

Supporting Information

BaCu₂M^{IV}Q₄ (M^{IV} = Si, Ge, and Sn; Q = S, Se): synthesis, crystal structures, optical performances and theoretical calculations

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Table S1(b) Atomic coordinates ($\times 10^4$), equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for $\text{BaCu}_2\text{GeSe}_4$. $U(\text{eq})$ is defined as one third of the trace of the orthogonalized U_{ij} tensor.

Table S1(c) Atomic coordinates ($\times 10^4$), equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for $\text{BaCu}_2\text{GeSe}_4$. $U(\text{eq})$ is defined as one third of the trace of the orthogonalized U_{ij} tensor.

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Fig. S2(a) The IR spectrum of as-synthesized $\text{BaCu}_2\text{SiSe}_4$.

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Fig. S5(b) The electronic structure of BaCu₂GeS₄.

Fig. S5(c) The electronic structure of BaCu₂GeSe₄.

Fig. S5(d) The electronic structure of BaCu₂SnSe₄.

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Fig. S6(b) The PDOS of BaCu₂GeS₄.

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Fig. S7(a) SHG density of BaCu₂GeS₄.

Fig. S7(b) SHG density of BaCu₂GeSe₄.

Fig. S7(c) SHG density of BaCu₂SiSe₄.

Fig. S7(d) SHG density of BaCu₂SnSe₄.

Table S1(a) Atomic coordinates ($\times 10^4$), equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for $\text{BaCu}_2\text{SiSe}_4$. $U(\text{eq})$ is defined as one third of the trace of the orthogonalized U_{ij} tensor.

Atoms	Wyck.	x	y	z	$U(\text{eq})$	BVS
Ba(1)	3a	5496(1)	10000	6667	14(1)	2.46
Cu(1)	6c	9203(2)	5863(2)	5767(1)	23(1)	0.85
Se(1)	6c	6748(1)	7671(1)	8276(1)	12(1)	1.99
Se(2)	6c	10283(1)	5168(1)	7220(1)	12(1)	2.06
Si(1)	3b	10000	7165(5)	8333	9(1)	3.94

Table S1(b) Atomic coordinates ($\times 10^4$), equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for $\text{BaCu}_2\text{GeS}_4$. $U(\text{eq})$ is defined as one third of the trace of the orthogonalized U_{ij} tensor.

Atoms	Wyck	x	y	z	$U(\text{eq})$	BVS
Ba(1)	3b	0	4361(1)	1667	12(1)	2.49
Cu(1)	6c	4104(1)	749(1)	766(1)	21(1)	1.11
Ge(1)	3a	7142(1)	7142(1)	0	9(1)	4.01
S(1)	6c	5178(2)	4805(2)	1131(1)	11(1)	2.13
S(2)	6c	7628(2)	10930(2)	35(1)	11(1)	2.23

Table S1(c) Atomic coordinates ($\times 10^4$), equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for $\text{BaCu}_2\text{GeSe}_4$. $U(\text{eq})$ is defined as one third of the trace of the orthogonalized U_{ij} tensor.

Atoms	Wyck.	x	y	z	$U(\text{eq})$	BVS
Ba(1)	3a	4497.2(12)	4497.2(12)	0	12(2)	2.30
Cu(1)	6c	6608.(2)	797.(2)	8999(7)	21(3)	0.86
Ge(1)	3b	10000	7149(2)	1666.7	8(3)	3.92
Se(1)	6c	9669.4(16)	4781.8(15)	523.9(5)	10(2)	1.95
Se(2)	6c	6662.5(15)	7675.0(16)	1710.5(5)	10(3)	2.02

Table S1(d) Atomic coordinates ($\times 10^4$), equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for $\text{BaCu}_2\text{SnS}_4$. $U(\text{eq})$ is defined as one third of the trace of the orthogonalized U_{ij} tensor.

Atoms	Wyck.	x	y	z	$U(\text{eq})$	BVS
Ba(1)	3a	4324(1)	4324(1)	0	14(1)	2.24
Cu(1)	6c	728(2)	6536(2)	893(1)	23(1)	1.12
S(1)	6c	4575(4)	9522(4)	478(1)	13(1)	2.12
S(2)	6c	7650(4)	6548(4)	1670(1)	13(1)	2.20
Sn(1)	3b	7095(1)	10000	1667	11(1)	4.13

Table S1(e) Atomic coordinates ($\times 10^4$), equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for $\text{BaCu}_2\text{SnSe}_4$. $U(\text{eq})$ is defined as one third of the trace of the orthogonalized U_{ij} tensor.

Atoms	Wyck.	x	y	z	$U(\text{eq})$	BVS
Ba(1)	4a	0	5000	4992(1)	15(1)	2.23
Cu(1)	8c	1285(1)	2853(1)	862(2)	23(1)	0.84
Se(1)	4b	2500	1096(1)	2189(2)	13(1)	1.88
Se(2)	4b	2500	-588(1)	7456(2)	13(1)	1.97
Se(3)	8c	717(1)	2525(1)	7415(2)	13(1)	1.95
Sn(1)	4b	2500	1476(1)	5865(1)	12(1)	3.82

Table S2(a) Bond lengths (Å) and angles (°) for BaCu₂SiSe₄.

Ba(1)-Se(1)	3.2843(15)	Se(1)#3-Ba(1)-Se(2)#5	82.26(2)
Ba(1)-Se(1)#1	3.2843(15)	Se(2)#4-Ba(1)-Se(2)#5	129.61(3)
Ba(1)-Se(1)#2	3.3108(16)	Se(1)-Ba(1)-Se(2)#6	74.20(2)
Ba(1)-Se(1)#3	3.3108(17)	Se(1)#1-Ba(1)-Se(2)#6	141.103(18)
Ba(1)-Se(2)#4	3.3232(12)	Se(1)#2-Ba(1)-Se(2)#6	67.74(2)
Ba(1)-Se(2)#5	3.3232(12)	Se(1)#3-Ba(1)-Se(2)#6	79.46(3)
Ba(1)-Se(2)#6	3.3508(12)	Se(2)#4-Ba(1)-Se(2)#6	148.21(3)
Ba(1)-Se(2)#7	3.3508(12)	Se(2)#5-Ba(1)-Se(2)#6	66.799(13)
Cu(1)-Se(2)#5	2.4285(14)	Se(1)-Ba(1)-Se(2)#7	141.103(18)
Cu(1)-Se(1)#8	2.4286(15)	Se(1)#1-Ba(1)-Se(2)#7	74.20(2)
Cu(1)-Se(1)#9	2.5045(14)	Se(1)#2-Ba(1)-Se(2)#7	79.46(3)
Cu(1)-Se(2)	2.5391(18)	Se(1)#3-Ba(1)-Se(2)#7	67.738(19)
Si(1)-Se(2)#14	2.263(2)	Se(2)#4-Ba(1)-Se(2)#7	66.799(13)
Si(1)-Se(1)#14	2.269(2)	Se(2)#5-Ba(1)-Se(2)#7	148.21(3)
Se(1)-Ba(1)-Se(1)#1	123.62(4)	Se(2)#6-Ba(1)-Se(2)#7	115.23(3)
Se(1)-Ba(1)-Se(1)#2	69.44(4)	Se(2)#5-Cu(1)-Se(1)#8	132.69(5)
Se(1)#1-Ba(1)-Se(1)#2	147.85(2)	Se(2)#5-Cu(1)-Se(1)#9	108.47(5)
Se(1)-Ba(1)-Se(1)#3	147.85(2)	Se(1)#8-Cu(1)-Se(1)#9	99.17(4)
Se(1)#1-Ba(1)-Se(1)#3	69.44(4)	Se(2)#5-Cu(1)-Se(2)	95.36(4)
Se(1)#2-Ba(1)-Se(1)#3	116.75(5)	Se(1)#8-Cu(1)-Se(2)	117.98(5)
Se(1)-Ba(1)-Se(2)#4	85.92(2)	Se(1)#9-Cu(1)-Se(2)	98.53(5)
Se(1)#1-Ba(1)-Se(2)#4	70.67(3)	Se(2)-Si(1)-Se(1)#14	110.03(3)
Se(1)#2-Ba(1)-Se(2)#4	82.26(2)	Se(2)#14-Si(1)-Se(1)#14	112.92(3)
Se(1)#3-Ba(1)-Se(2)#4	125.534(17)	Se(2)-Si(1)-Se(1)	112.92(3)
Se(1)-Ba(1)-Se(2)#5	70.67(3)	Se(2)#14-Si(1)-Se(1)	110.03(3)
Se(1)#1-Ba(1)-Se(2)#5	85.92(2)	Se(1)#14-Si(1)-Se(1)	105.84(13)
Se(1)#2-Ba(1)-Se(2)#5	125.534(17)		

