

Supplementary Information (SI) of “Electric field tunable band-gap  
crossover in black(blue) phosphorus/g-ZnO van der Waals  
heterostructures”

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### SI.1: Convergence tests.

black-p/g-ZnO

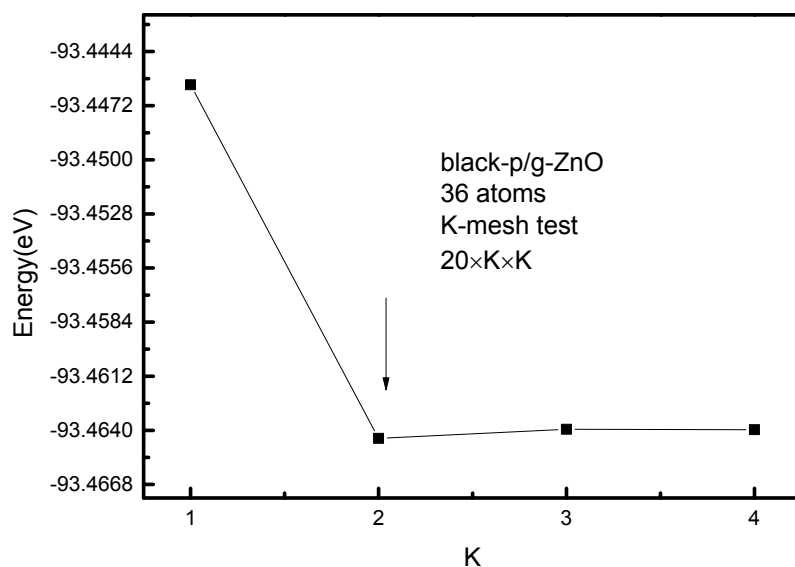


Fig. S1.1 Change of energy of black-p/g-ZnO with k-point meshes (20×K×K).

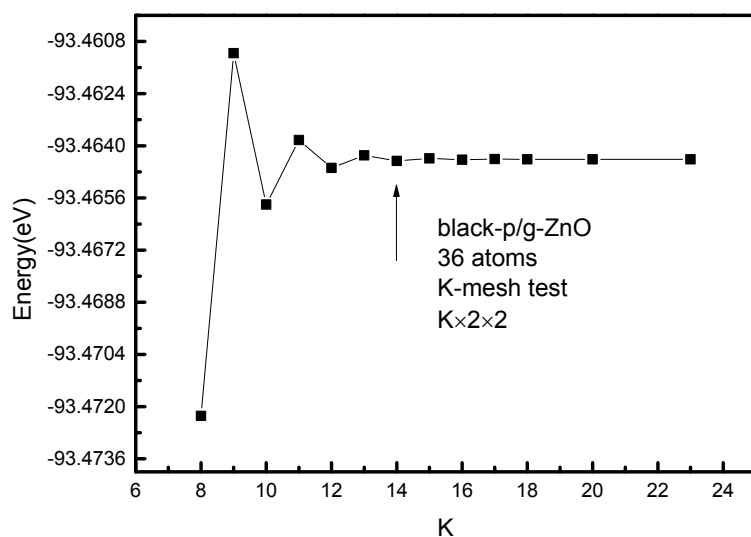


Fig. S1.2 Change of energy of black-p/g-ZnO with k-point meshes (K×2×2).

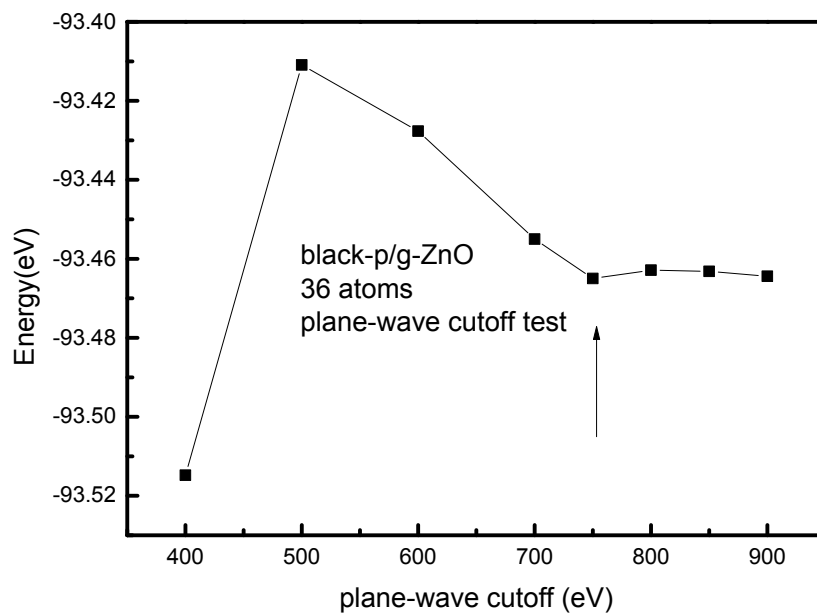


Fig. S1.3 Change of energy of black-p/g-ZnO with plane-wave cutoffs.

