

In the case of perovskite materials, the following parameters can be used as reliable polyhedra deformation indicators [i-ii]:

Distortion index  $D$ :

$$D = \frac{1}{n} \sum_{i=1}^n \frac{|l_i - l_{av}|}{l_{av}}$$

where  $l_i$  is the distance from the central atom to the  $i^{\text{th}}$  coordinating atom, and  $l_{av}$  is the average bond length.

Quadratic elongation  $\langle \lambda \rangle$ :

$$\langle \lambda \rangle = \frac{1}{n} \sum_{i=1}^n \left( \frac{l_i}{l_0} \right)^2$$

where  $l_0$  is a bond length in a regular polyhedron of the same volume and thus  $\langle \lambda \rangle$  is a dimensionless parameter, a quantitative measure of polyhedral distortion independent of its effective size.

Bond angle variance  $\sigma^2$ :

$$\sigma^2 = \frac{1}{m-1} \sum_{i=1}^m (\phi_i - \phi_0)^2$$

where  $m$  is a number of bond angles,  $\phi_i$  is  $i^{\text{th}}$  bond angle and  $\phi_0 = 90^\circ$  (ideal bond angle in regular octahedron).

Effective coordination number  $ECoN$ :

$$ECoN = \sum_i w_i; \quad w_i = \exp \left[ 1 - \left( \frac{l_i}{l_{av}} \right)^6 \right]; \quad l_{av} = \frac{\sum_i l_i \exp[1 - (l_i / l_{min})^6]}{\sum_i \exp[1 - (l_i / l_{min})^6]}$$

where  $w_i$  is  $i^{\text{th}}$  bond weight,  $l_{av}$  is weighted average bond length and  $l_{min}$  is the smallest bond length in the coordination octahedron.

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[i] W. H. Baur, *Acta Crystallogr., Sect. B: Struct. Sci.*, 1974, **30**, 1195.

[ii] R. Hoppe, *Z. Kristallogr.*, 1979, **150**, 23.

correspond to spin-up, spin-down and average effective masses).

<b>SrTiO<sub>3</sub></b>		<b><i>h</i> (up / dn / average)</b>					<b><i>e</i> (up / dn / average)</b>				
<b>R → <math>\Gamma</math></b>	<b>R → X</b>	<b><math>\Gamma</math> → M</b>	<b><math>\Gamma</math> → R</b>	<b><math>\Gamma</math> → X</b>							
(-0.607 / -0.607 / -0.607)	(-0.828 / -0.828 / -0.828)	(0.38 / 0.38 / 0.38)	(0.628 / 0.628 / 0.628)	(0.352 / 0.352 / 0.352)							
(-0.608 / -0.608 / -0.608)	(-1.015 / -1.015 / -1.015)	(0.504 / 0.504 / 0.504)	(0.522 / 0.522 / 0.522)	(0.352 / 0.352 / 0.352)							
(-1.511 / -1.511 / -1.511)	(-2.756 / -2.756 / -2.756)	(0.66 / 0.66 / 0.66)	(0.499 / 0.499 / 0.499)	(5.464 / 5.464 / 5.464)							
<b>SrTi<sub>0.98</sub>Nb<sub>0.02</sub>O<sub>3</sub></b>											
<b>Z → <math>\Gamma</math></b>	<b>Z → R</b>	<b><math>\Gamma</math> → M</b>	<b><math>\Gamma</math> → Z</b>	<b><math>\Gamma</math> → X</b>							
(-0.905 / -0.905 / -0.905)	(-0.799 / -0.799 / -0.799)	(0.384 / 0.384 / 0.384)	(0.387 / 0.387 / 0.387)	(0.344 / 0.344 / 0.344)							
(-0.938 / -0.937 / -0.938)	(-0.799 / -0.799 / -0.799)	(0.618 / 0.618 / 0.618)	(0.387 / 0.387 / 0.387)	(0.346 / 0.346 / 0.346)							
(-6.341 / -6.442 / -6.391)	(-14.414 / -15.266 / -14.84)	(0.859 / 0.859 / 0.859)	(2.219 / 2.32 / 2.27)	(5.511 / 5.621 / 5.566)							
<b>SrTi<sub>0.97</sub>Nb<sub>0.03</sub>O<sub>3</sub></b>											
<b>M → <math>\Gamma</math></b>	<b>M → X</b>	<b><math>\Gamma</math> → M</b>	<b><math>\Gamma</math> → Z</b>	<b><math>\Gamma</math> → X</b>							
(-0.943 / -0.943 / -0.943)	(-0.823 / -0.823 / -0.823)	(0.405 / 0.405 / 0.405)	(0.372 / 0.372 / 0.372)	(0.365 / 0.365 / 0.365)							
(-1.049 / -1.051 / -1.05)	(-0.826 / -0.826 / -0.826)	(0.608 / 0.609 / 0.609)	(0.372 / 0.372 / 0.372)	(0.365 / 0.372 / 0.369)							
(-2.777 / -2.798 / -2.788)	(-15.599 / -12.871 / -14.235)	(0.737 / 0.752 / 0.745)	(4.629 / 4.979 / 4.804)	(5.324 / 4.208 / 4.766)							