Symmetry transformations used to generate equivalent atoms:

#1 $x-y+1, -y+2, -z+4/3$	#2 $-x+1, -x+y+1, -z+5/3$	#3 $-y+1, x-y+1, z-1/3$
#4 $x, y+1, z$	#5 $x-y, -y+1, -z+4/3$	#6 $x-1, y, z$
#7 $x-y, -y+2, -z+4/3$	#8 $-y+2, x-y+1, z-1/3$	#9 $x-y+1, -y+1, -z+4/3$
#10 $x, y-1, z$	#11 $x+1, y, z$	#12 $-x+y+1, -x+2, z+1/3$
#13 $-x+y, -x+1, z+1/3$	#14 $-x+2, -x+y+1, -z+5/3$	

Table S2(b) Bond lengths (Å) and angles (°) for BaCu₂GeS₄.

Ba(1)-S(2)#1	3.1597(13)	S(1)#3-Ba(1)-S(2)#5	125.23(3)
Ba(1)-S(2)#2	3.1597(13)	S(1)-Ba(1)-S(2)#5	82.87(3)
Ba(1)-S(1)#3	3.1967(14)	S(2)#4-Ba(1)-S(2)#5	114.17(5)
Ba(1)-S(1)	3.1967(13)	S(2)#1-Ba(1)-S(1)#6	73.35(3)
Ba(1)-S(2)#4	3.2017(13)	S(2)#2-Ba(1)-S(1)#6	140.17(3)
Ba(1)-S(2)#5	3.2017(13)	S(1)#3-Ba(1)-S(1)#6	148.87(4)
Ba(1)-S(1)#6	3.2489(14)	S(1)-Ba(1)-S(1)#6	66.340(16)
Ba(1)-S(1)#7	3.2489(14)	S(2)#4-Ba(1)-S(1)#6	67.49(3)
Cu(1)-S(2)#10	2.3162(13)	S(2)#5-Ba(1)-S(1)#6	77.87(3)
Cu(1)-S(1)	2.3300(13)	S(2)#1-Ba(1)-S(1)#7	140.17(3)
Cu(1)-S(2)#11	2.4164(13)	S(2)#2-Ba(1)-S(1)#7	73.35(3)
Cu(1)-S(1)#1	2.4426(14)	S(1)#3-Ba(1)-S(1)#7	66.340(16)
Ge(1)-S(1)#14	2.2147(12)	S(1)-Ba(1)-S(1)#7	148.87(4)
Ge(1)-S(1)	2.2147(12)	S(2)#4-Ba(1)-S(1)#7	77.87(3)
Ge(1)-S(2)	2.2173(13)	S(2)#5-Ba(1)-S(1)#7	67.49(3)
Ge(1)-S(2)#14	2.2173(13)	S(1)#6-Ba(1)-S(1)#7	113.87(4)
S(2)#1-Ba(1)-S(2)#2	127.65(5)	S(2)#10-Cu(1)-S(1)	134.35(5)
S(2)#1-Ba(1)-S(1)#3	87.68(3)	S(2)#10-Cu(1)-S(2)#11	99.15(3)
S(2)#2-Ba(1)-S(1)#3	70.91(3)	S(1)-Cu(1)-S(2)#11	107.51(5)
S(2)#1-Ba(1)-S(1)	70.91(3)	S(2)#10-Cu(1)-S(1)#1	116.81(5)
S(2)#2-Ba(1)-S(1)	87.68(3)	S(1)-Cu(1)-S(1)#1	95.26(3)
S(1)#3-Ba(1)-S(1)	130.75(4)	S(2)#11-Cu(1)-S(1)#1	98.72(5)
S(2)#1-Ba(1)-S(2)#4	69.00(2)	S(1)#14-Ge(1)-S(1)	105.85(7)
S(2)#2-Ba(1)-S(2)#4	146.90(3)	S(1)#14-Ge(1)-S(2)	107.91(5)
S(1)#3-Ba(1)-S(2)#4	82.87(3)	S(1)-Ge(1)-S(2)	114.46(4)
S(1)-Ba(1)-S(2)#4	125.23(3)	S(1)#14-Ge(1)-S(2)#14	114.46(4)
S(2)#1-Ba(1)-S(2)#5	146.90(3)	S(1)-Ge(1)-S(2)#14	107.91(5)
S(2)#2-Ba(1)-S(2)#5	69.00(2)	S(2)-Ge(1)-S(2)#14	106.49(7)

Symmetry transformations used to generate equivalent atoms:

#1 -x+1,-x+y,-z+1/3	#2 x-1,y-1,z	#3 -x,-x+y,-z+1/3
#4 -y+1,x-y+1,z+1/3	#5 y-1,x,-z	#6 -x+1,-x+y+1,-z+1/3
#7 x-1,y,z	#8 -x,-x+y+1,-z+1/3	#9 x,y+1,z
#10 y-1,x-1,-z	#11 x,y-1,z	#12 x+1,y,z
#13 -x+y,-x,z-1/3	#14 y,x,-z	#15 y+1,x+1,-z
#16 x+1,y+1,z	#17 -x+y,-x+1,z-1/3	

Table S2(c) Bond lengths (Å) and angles (°) for BaCu₂GeSe₄.