blue-p/g-ZnO

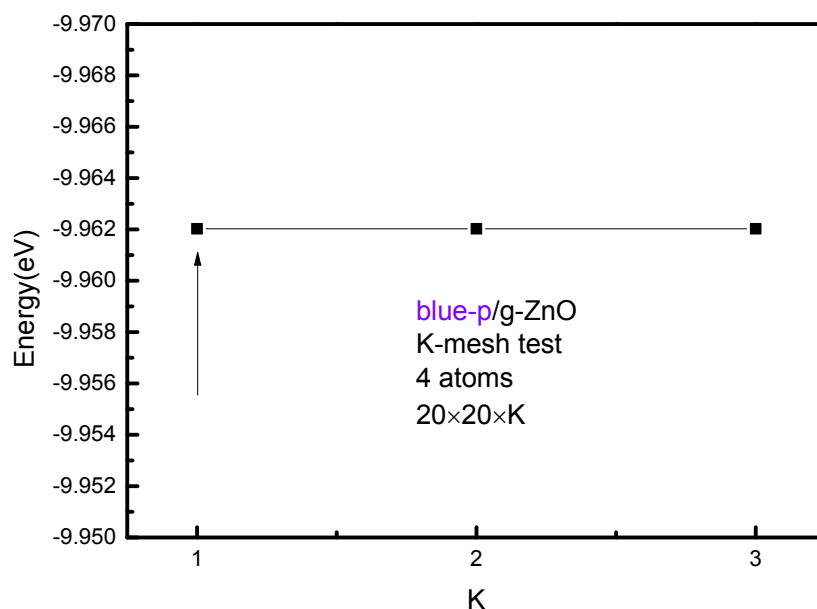


Fig. S1.4 Change of energy of blue-p/g-ZnO with k-point meshes (20×20×K).

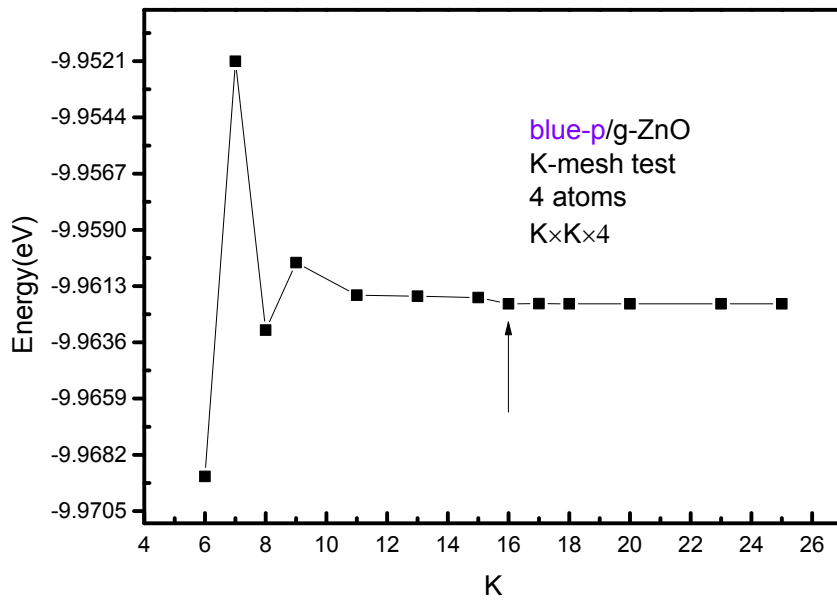


Fig. S1.5 Change of energy of blue-p/g-ZnO with k-point meshes (K×K×4).

