a nanosphere with an effective radius of $a$, and this does not necessarily reflect the actual radius of curvature of the tip-end. As such, we treat the radius of curvature (a), average tip-sample distance ( $z_{0}$ ), and tip-oscillation amplitude ( $\delta z$ ) as fitting parameters. The tip parameters are chosen such that it gives the best match to the
experimental sSNOM intensities of AB-BLG at $\omega_{1}$ and $\omega_{2}$, and the same parameters are used for the calculation of sSNOM intensities of AA-BLG at the two photon energies. For the model calculation shown in main text, we use tip radius as 20 nm , minimum tip-sample distance as 12 nm and tip oscillation amplitude as 35 nm .

## D. Intensity and phase contrasts of sSNOM images of BLG



Figure S3. 2-dimensional intensity-phase ( $\left|s_{2}\right|^{2}$ vs $\phi_{2}$ ) histograms of sSNOM images (Figure S1i~1) at $\omega_{1}$ and $\omega_{2}$ frequencies, along with sSNOM model of AB-BLG and AA-BLG (red dots). The intensity and phase contrasts of AB-BLG domain can be satisfactorily reproduced by the model, whereas the phase contrasts of AA'-BLG cannot be reproduced by the model that is based on the optical conductivity of AA-BLG.

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