Ba(1)-Se(4)	3.3096(13)	Se(3)#1-Ba(1)-Se(2)#4	86.32(3)
Ba(1)-Se(3)#1	3.3118(13)	Se(3)-Ba(1)-Se(2)#4	126.17(3)
Ba(1)-Se(3)	3.3281(13)	Se(4)#2-Ba(1)-Se(2)#4	82.51(3)
Ba(1)-Se(4)#2	3.3303(13)	Se(1)#3-Ba(1)-Se(2)#4	127.61(3)
Ba(1)-Se(1)#3	3.3441(13)	Se(4)-Ba(1)-Se(2)	139.63(3)
Ba(1)-Se(2)#4	3.3472(13)	Se(3)#1-Ba(1)-Se(2)	73.53(3)
Ba(1)-Se(2)	3.3818(12)	Se(3)-Ba(1)-Se(2)	78.36(3)
Ba(1)-Se(1)#5	3.3845(12)	Se(4)#2-Ba(1)-Se(2)	69.83(3)
Ba(1)-Cu(2)#3	3.6200(16)	Se(1)#3-Ba(1)-Se(2)	66.17(3)
Ba(1)-Cu(1)#4	3.6240(16)	Se(2)#4-Ba(1)-Se(2)	150.11(4)
Ba(1)-Cu(2)#5	3.8959(16)	Se(4)-Ba(1)-Se(1)#5	73.53(3)
Ba(1)-Cu(1)	3.8971(17)	Se(3)#1-Ba(1)-Se(1)#5	139.59(3)
Cu(1)-Se(1)#6	2.4269(18)	Se(3)-Ba(1)-Se(1)#5	69.81(3)
Cu(1)-Se(3)	2.4342(17)	Se(4)#2-Ba(1)-Se(1)#5	78.31(3)
Cu(1)-Se(4)#7	2.4944(18)	Se(1)#3-Ba(1)-Se(1)#5	150.14(4)
Cu(1)-Se(2)	2.541(2)	Se(2)#4-Ba(1)-Se(1)#5	66.15(3)
Cu(2)-Se(2)#1	2.4266(18)	Se(2)-Ba(1)-Se(1)#5	116.75(3)
Cu(2)-Se(4)#8	2.4363(18)	Se(1)#6-Cu(1)-Se(3)	132.96(7)
Cu(2)-Se(3)#8	2.4944(18)	Se(1)#6-Cu(1)-Se(4)#7	109.02(6)
Cu(2)-Se(1)	2.536(2)	Se(3)-Cu(1)-Se(4)#7	99.27(6)
Ge(1)-Se(1)	2.3519(16)	Se(1)#6-Cu(1)-Se(2)	95.34(6)
Ge(1)-Se(2)	2.3550(16)	Se(3)-Cu(1)-Se(2)	116.84(7)
Ge(1)-Se(3)#9	2.3605(15)	Se(4)#7-Cu(1)-Se(2)	98.97(6)
Ge(1)-Se(4)#2	2.3605(15)	Se(2)#1-Cu(2)-Se(4)#8	132.82(7)
Se(4)-Ba(1)-Se(3)#1	125.75(3)	Se(2)#1-Cu(2)-Se(3)#8	109.01(6)
Se(4)-Ba(1)-Se(3)	68.85(3)	Se(4)#8-Cu(2)-Se(3)#8	99.11(6)
Se(3)#1-Ba(1)-Se(3)	146.81(3)	Se(2)#1-Cu(2)-Se(1)	95.42(6)
Se(4)-Ba(1)-Se(4)#2	146.75(3)	Se(4)#8-Cu(2)-Se(1)	117.01(7)
Se(3)#1-Ba(1)-Se(4)#2	68.86(3)	Se(3)#8-Cu(2)-Se(1)	99.11(6)
Se(3)-Ba(1)-Se(4)#2	117.10(3)	Se(1)-Ge(1)-Se(2)	105.07(5)
Se(4)-Ba(1)-Se(1)#3	86.33(3)	Se(1)-Ge(1)-Se(3)#9	109.21(6)
Se(3)#1-Ba(1)-Se(1)#3	70.22(3)	Se(2)-Ge(1)-Se(3)#9	113.93(6)
Se(3)-Ba(1)-Se(1)#3	82.56(3)	Se(1)-Ge(1)-Se(4)#2	114.08(6)
Se(4)#2-Ba(1)-Se(1)#3	126.21(3)	Se(2)-Ge(1)-Se(4)#2	109.14(6)
Se(4)-Ba(1)-Se(2)#4	70.21(3)	Se(3)#9-Ge(1)-Se(4)#2	105.63(5)

Symmetry transformations used to generate equivalent atoms:

#1 -x+y,-x+1,z-1/3	#2 -x+y+1,-x+2,z-1/3	#3 -y+1,x-y+1,z+1/3
#4 x+1,y,z	#5 -y+2,x-y+2,z+1/3	#6 -y+1,x-y+2,z+1/3
#7 x-1,y,z	#8 -y+1,x-y+1,z-2/3	#9 -x+y,-x+2,z-1/3
#10 -x+y-1,-x+1,z-1/3	#11 -x+y,-x+1,z+2/3	#12 -y+2,x-y+1,z+1/3

Table S2(d) Bond lengths (Å) and angles (°) for BaCu₂SnS₄.

Ba(1)-S(2)#1	3.203(3)	S(1)#4-Ba(1)-S(2)#5	126.73(5)
Ba(1)-S(2)#2	3.203(3)	S(2)-Ba(1)-S(2)#5	113.81(9)
Ba(1)-S(1)#3	3.223(3)	S(2)#1-Ba(1)-S(1)	136.92(5)
Ba(1)-S(1)#4	3.223(3)	S(2)#2-Ba(1)-S(1)	72.17(5)
Ba(1)-S(2)	3.229(3)	S(1)#3-Ba(1)-S(1)	65.09(3)
Ba(1)-S(2)#5	3.229(3)	S(1)#4-Ba(1)-S(1)	152.85(7)
Ba(1)-S(1)	3.313(3)	S(2)-Ba(1)-S(1)	71.53(5)
Ba(1)-S(1)#5	3.313(3)	S(2)#5-Ba(1)-S(1)	75.30(6)
Cu(1)-S(2)#9	2.311(2)	S(2)#1-Ba(1)-S(1)#5	72.17(5)
Cu(1)-S(1)	2.316(2)	S(2)#2-Ba(1)-S(1)#5	136.92(5)
Cu(1)-S(2)#2	2.416(2)	S(1)#3-Ba(1)-S(1)#5	152.85(7)
Cu(1)-S(1)#3	2.423(3)	S(1)#4-Ba(1)-S(1)#5	65.09(3)
Sn(1)-S(1)#14	2.386(2)	S(2)-Ba(1)-S(1)#5	75.30(6)
Sn(1)-S(2)#14	2.389(2)	S(2)#5-Ba(1)-S(1)#5	71.53(5)
S(2)#1-Ba(1)-S(2)#2	132.11(8)	S(1)-Ba(1)-S(1)#5	116.99(7)
S(2)#1-Ba(1)-S(1)#3	88.53(6)	S(2)#9-Cu(1)-S(1)	134.06(9)
S(2)#2-Ba(1)-S(1)#3	70.23(6)	S(2)#9-Cu(1)-S(2)#2	99.33(6)
S(2)#1-Ba(1)-S(1)#4	70.23(6)	S(1)-Cu(1)-S(2)#2	108.39(8)
S(2)#2-Ba(1)-S(1)#4	88.53(6)	S(2)#9-Cu(1)-S(1)#3	115.15(9)
S(1)#3-Ba(1)-S(1)#4	126.71(7)	S(1)-Cu(1)-S(1)#3	95.79(6)
S(2)#1-Ba(1)-S(2)	144.61(5)	S(2)#2-Cu(1)-S(1)#3	99.60(9)
S(2)#2-Ba(1)-S(2)	68.16(6)	S(1)#14-Sn(1)-S(1)	105.19(12)
S(1)#3-Ba(1)-S(2)	126.73(5)	S(1)#14-Sn(1)-S(2)#14	106.41(8)
S(1)#4-Ba(1)-S(2)	83.79(5)	S(1)-Sn(1)-S(2)#14	117.03(7)
S(2)#1-Ba(1)-S(2)#5	68.16(6)	S(1)#14-Sn(1)-S(2)	117.03(7)
S(2)#2-Ba(1)-S(2)#5	144.61(5)	S(1)-Sn(1)-S(2)	106.41(8)
S(1)#3-Ba(1)-S(2)#5	83.79(5)	S(2)#14-Sn(1)-S(2)	105.32(11)

Symmetry transformations used to generate equivalent atoms:

#1 -y+1,x-y,z-1/3	#2 x-y,-y+1,-z+1/3	#3 y-1,x,-z
#4 x,y-1,z	#5 y,x,-z	#6 x+1,y,z
#7 y,x+1,-z	#8 -y+1,x-y+1,z-1/3	#9 x-1,y,z
#10 -x+y,-x+1,z+1/3	#11 x,y+1,z	#12 x-y+1,-y+1,-z+1/3
#13 -x+y+1,-x+1,z+1/3	#14 x-y+1,-y+2,-z+1/3	

Table S2(e) Bond lengths (Å) and angles (°) for BaCu₂SnSe₄.