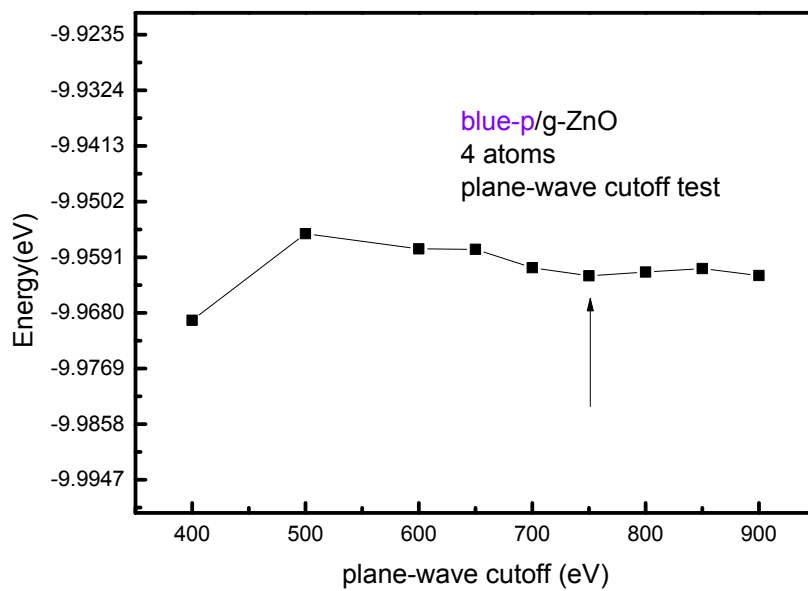


Fig. S1.6 Change of energy of blue-p/g-ZnO with plane-wave cutoffs.

SI.2: Other typical patterns of heterostructures.

black-p/g-ZnO

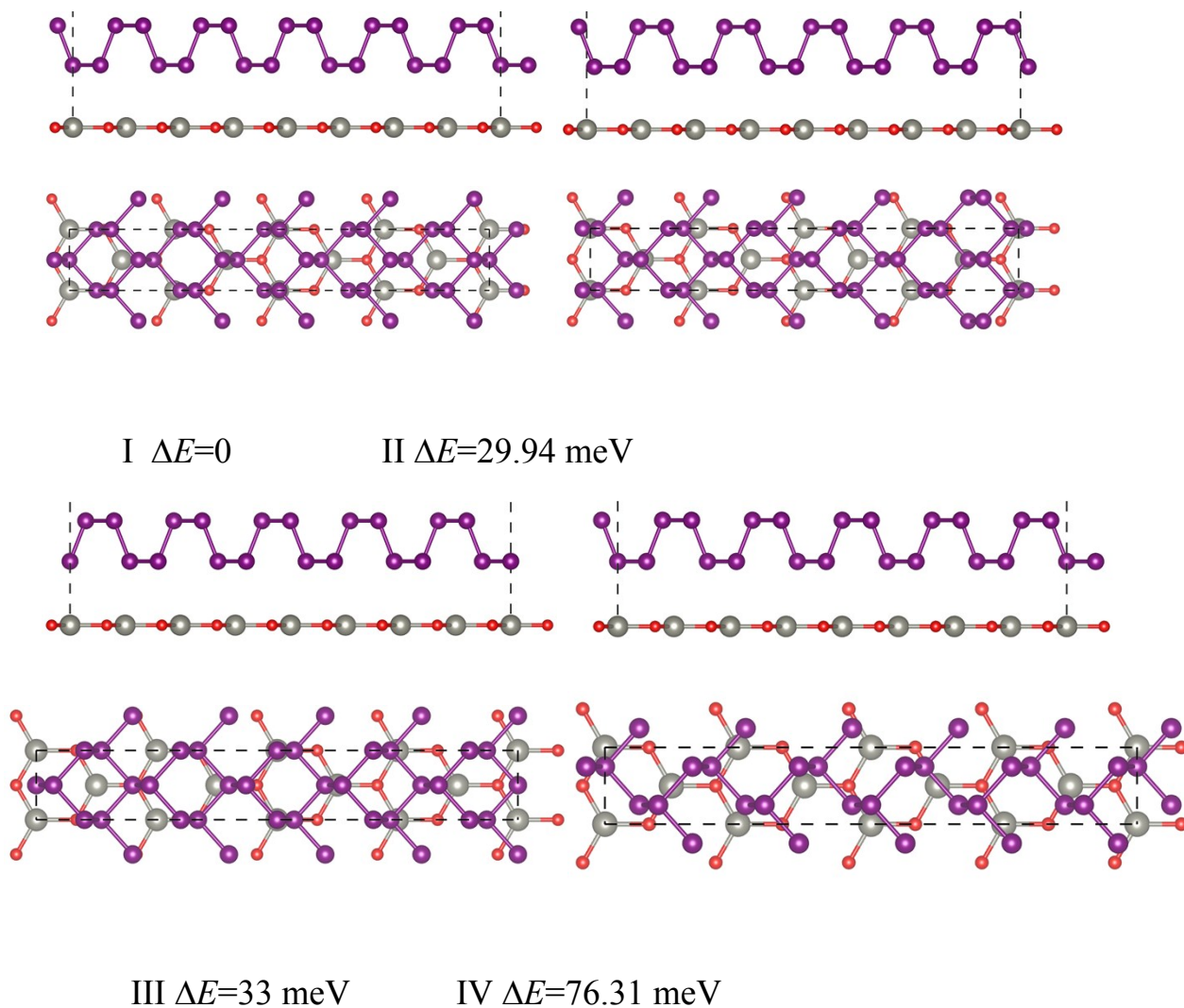
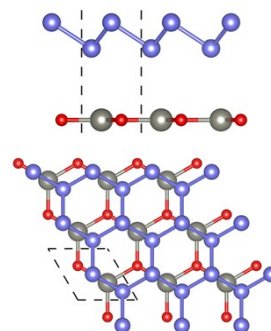