Ba(1)-Se(3)#1	3.311(2)	Se(2)#3-Ba(1)-Se(1)#5	147.11(4)
Ba(1)-Se(3)	3.311(2)	Se(1)#4-Ba(1)-Se(1)#5	128.05(7)
Ba(1)-Se(2)#2	3.323(2)	Se(3)#1-Ba(1)-Se(3)#2	152.57(4)
Ba(1)-Se(2)#3	3.323(2)	Se(3)-Ba(1)-Se(3)#2	67.25(6)
Ba(1)-Se(1)#4	3.375(2)	Se(2)#2-Ba(1)-Se(3)#2	73.02(4)
Ba(1)-Se(1)#5	3.375(2)	Se(2)#3-Ba(1)-Se(3)#2	76.70(4)
Ba(1)-Se(3)#2	3.409(2)	Se(1)#4-Ba(1)-Se(3)#2	135.70(2)
Ba(1)-Se(3)#3	3.409(2)	Se(1)#5-Ba(1)-Se(3)#2	74.32(4)
Cu(1)-Se(3)#6	2.431(3)	Se(3)#1-Ba(1)-Se(3)#3	67.25(6)
Cu(1)-Se(2)#3	2.4528(19)	Se(3)-Ba(1)-Se(3)#3	152.57(4)
Cu(1)-Se(3)#2	2.492(2)	Se(2)#2-Ba(1)-Se(3)#3	76.70(4)
Cu(1)-Se(1)	2.546(2)	Se(2)#3-Ba(1)-Se(3)#3	73.02(4)
Sn(1)-Se(3)#7	2.5266(18)	Se(1)#4-Ba(1)-Se(3)#3	74.32(4)
Sn(1)- Se(2)	2.545(2)	Se(1)#5-Ba(1)-Se(3)#3	135.70(2)
Sn(1)- Se(1)	2.509(3)	Se(3)#6-Cu(1)-Se(3)#2	98.23(6)
Sn(1)- Se(3)	2.5266(18)	Se(2)#3-Cu(1)-Se(3)#2	115.30(7)
Se(3)#1-Ba(1)-Se(3)	121.00(7)	Se(3)#6-Cu(1)-Se(1)	110.83(6)
Se(3)#1-Ba(1)-Se(2)#2	83.49(4)	Se(2)#3-Cu(1)-Se(1)	96.01(8)
Se(3)-Ba(1)-Se(2)#2	128.24(3)	Se(3)#2-Cu(1)-Se(1)	101.21(7)
Se(3)#1-Ba(1)-Se(2)#3	128.24(3)	Se(3)#6-Cu(1)-Cu(1)#7	105.04(4)
Se(3)-Ba(1)-Se(2)#3	83.49(4)	Se(2)#3-Cu(1)-Cu(1)#7	56.64(4)
Se(2)#2-Ba(1)-Se(2)#3	118.23(8)	Se(3)#2-Cu(1)-Cu(1)#7	153.10(4)
Se(3)#1-Ba(1)-Se(1)#4	71.23(5)	Se(1)-Cu(1)-Cu(1)#7	58.01(4)
Se(3)-Ba(1)-Se(1)#4	83.71(5)	Se(1)-Sn(1)-Se(3)#7	119.06(4)
Se(2)#2-Ba(1)-Se(1)#4	147.11(4)	Se(1)-Sn(1)-Se(3)	119.06(4)
Se(2)#3-Ba(1)-Se(1)#4	67.04(6)	Se(3)#7-Sn(1)-Se(3)	103.15(8)
Se(3)#1-Ba(1)-Se(1)#5	83.71(5)	Se(1)-Sn(1)-Se(2)	105.11(6)
Se(3)-Ba(1)-Se(1)#5	71.23(5)	Se(3)#7-Sn(1)-Se(2)	104.34(5)
Se(2)#2-Ba(1)-Se(1)#5	67.04(6)	Se(3)-Sn(1)-Se(2)	104.34(5)

Symmetry transformations used to generate equivalent atoms:

#1 -x,-y+1,z	#2 -x,-y+1/2,z-1/2	#3 x,y+1/2,z-1/2
#4 x,y+1/2,z+1/2	#5 -x,-y+1/2,z+1/2	#6 x,y,z-1
#7 -x+1/2,y,z	#8 x,y-1/2,z-1/2	#9 -x+1/2,y-1/2,z-1/2
#10 x,y-1/2,z+1/2	#11 -x+1/2,y-1/2,z+1/2	#12 x,y,z+1

Table S3 Calculated NLO SHG coefficients and percentage of VH (Virtual-Hole) and VE (Virtual-Electron) in $\text{BaCu}_2\text{M}^{\text{IV}}\text{Q}_4$ ($\text{M}^{\text{IV}} = \text{Si, Ge, and Sn}$; $\text{Q} = \text{S, Se}$).

Compounds	SHG coefficients (pm/V)		
	Total	VH	VE
$\text{BaCu}_2\text{SiSe}_4$	$d_{12} = 4.18$	36.53%	63.47%
$\text{BaCu}_2\text{GeS}_4$	$d_{12} = 0.28$	48.46%	51.54%
$\text{BaCu}_2\text{GeSe}_4$	$d_{12} = 5.62$	43.37%	56.63%
$\text{BaCu}_2\text{SnS}_4$	$d_{12} = 12.09$	90.01%	9.99%
$\text{BaCu}_2\text{SnSe}_4$	$d_{12} = 1.45$	47.72%	52.28%

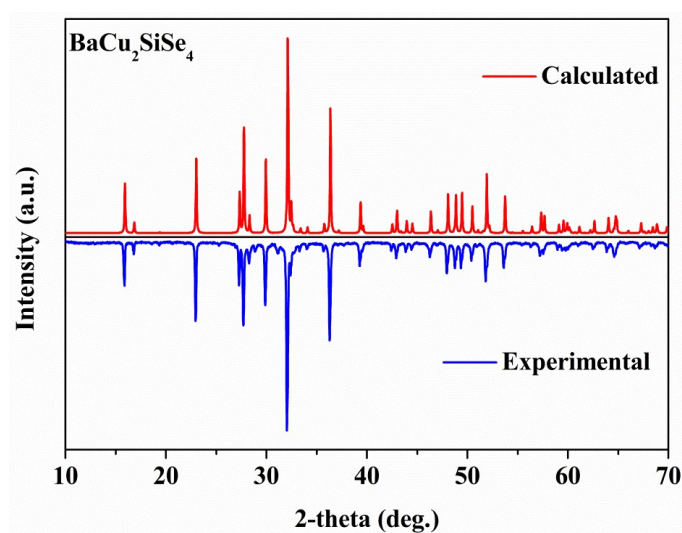


Fig. S1(a) Powder XRD patterns of $\text{BaCu}_2\text{SiSe}_4$.

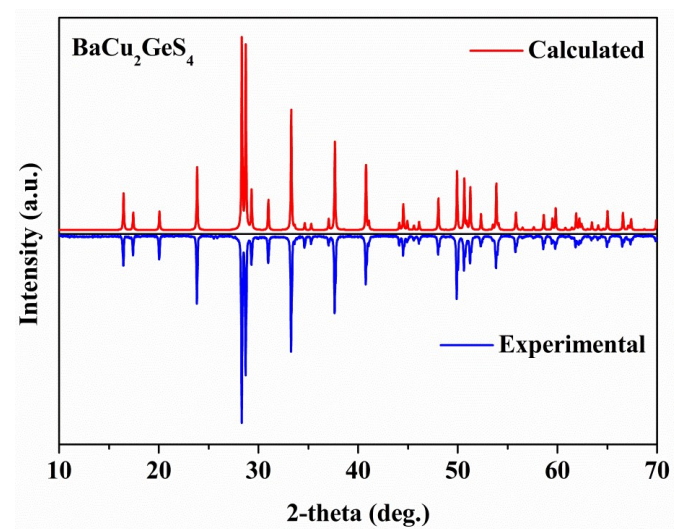


Fig. S1(b) Powder XRD patterns of $\text{BaCu}_2\text{GeS}_4$.

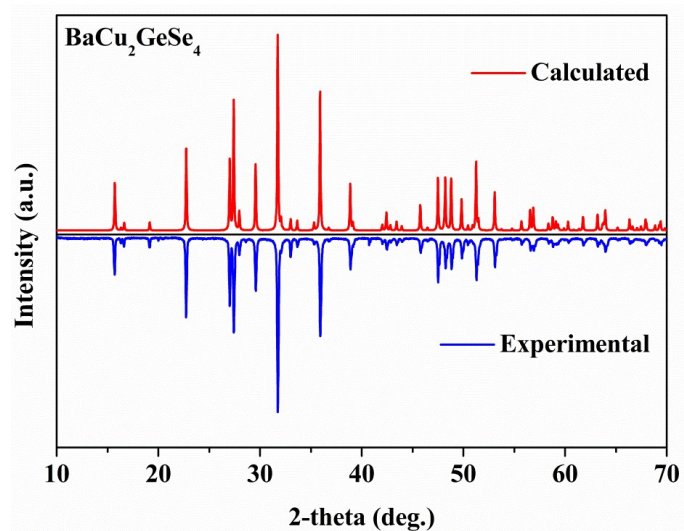


Fig. S1(c) Powder XRD patterns of $\text{BaCu}_2\text{GeSe}_4$.

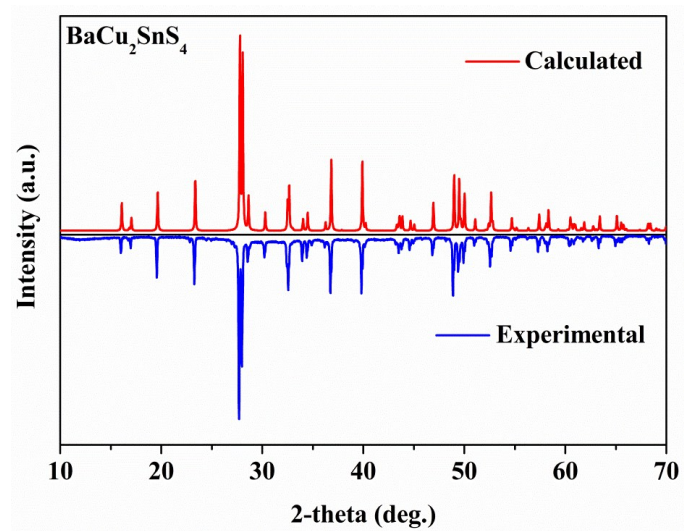


Fig. S1(d) Powder XRD patterns of $\text{BaCu}_2\text{SnS}_4$.

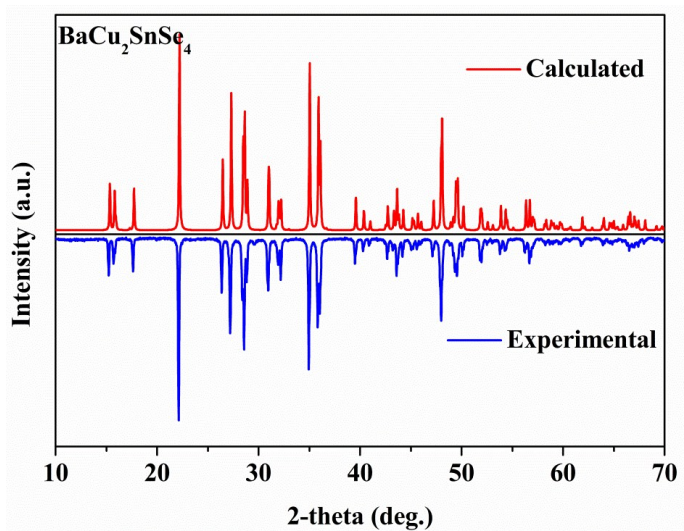


Fig. S1(e) Powder XRD patterns of $\text{BaCu}_2\text{SnSe}_4$.

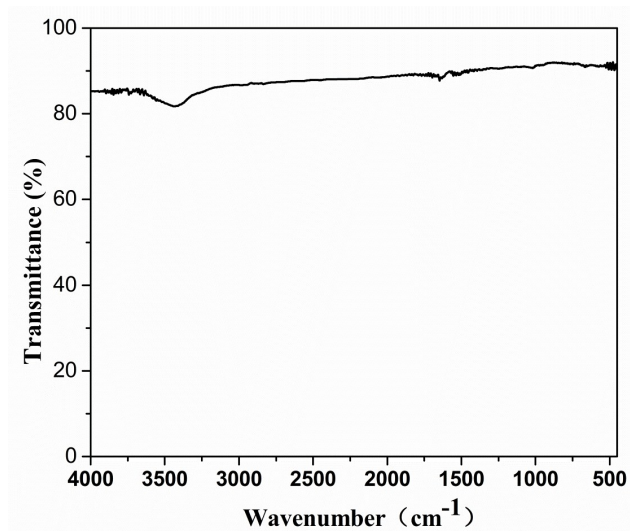


Fig. S2(a) The IR spectrum of as-synthesized $\text{BaCu}_2\text{SiSe}_4$.

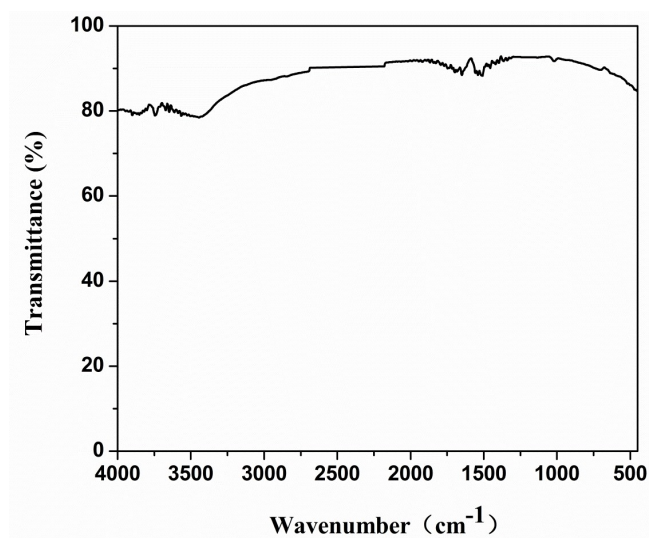


Fig. S2(b) The IR spectrum of as-synthesized $\text{BaCu}_2\text{GeSe}_4$.

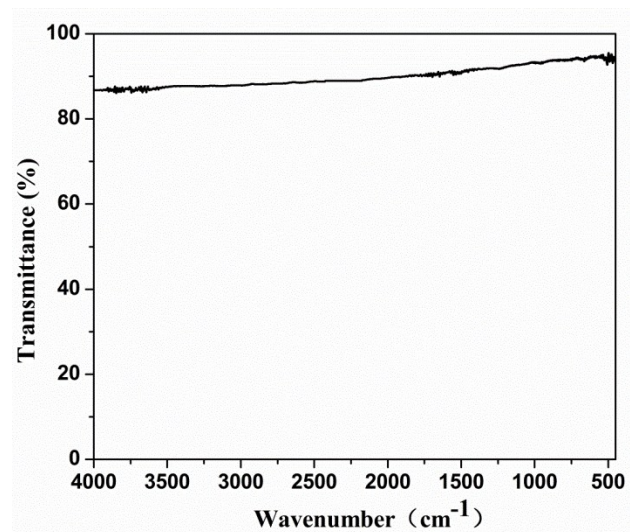


Fig. S2(c) The IR spectrum of as-synthesized $\text{BaCu}_2\text{GeSe}_4$.

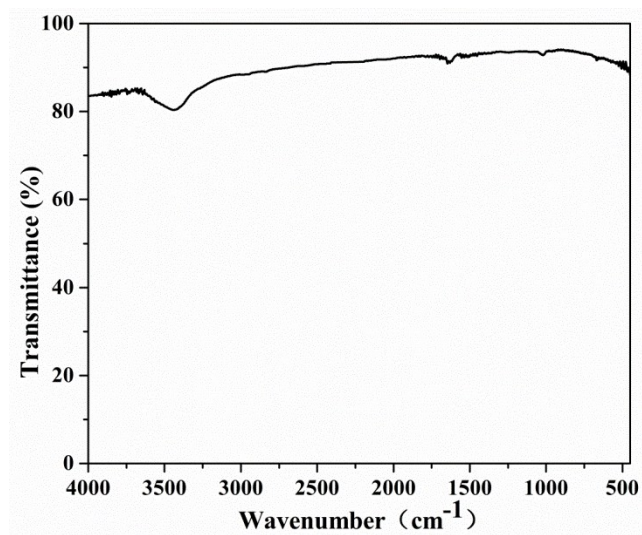


Fig. S2(d) The IR spectrum of as-synthesized BaCu₂SnS₄.