Fig. S2.1 Relative energy of other typical patterns of black-p/g-ZnO.

blue-p/g-ZnO



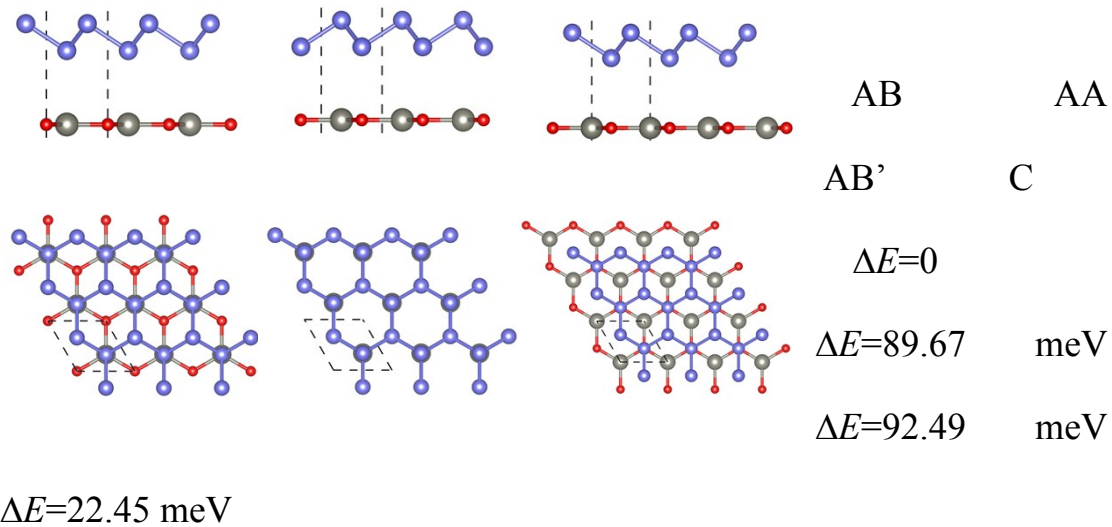


Fig. S2.2 Relative energy of other typical patterns of blue-p/g-ZnO.