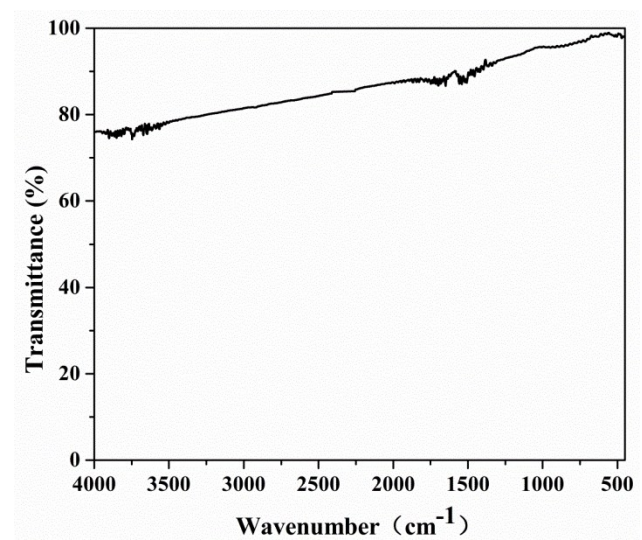


Fig. S2(e) The IR spectrum of as-synthesized BaCu₂SnSe₄.

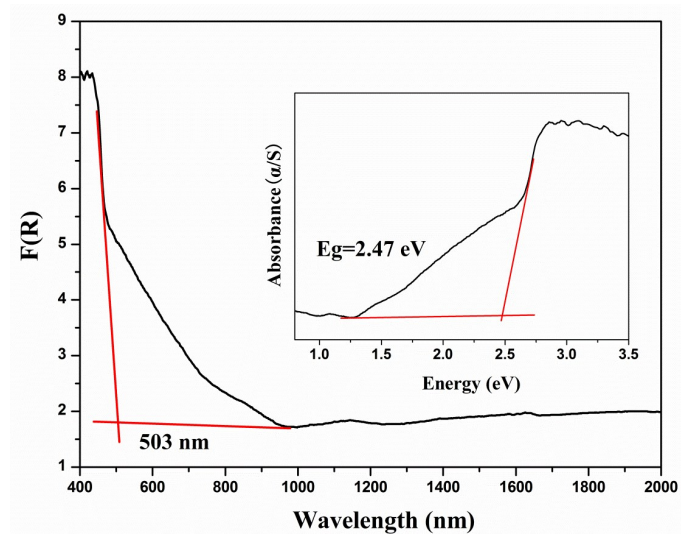


Fig. S3(a) Absorption spectrum of BaCu₂SiSe₄. The inset diagram is the experimental band gap.

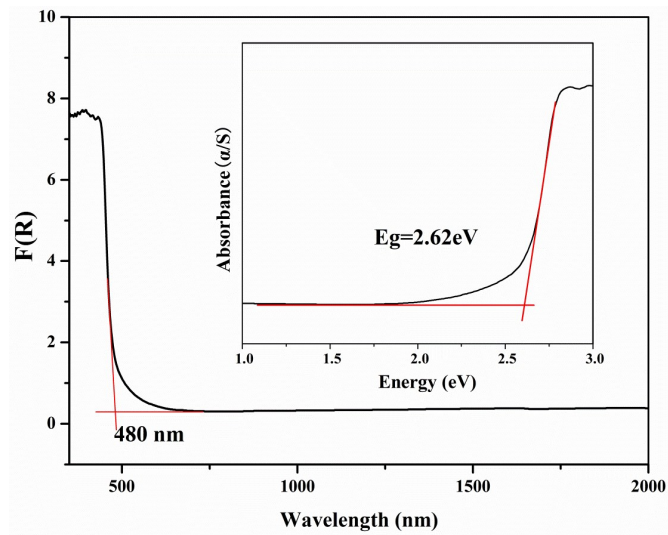


Fig. S3(b) Absorption spectrum of BaCu₂GeS₄. The inset diagram is the experimental band gap.

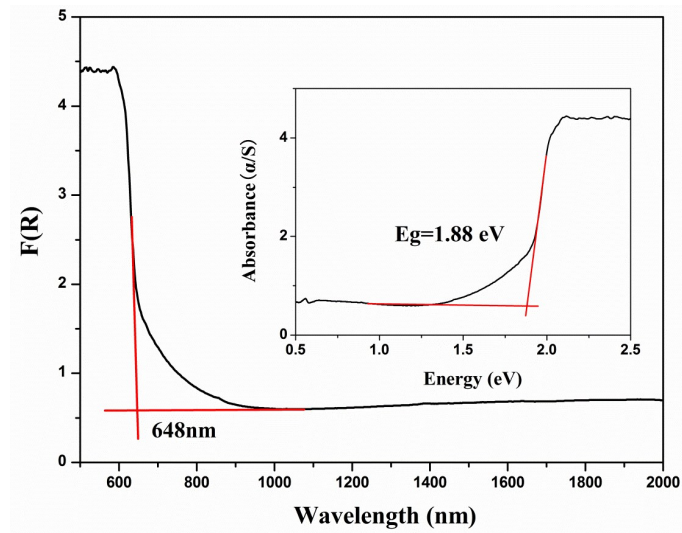


Fig. S3(c) Absorption spectrum of BaCu₂GeSe₄. The inset diagram is the experimental band gap.

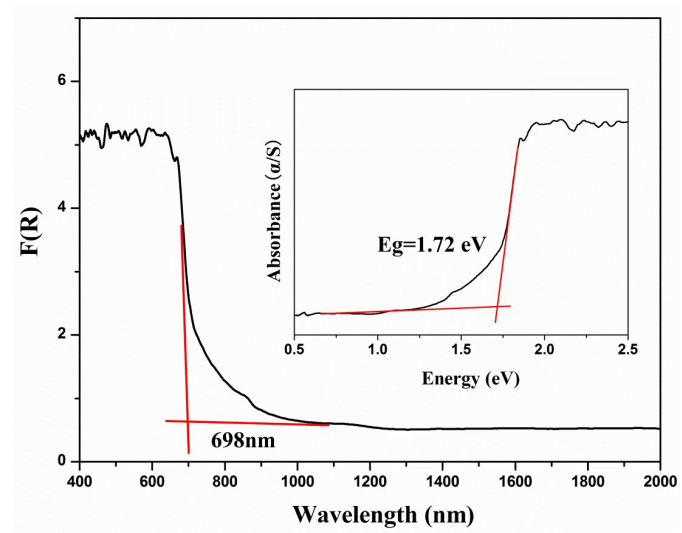


Fig. S3(d) Absorption spectrum of BaCu₂SnSe₄. The inset diagram is the experimental band gap.

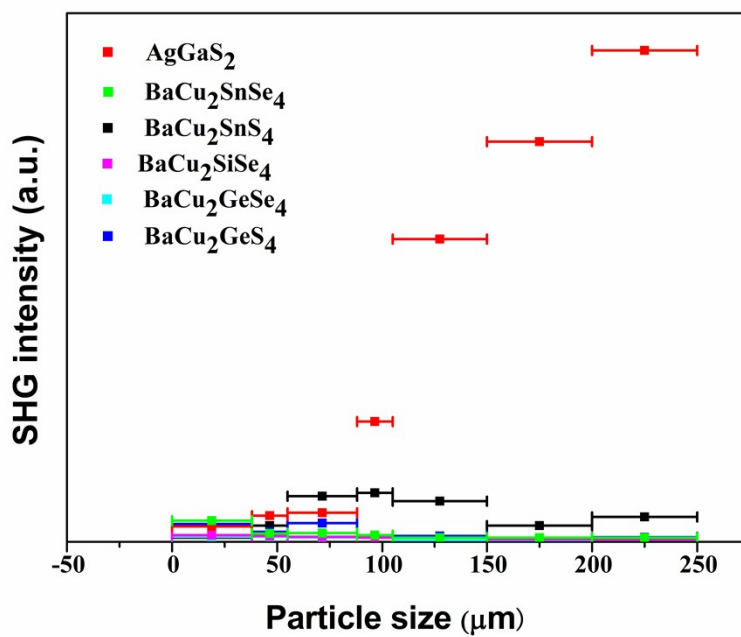


Fig. S4 SHG response for title compounds in different particle sizes (AgGaS₂ as the reference).

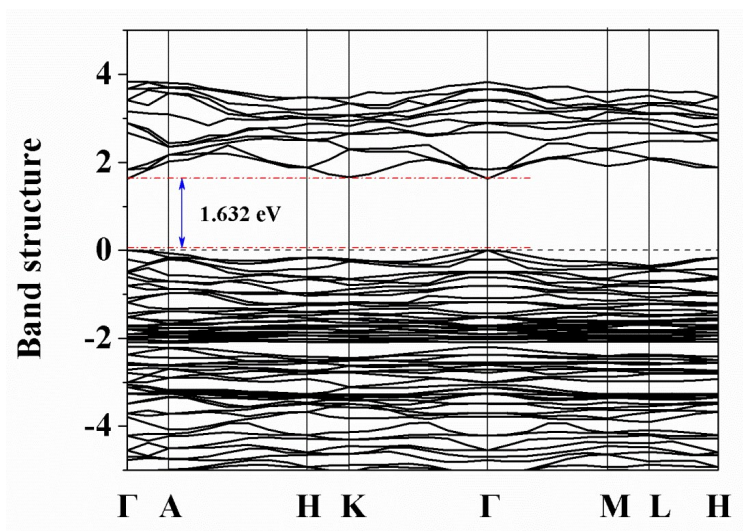


Fig. S5(a) The electronic structure of BaCu₂SiSe₄.

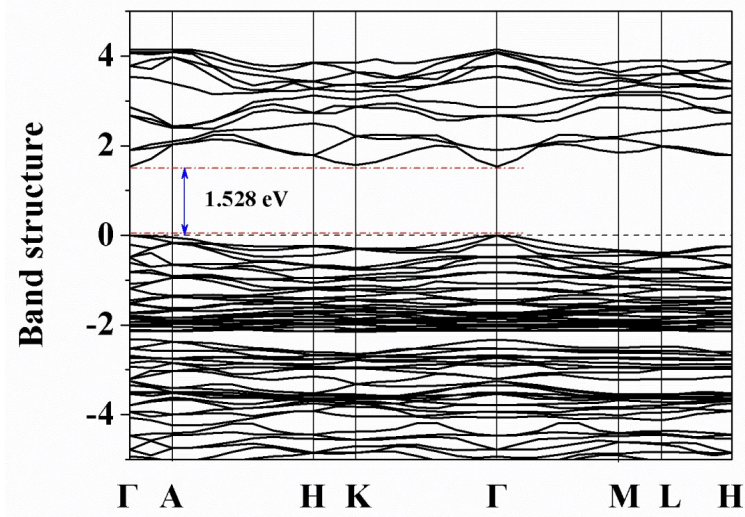


Fig. S5(b) The electronic structure of BaCu₂GeS₄.

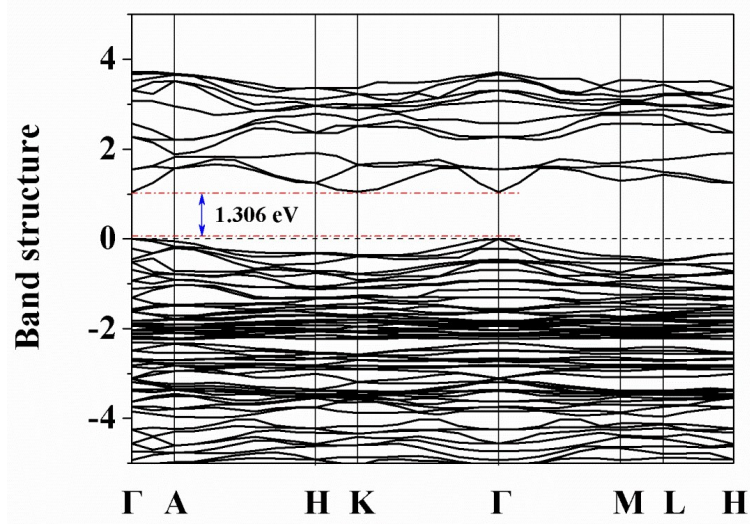


Fig. S5(c) The electronic structure of BaCu₂GeSe₄.

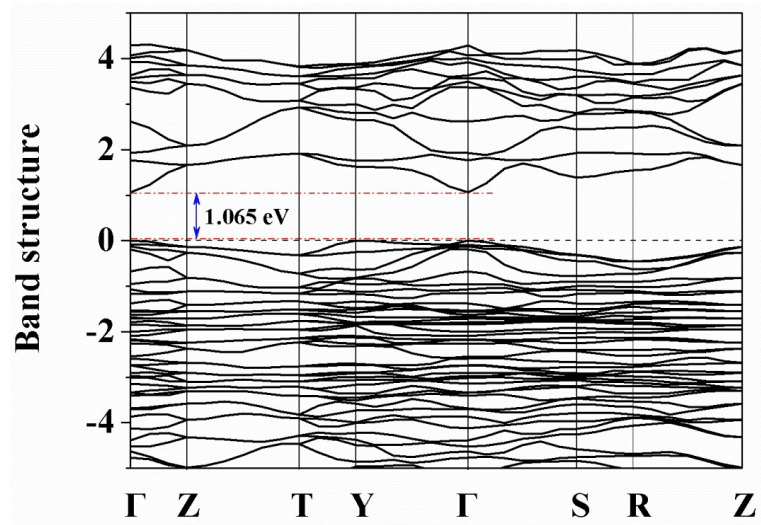


Fig. S5(d) The electronic structure of BaCu₂SnSe₄.

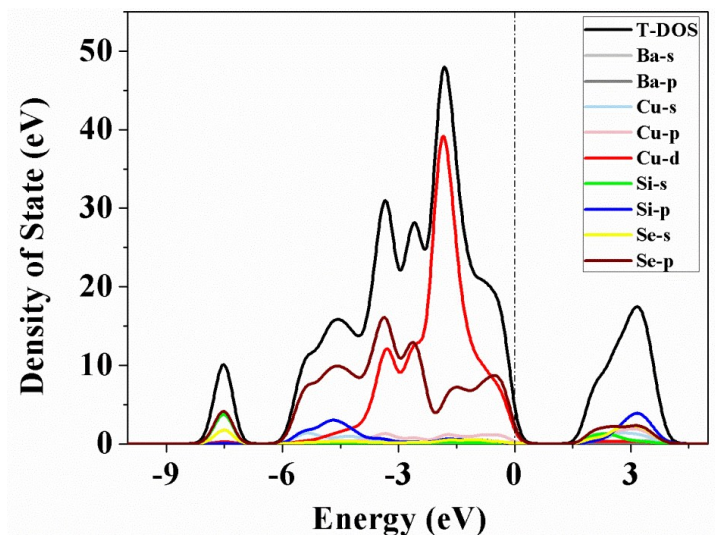


Fig. S6(a) The PDOS of BaCu₂SiSe₄.

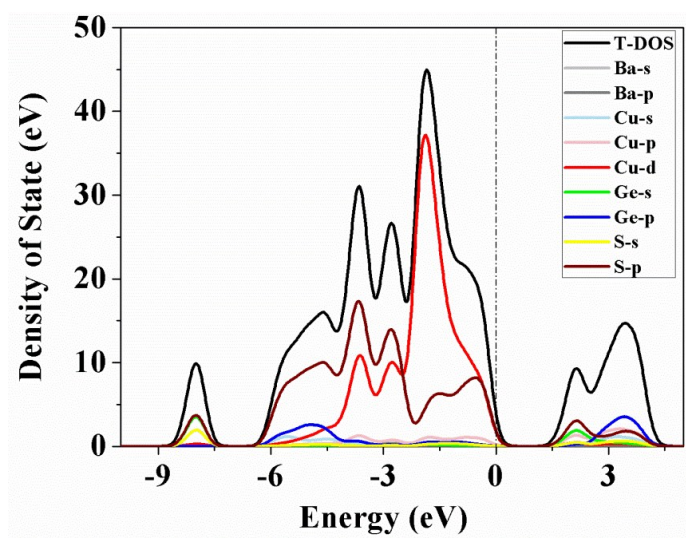


Fig. S6(b) The PDOS of BaCu₂GeS₄.