**SI.3:** Band structures of isolated black-p, g-ZnO and blue-p.

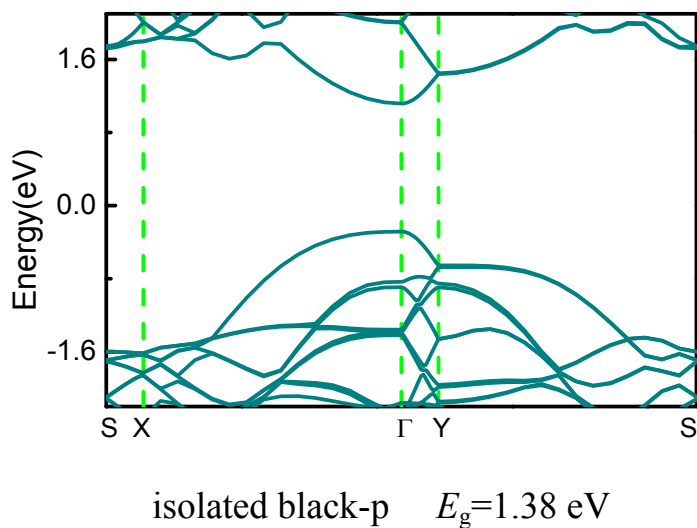
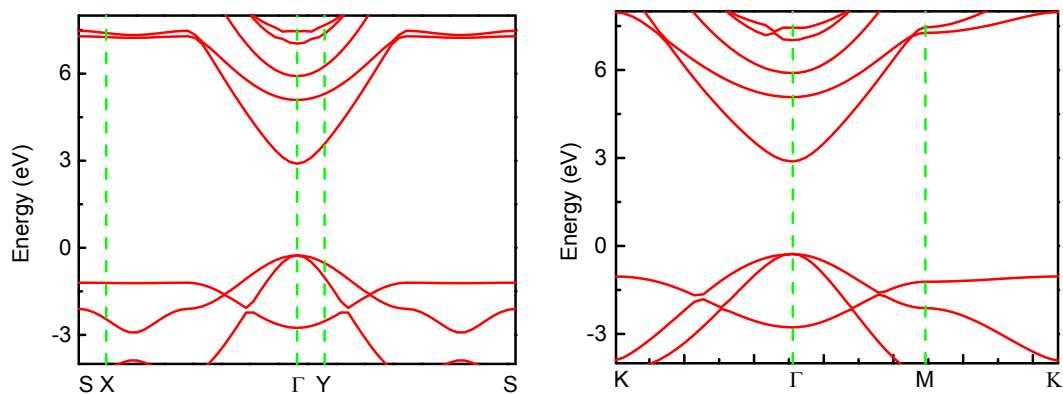
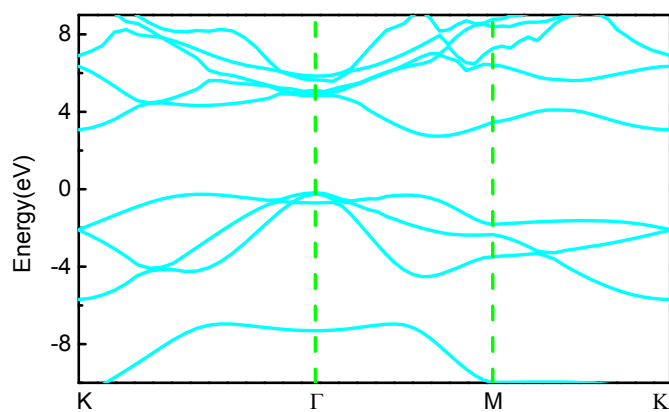


Fig. S3.1 Band structures of isolated black-p.



isolated g-ZnO  $E_g=3.29$  eV

Fig. S3.2 Band structures of isolated g-ZnO.



isolated blue-p  $E_g=2.86$  eV

Fig. S3.3 Band structures of isolated blue-p.

#### SI.4: Calculations of differential charge density.

$$\rho(x,y,z)$$

$\Delta\rho(z)$  without  $E$

$$\Delta\rho(z)=\int\rho(\text{blue-p/g-ZnO})dxdy-\int\rho(\text{blue-p})dxdy-\int\rho(\text{g-ZnO})dxdy \text{ (Eq. S4.1)}$$

$\rho(\text{blue-p})$  and  $\rho(\text{g-ZnO})$  are the charge density of blue-p and g-ZnO single-layer in the supercell of heterostructure, respectively.  $(x,y,z)$  denote the positions in the supercell.

$\Delta\rho_E(z)$  with  $E$

$$\Delta\rho_E(z)=\int\rho_E(\text{blue-p/g-ZnO})dxdy-\int\rho(\text{blue-p/g-ZnO})dxdy \text{ (Eq. S4.2)}$$

$\rho_E(\text{blue-p/g-ZnO})$  and  $\rho(\text{blue-p/g-ZnO})$  are the charge density of blue-p/g-ZnO with and without  $E$ .

**SI.5:** Evolution of band-gap of blue-p/g-ZnO with  $E$ .

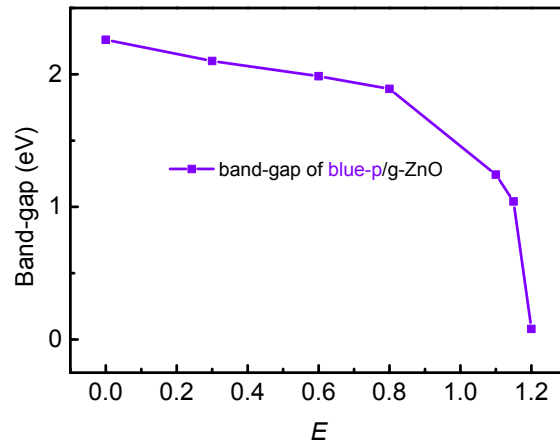


Fig. S5. Evolution of band-gap of blue-p/g-ZnO with  $E$ .