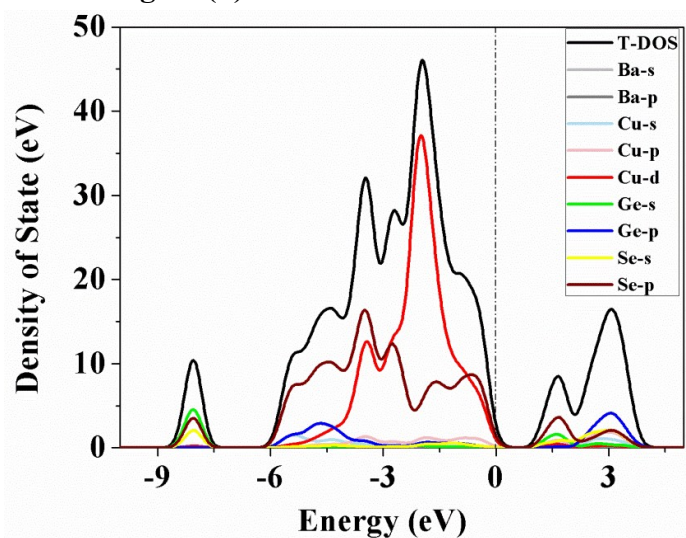


Fig. S6(c) The PDOS of BaCu₂GeSe₄.

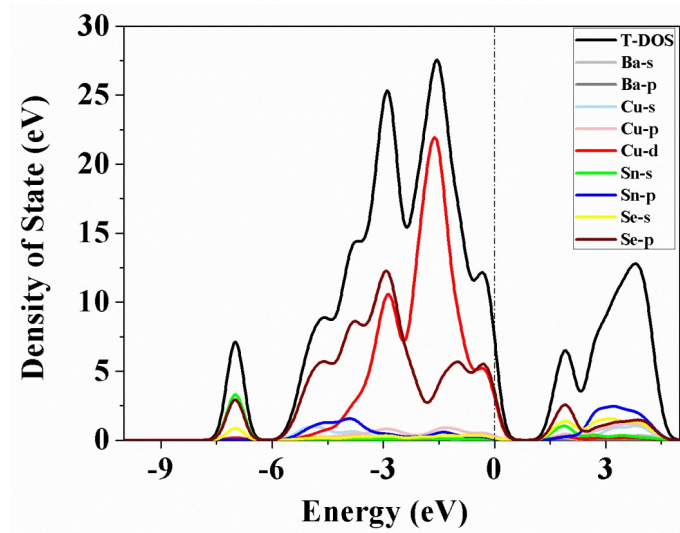


Fig. S6(d) The PDOS of $\text{BaCu}_2\text{SnSe}_4$.

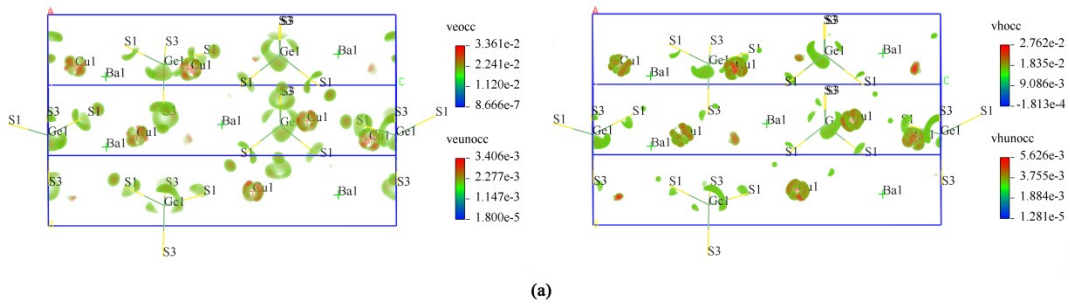


Fig. S7(a) SHG density of $\text{BaCu}_2\text{GeS}_4$.

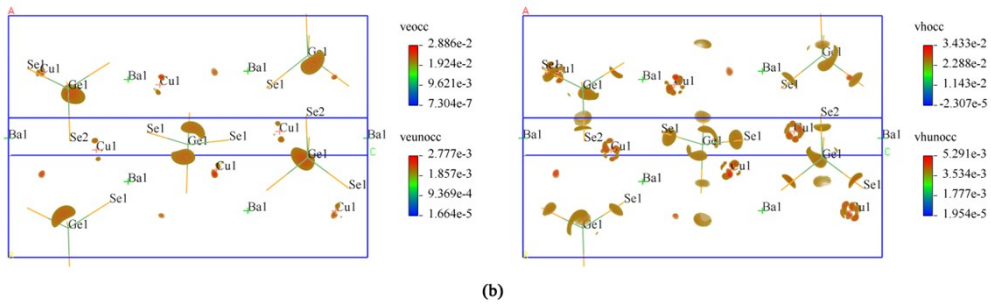


Fig. S7(b) SHG density of $\text{BaCu}_2\text{GeSe}_4$.

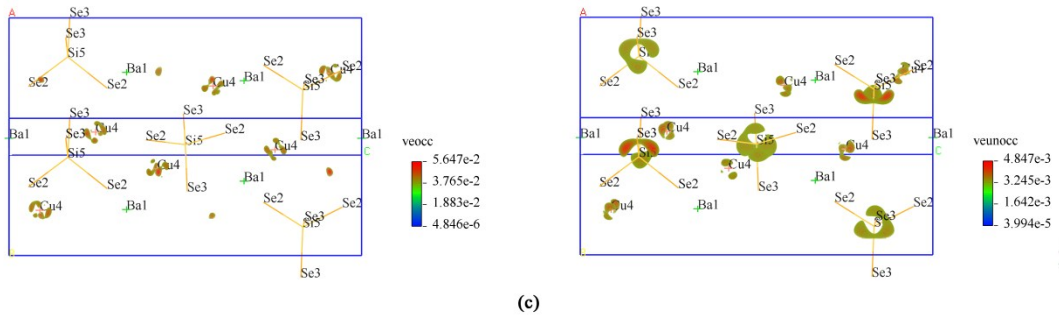
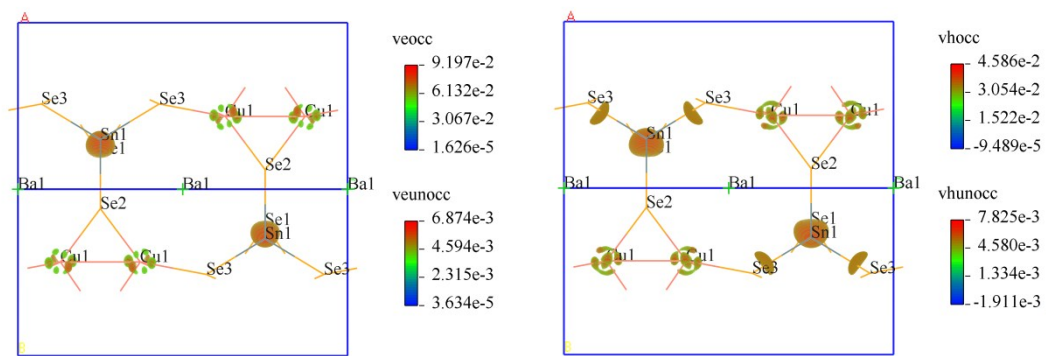


Fig. S7(c) SHG density of $\text{BaCu}_2\text{SiSe}_4$.



(d)

Fig. S7(d) SHG density of $\text{BaCu}_2\text{SnSe}_4$.